

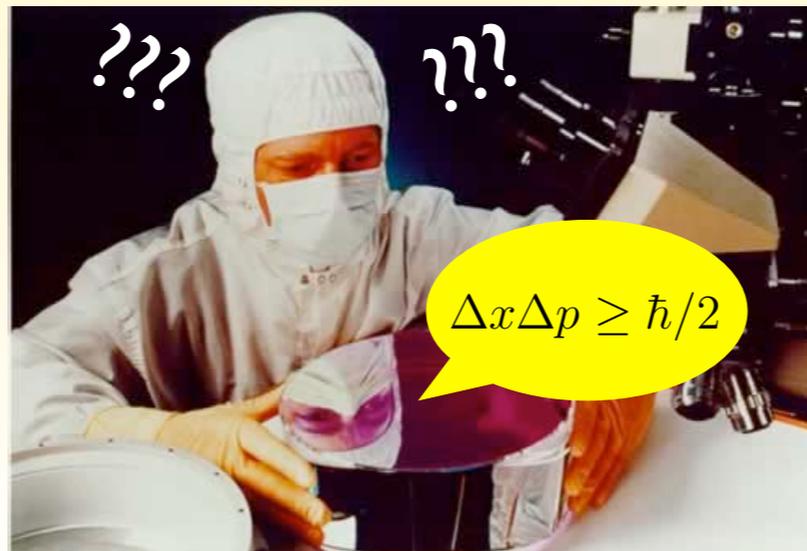
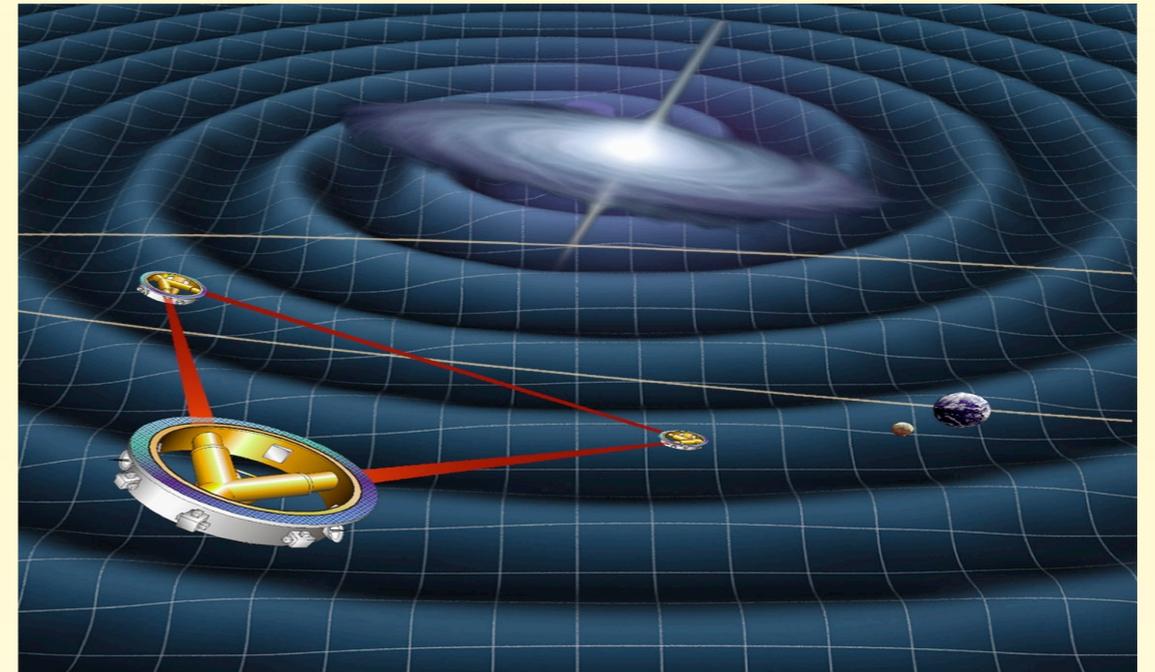
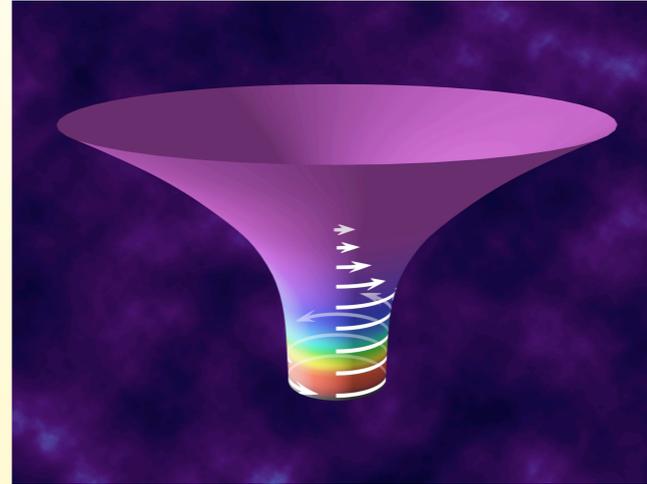
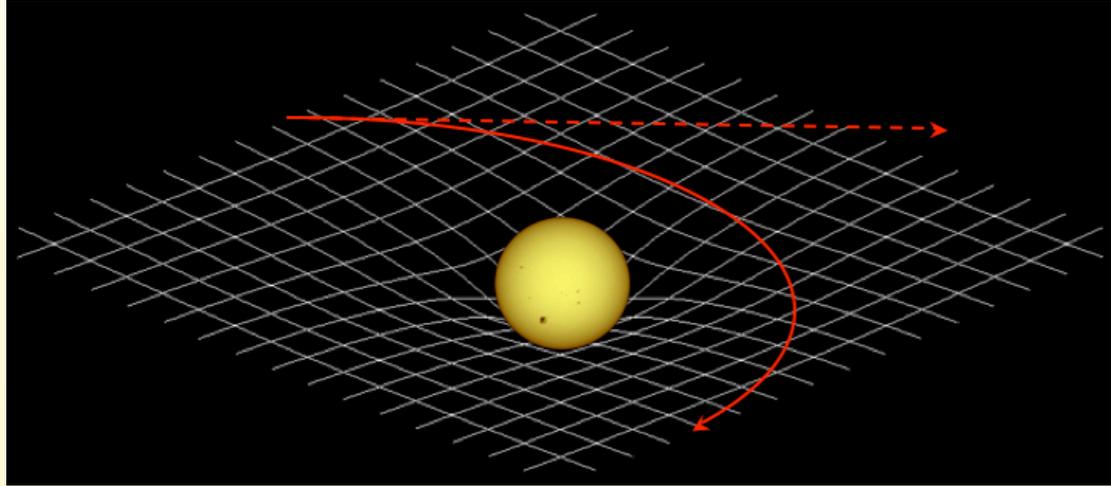
Gravitational-Wave Detection

SPACE-TIME WARPS IN THE UNIVERSE
QUANTUM UNCERTAINTIES OF MACROSCOPIC OBJECTS

Yanbei Chen
California Institute of Technology

Lyncean Group Meeting, San Diego, California
June 25, 2008

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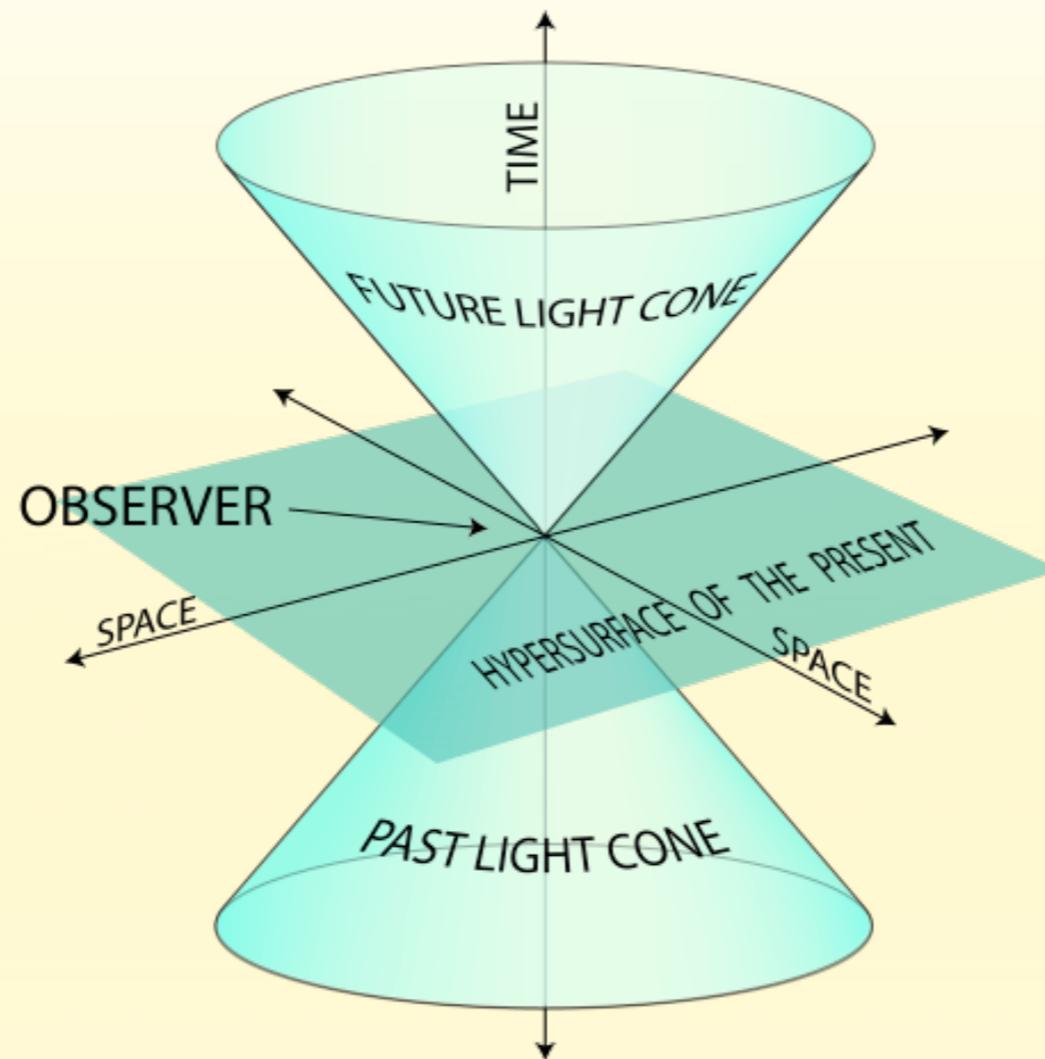
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- Ground-Based Gravitational-Wave Detector: LIGO
 - instrumentation
 - science
- Space-Based Gravitational-Wave Detector: LISA
 - instrumentation
 - science
- Using Gravitational-Wave Experiments to Study Quantum Mechanics

Special Relativity



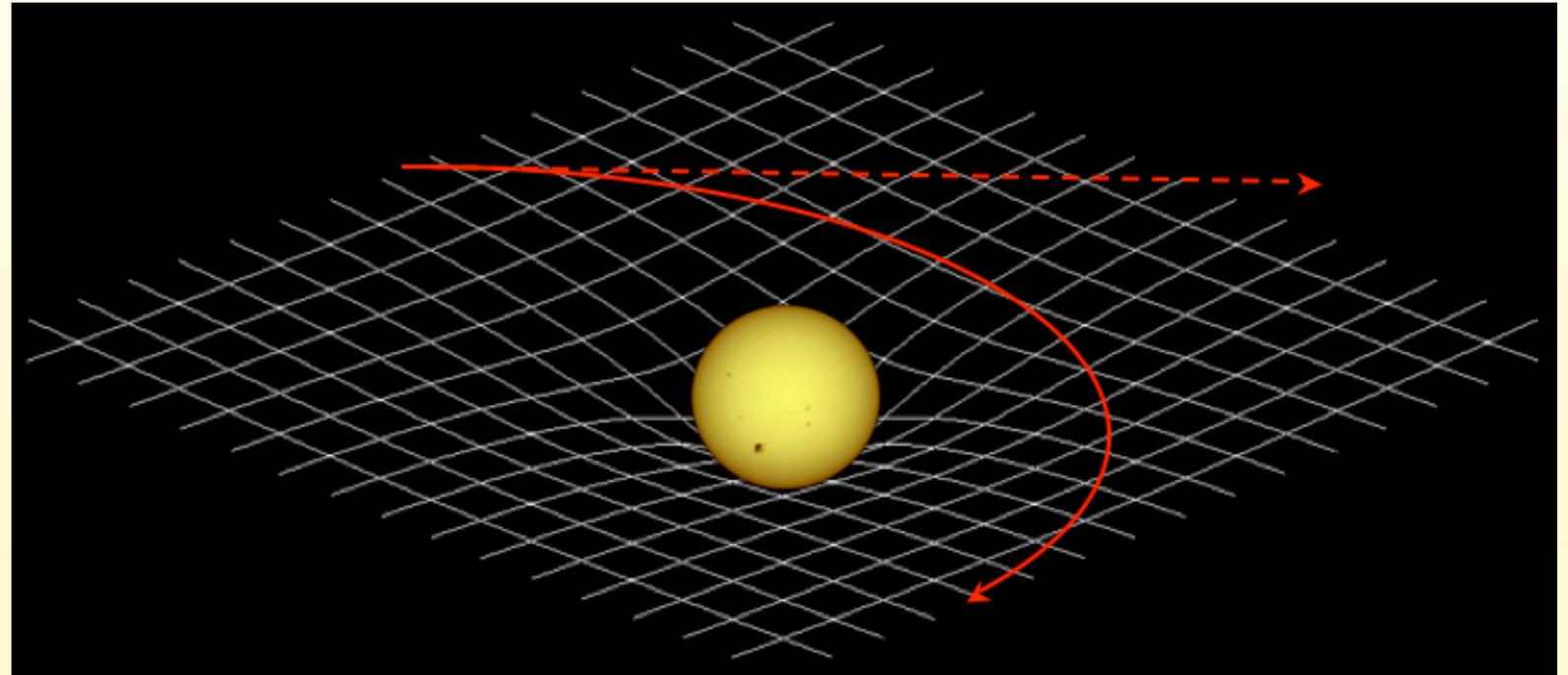
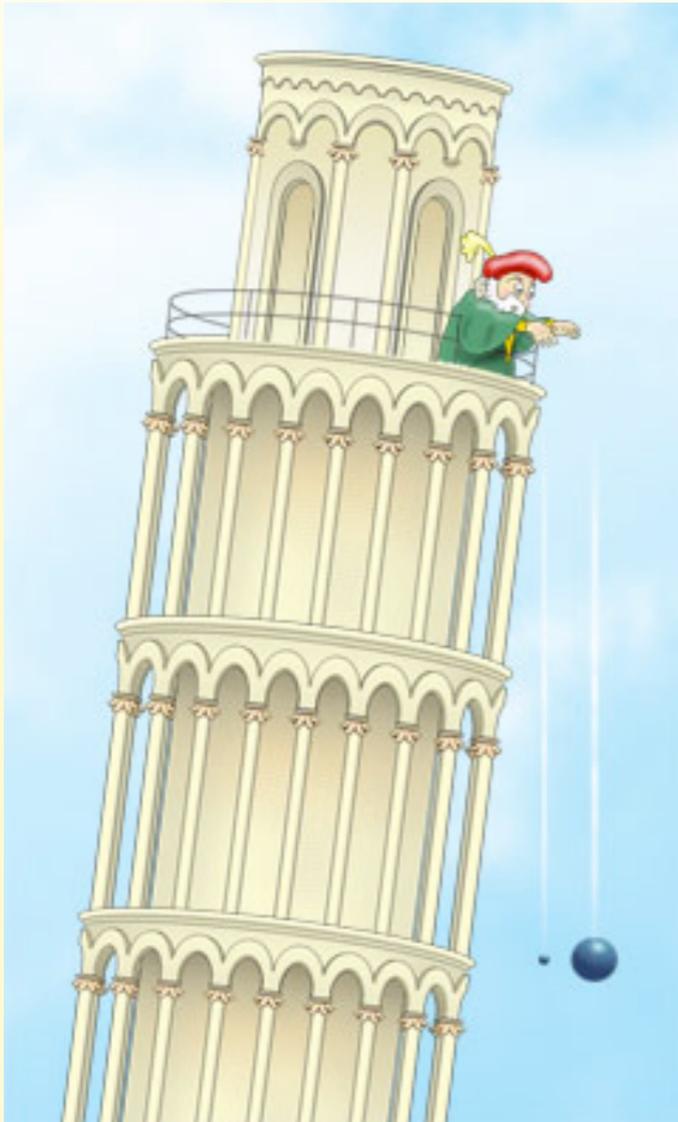
Albert Einstein



Hermann Minkowski

- Motivated by Maxwell's theory of Electromagnetism
- Unification of space and time: **spacetime**
- **The starting point for general relativity.**

General Relativity



- Motivation “Equivalence Principle”: everything fall with the same acceleration
- Gravity is Geometry, not a “force”

Einstein Field Equation

$$G_{\mu\nu} = 8\pi T_{\mu\nu}$$

Geometry

Matter

Conservation Law

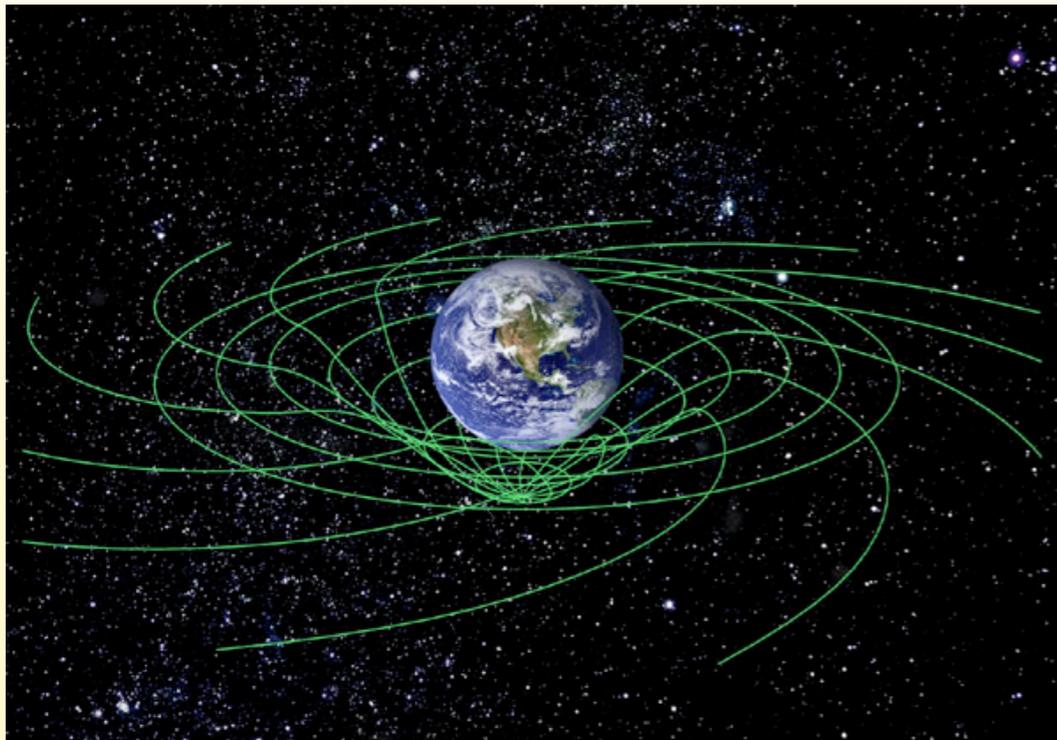
$$\nabla_{\mu} T^{\mu\nu} = 0$$

point particle follows
time-like geodesic

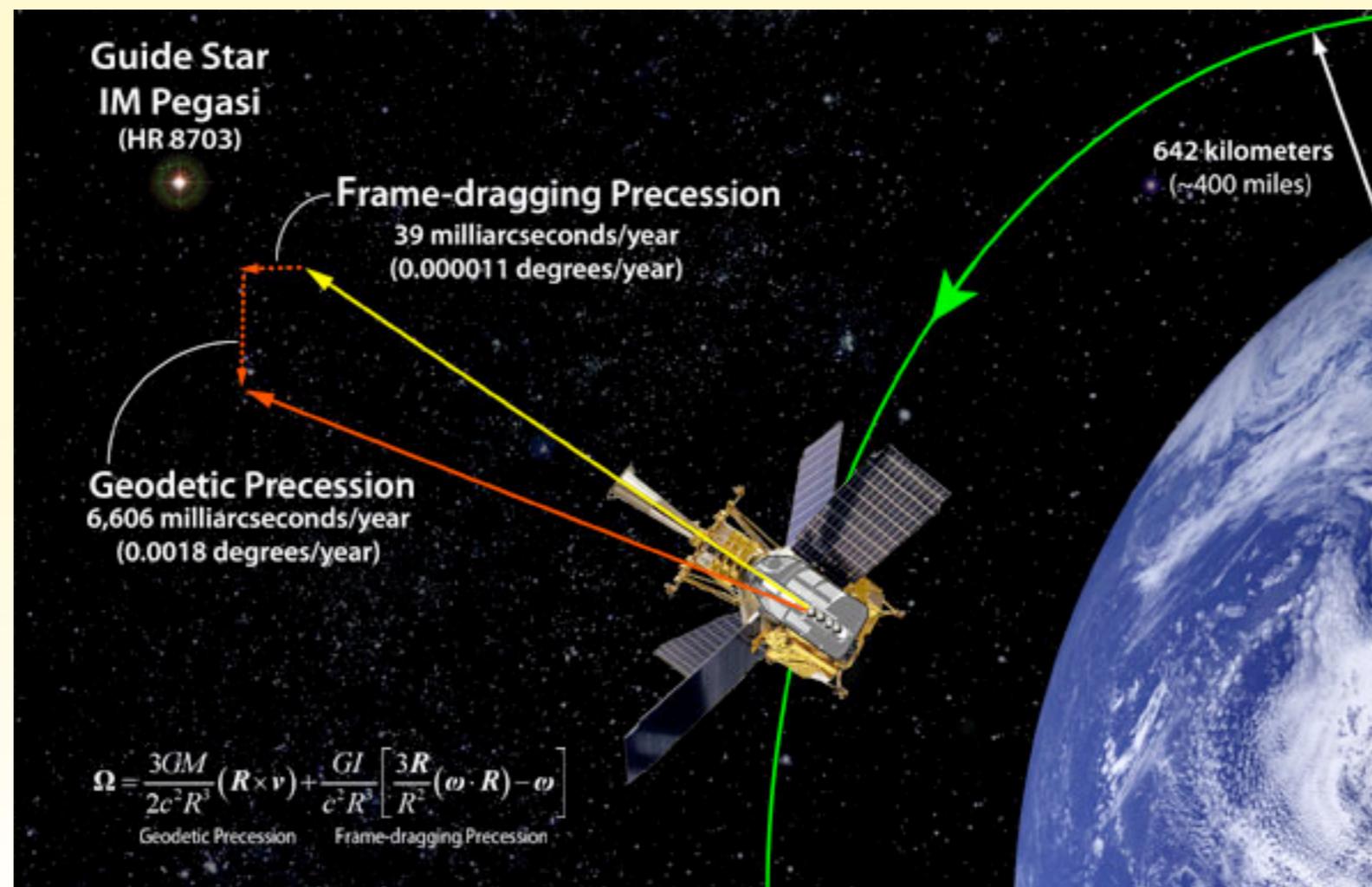


Gravitational Lens
Galaxy Cluster 0024+1654
Hubble Space Telescope • WFPC2

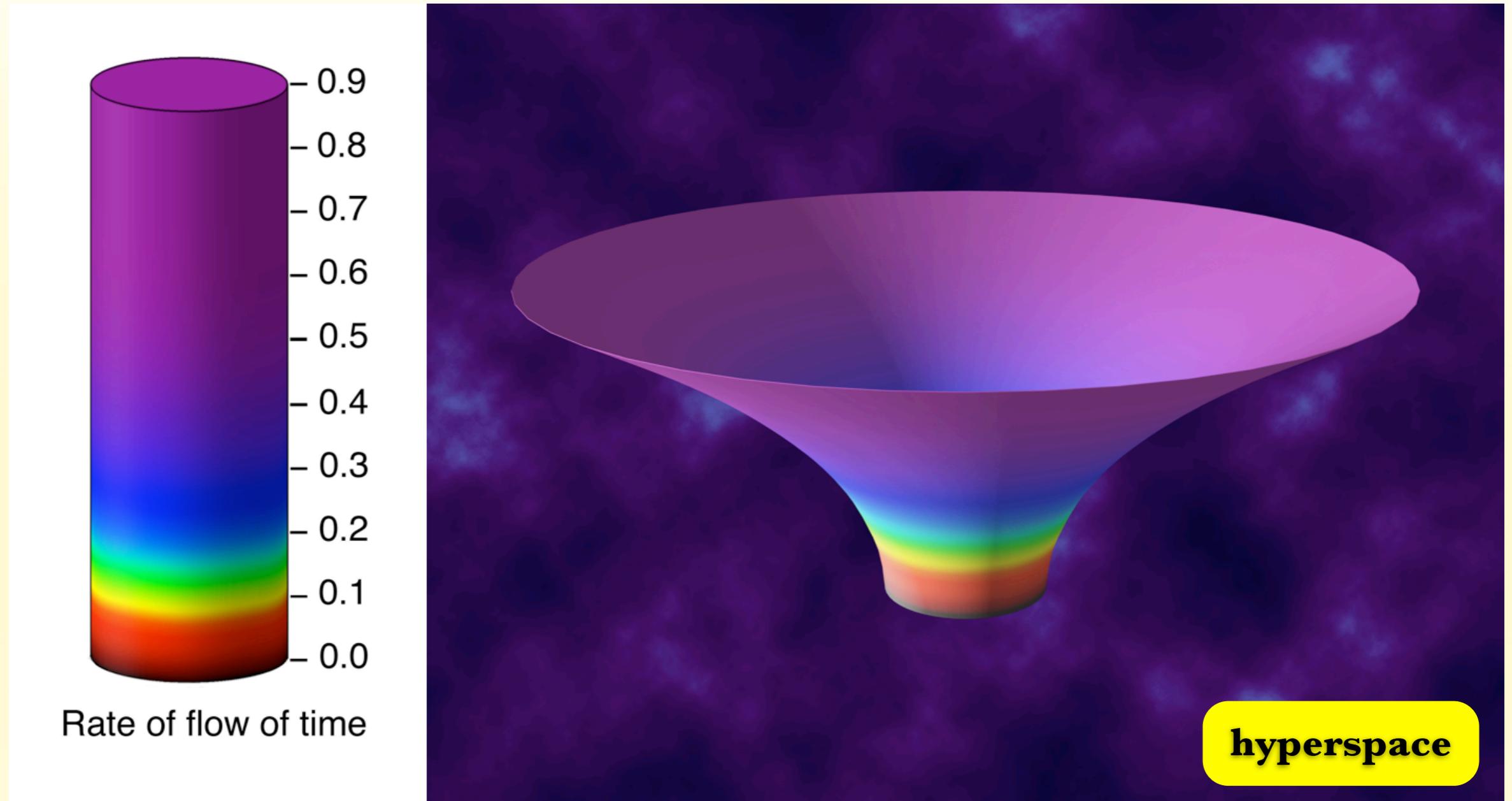
Weak-Field Predictions of GR



- Mass and rotation of the earth cause warp and whirl of nearby spacetime
- Gravity Probe B: aims at detecting both, using precession of gyroscopes.
- Warp already verified, whirl is more difficult ...

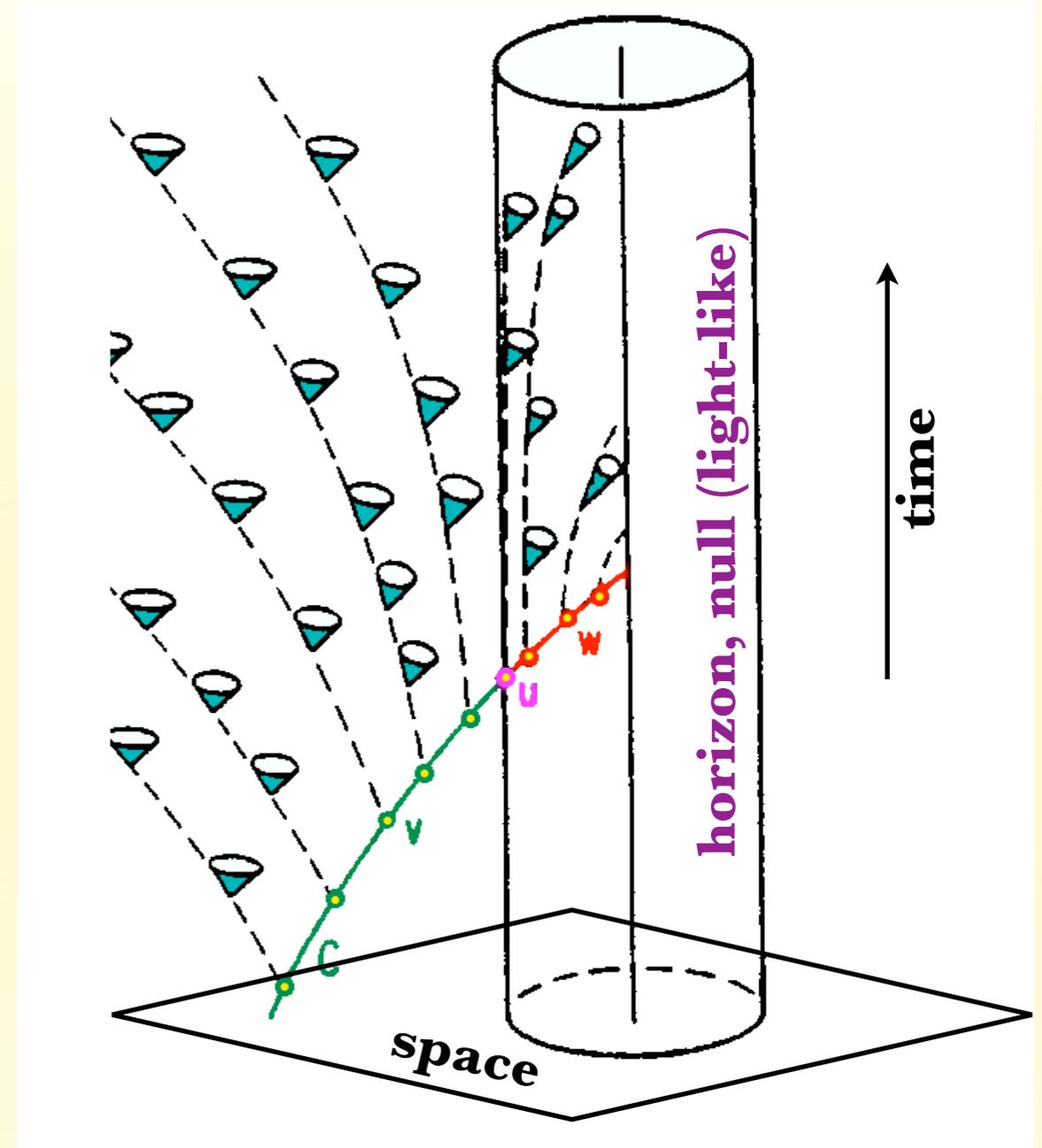
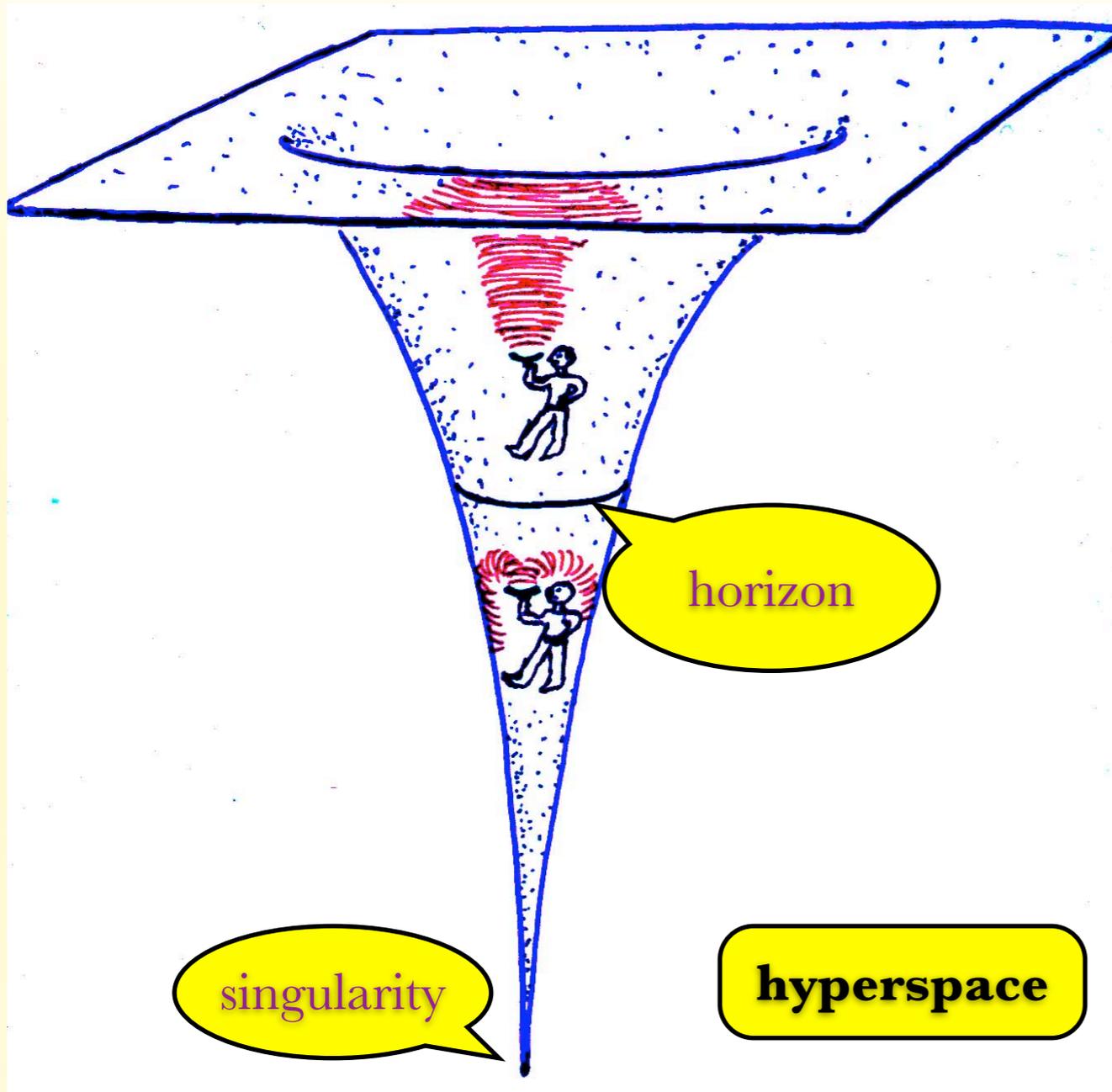


Black Holes: Pure, Nonlinear Spacetime



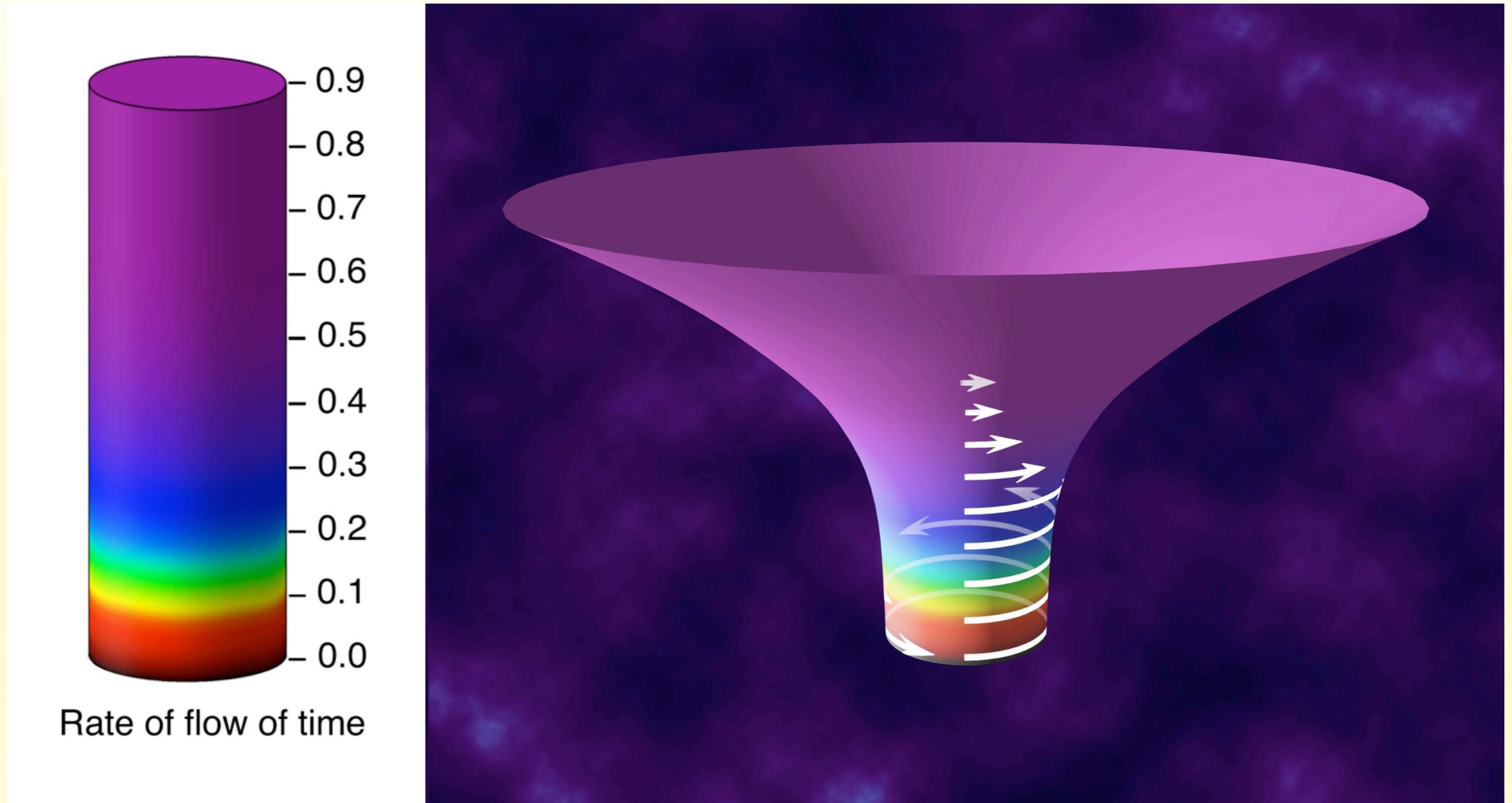
- Warp of spacetime: $\text{circumference} > 2\pi \times \text{radius}$, time slows

Black Holes: Pure Nonlinear Spacetime



- Warp of spacetime: circumference $> 2\pi \times$ radius, time slows
- Horizon: surface of no-escape

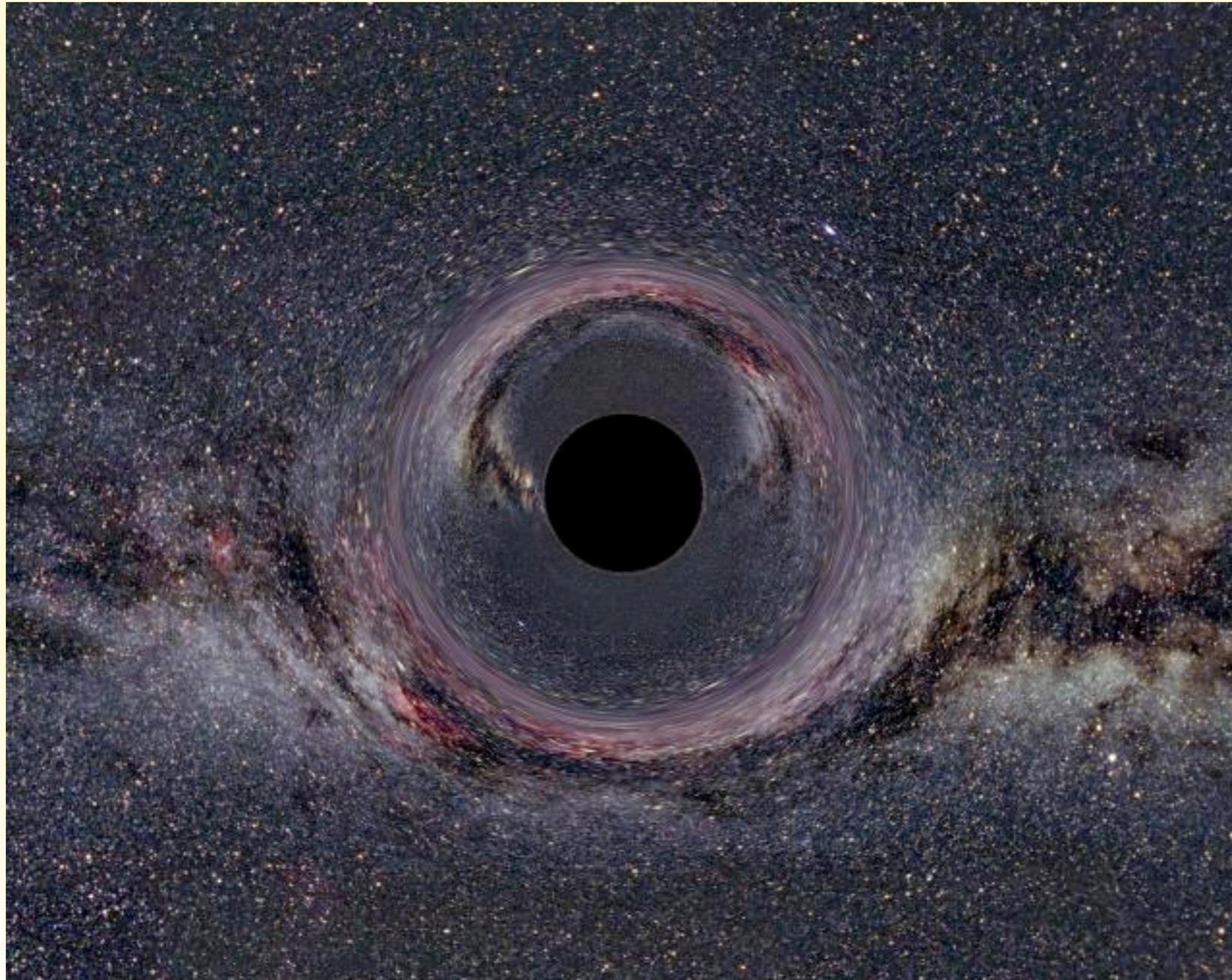
Black Holes: Pure Nonlinear Spacetime



- Warp of spacetime: $\text{circumference} > 2\pi \times \text{radius}$, time slows
- Horizon: surface of no-escape
- Whirl of spacetime: nobody can stay non-rotating within the ergosphere

Formations of Black Holes

- **Black Holes** can form as final stage of stellar evolution
 - low-mass stars (like the sun) end up as **White Dwarf** stars
 - higher mass end up as **Neutron Stars**
 - massive stars (initially above 20 solar masses) end up as **Black Holes**

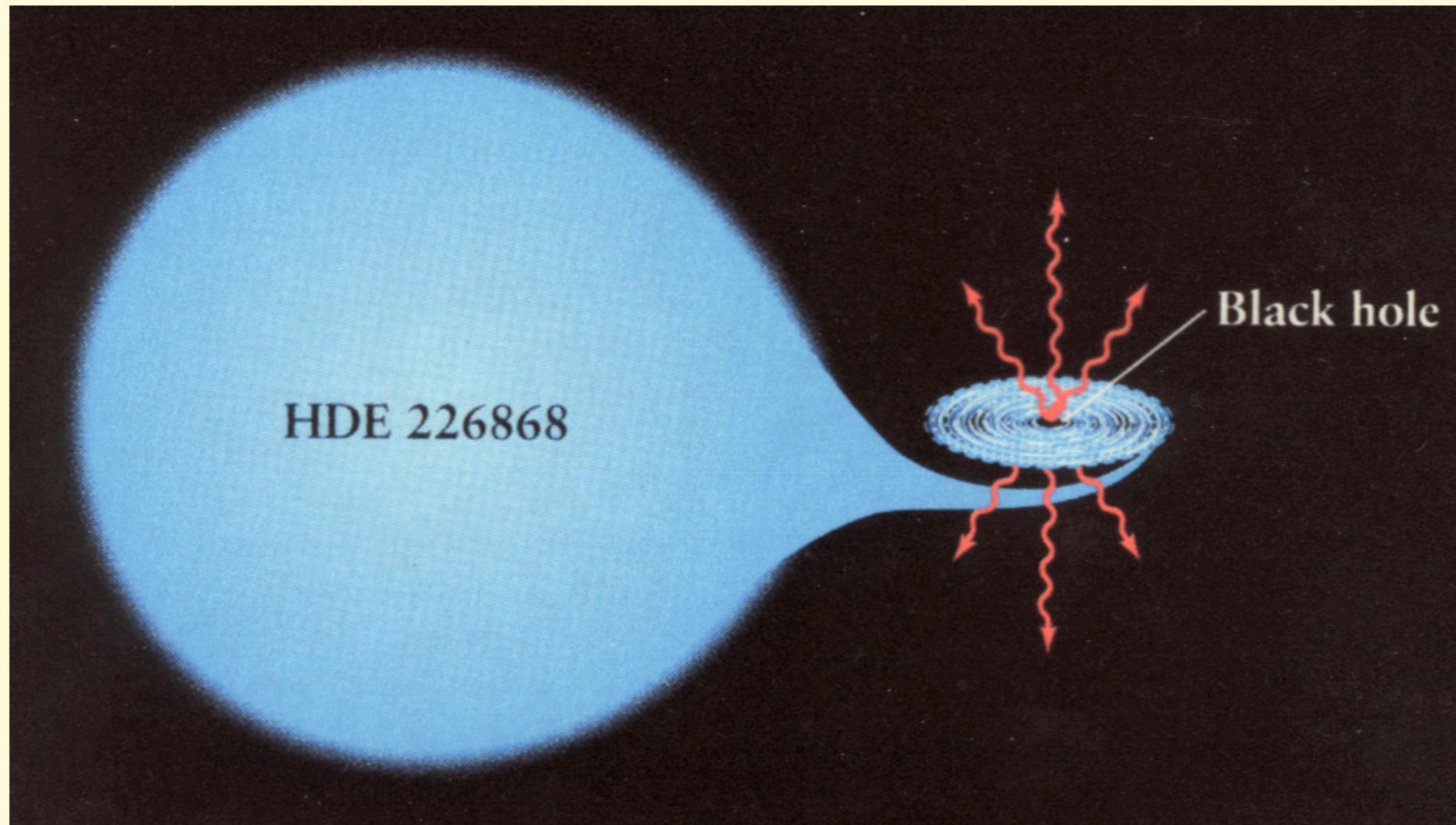


10 Solar Mass Schwarzschild
Black Hole (“size” = 30km)
viewed from 600 km away

Simulation by Ute Kraus,
Max-Planck Institute and
University of Tübingen

<http://spacetime.travel.org>

Stellar-Mass Black Holes

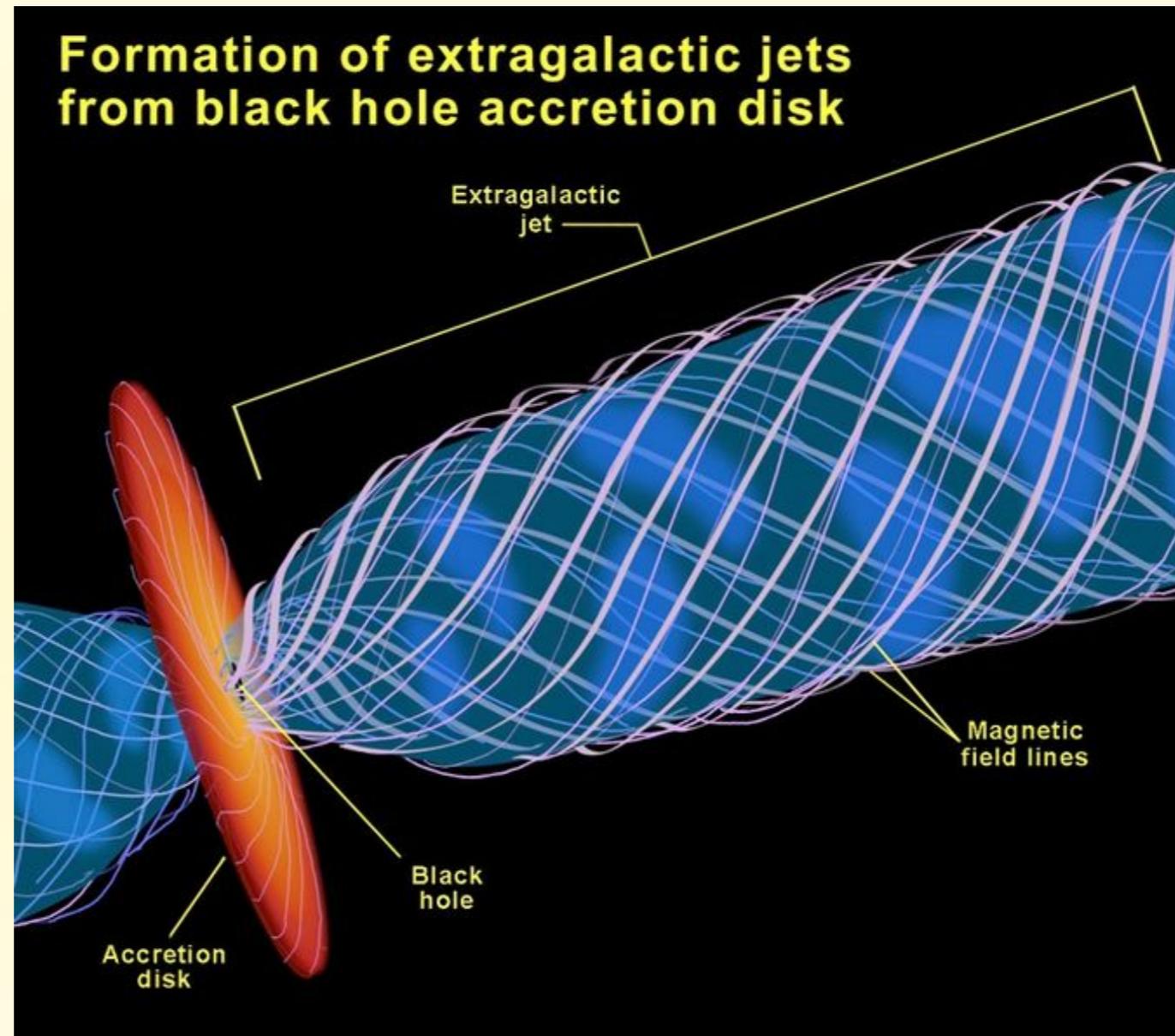


Black Holes are observable when they are in binaries

Primary criterion for being BH: mass > 3 solar mass

Supermassive Black Holes

- **Quasars** (1960s): supermassive Black Holes at centers of galaxies, with mass accretion



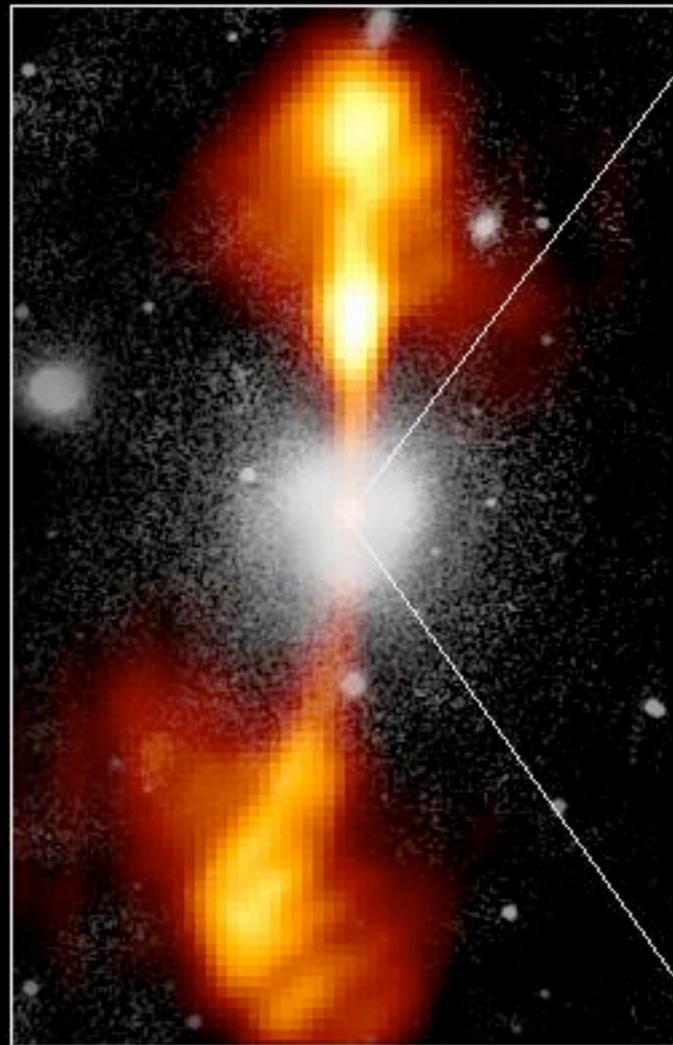
- 1% of all Galaxies are Active
- Every “respectable” nearby galaxy has a central black hole
- Origin of these black holes? Not entirely clear.

Core of Galaxy NGC 4261

Hubble Space Telescope

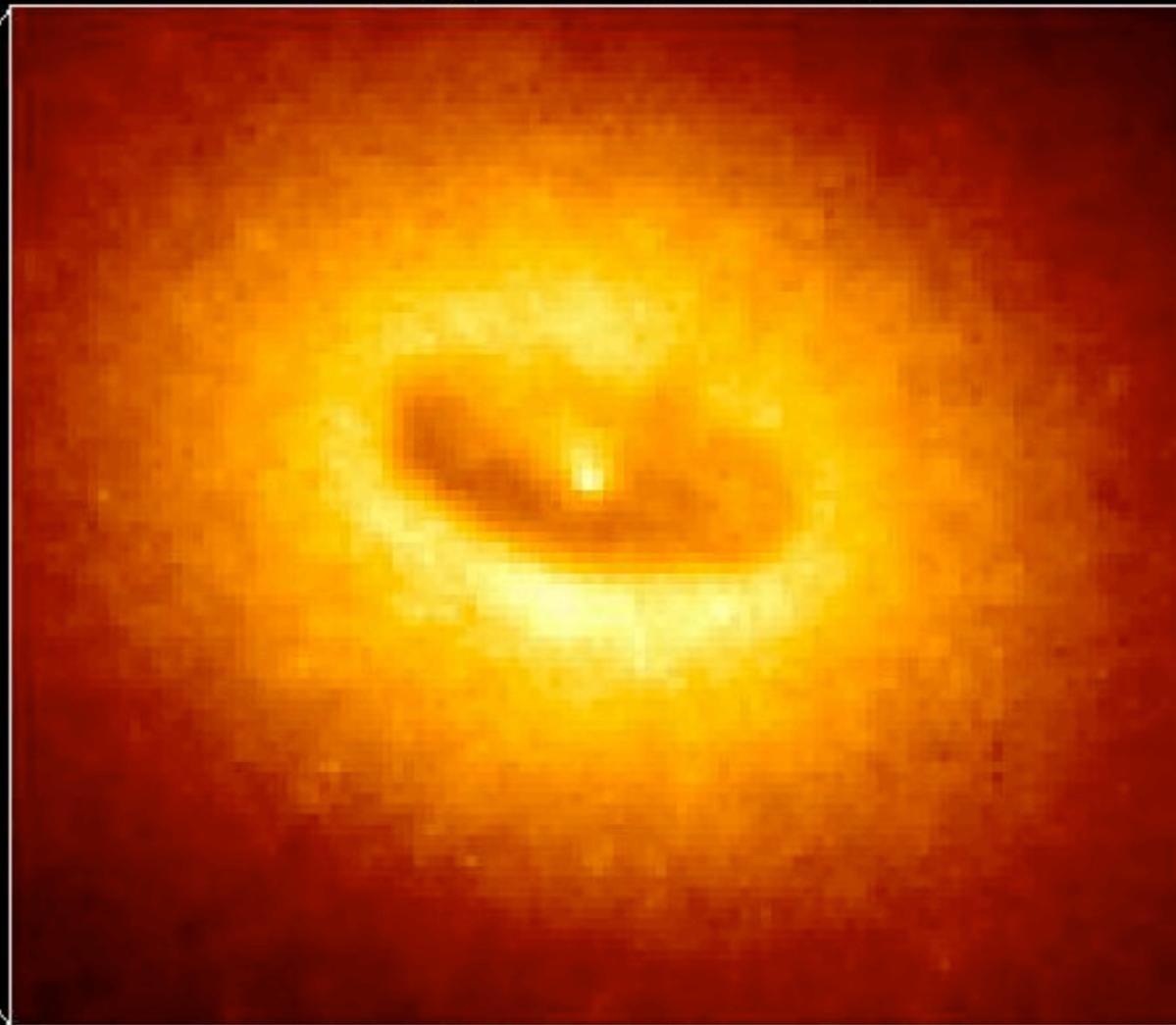
Wide Field / Planetary Camera

Ground-Based Optical/Radio Image



380 Arc Seconds
88,000 LIGHT-YEARS

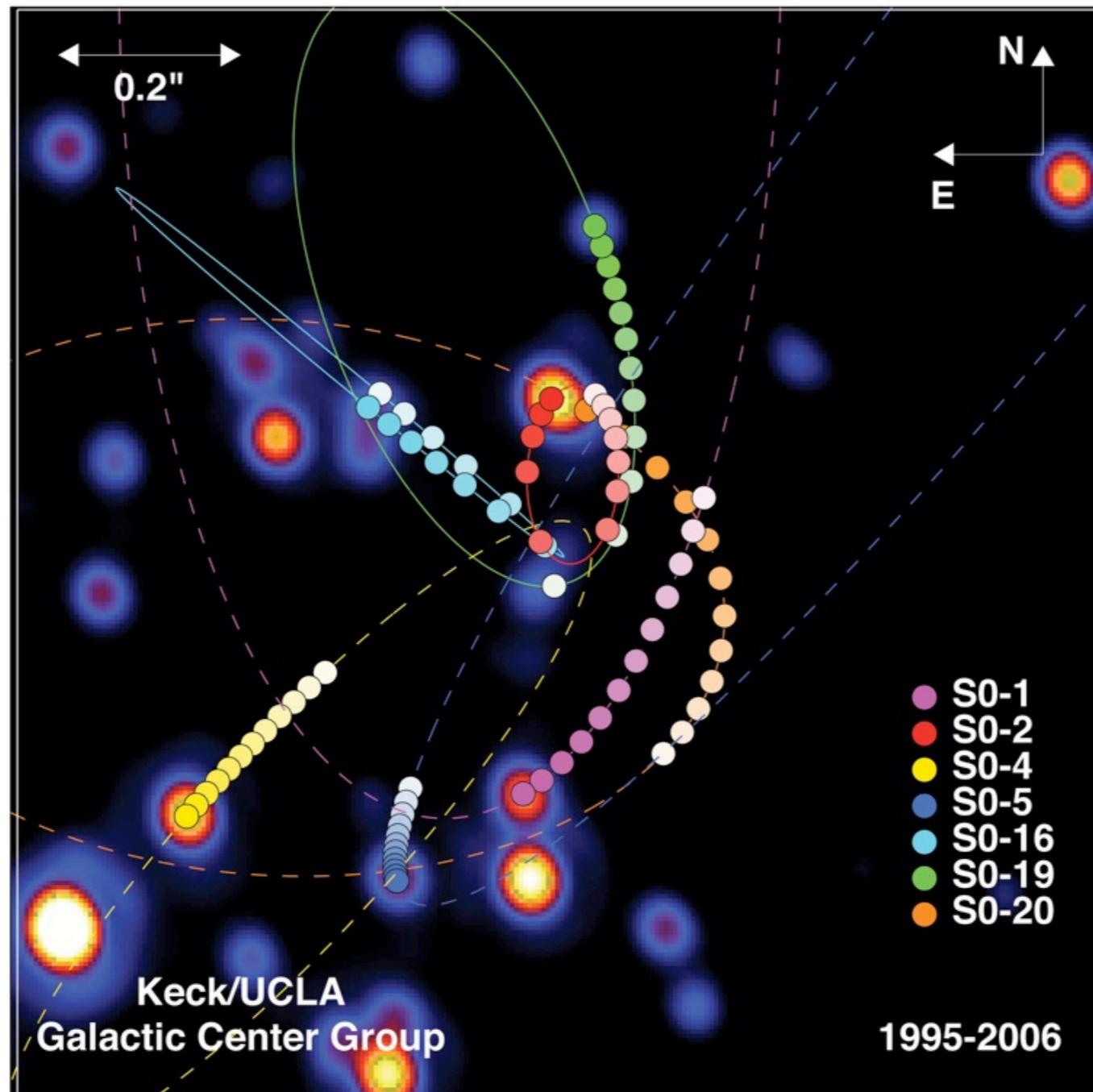
HST Image of a Gas and Dust Disk



17 Arc Seconds
400 LIGHT-YEARS

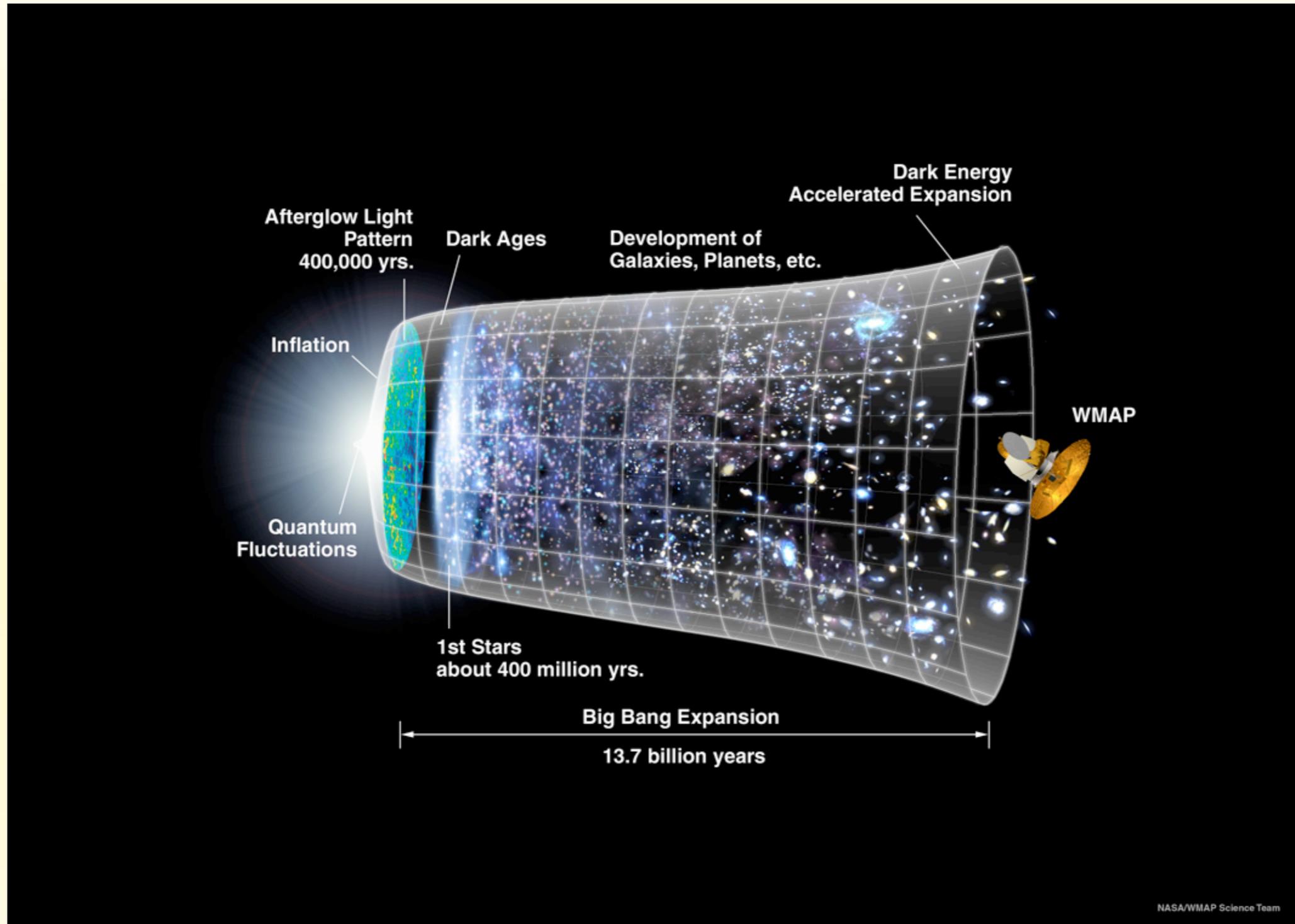
in the Virgo cluster, 59 Mly, or 18 Mpc

The Milky Way Black Hole



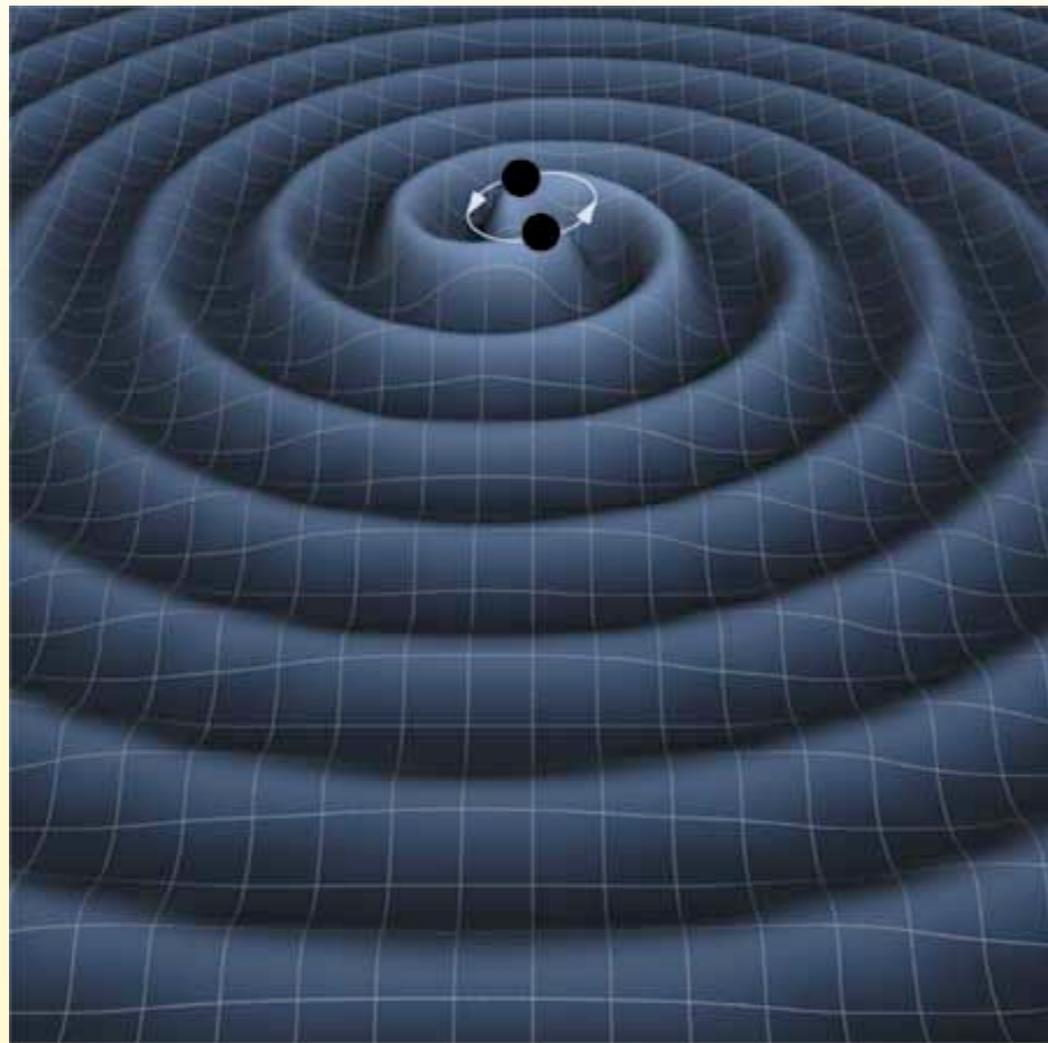
$M = 4$ Million Solar Masses

Cosmology, and the “Big Bang”



- General relativity also describes the dynamics of the universe

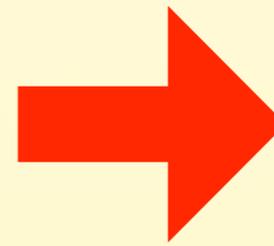
Gravitational Waves



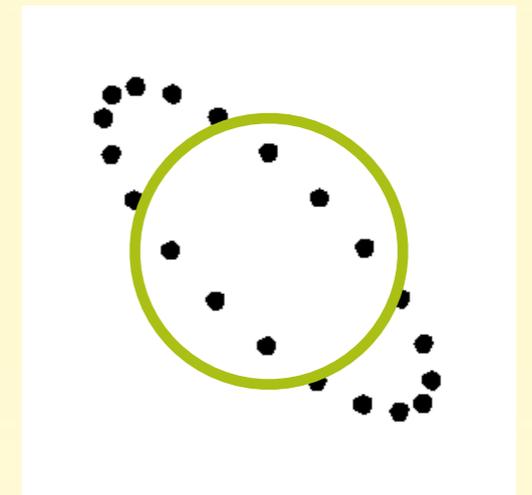
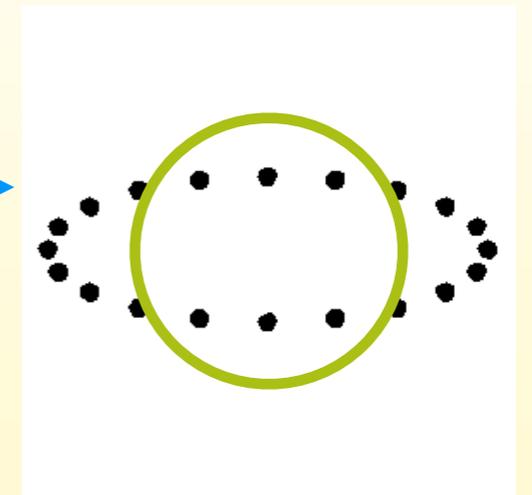
generation

distance = d

$$h \sim H/d$$



nearly free
propagation
(almost
unaffected by
matter)

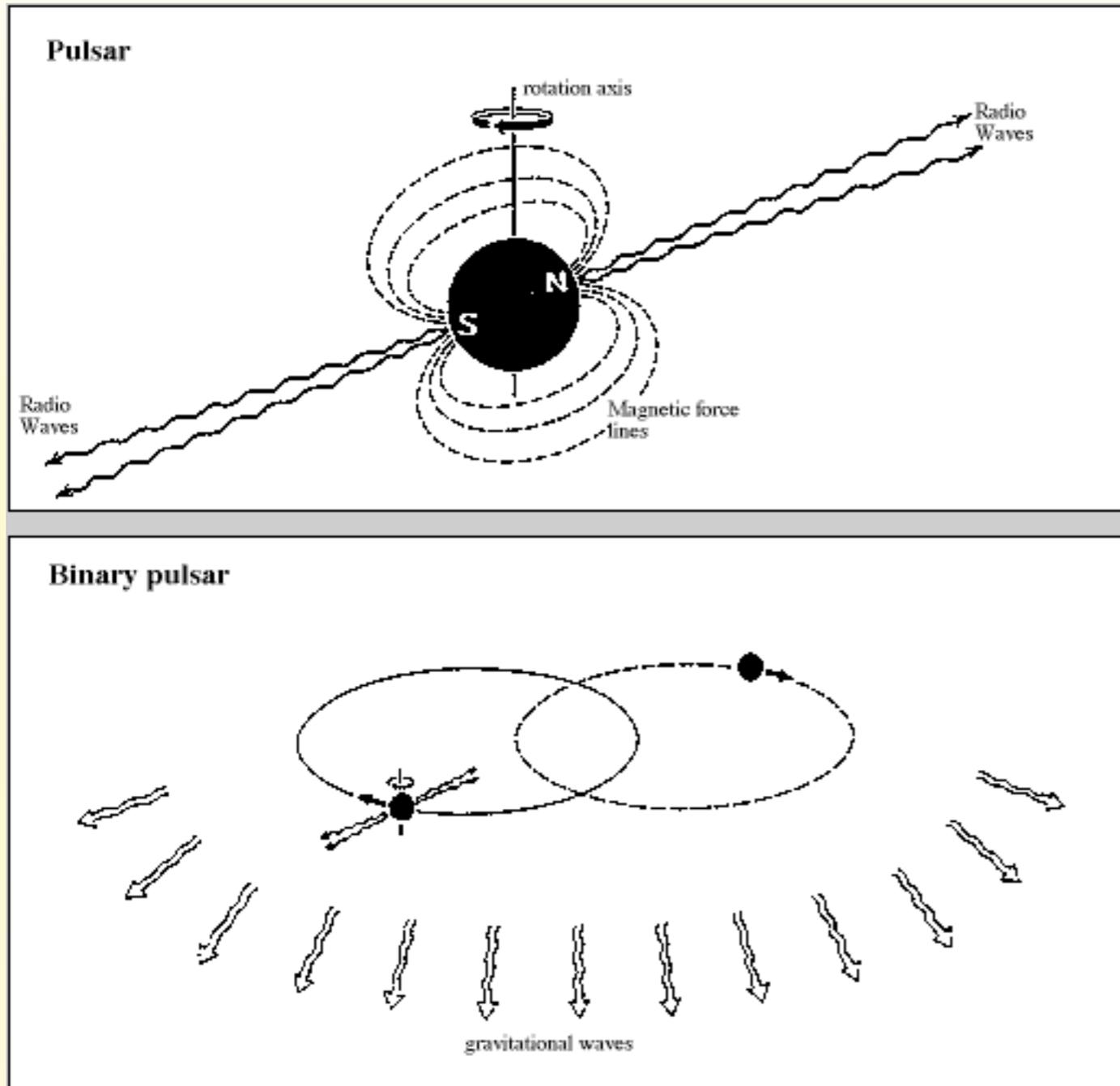


effect on free test masses

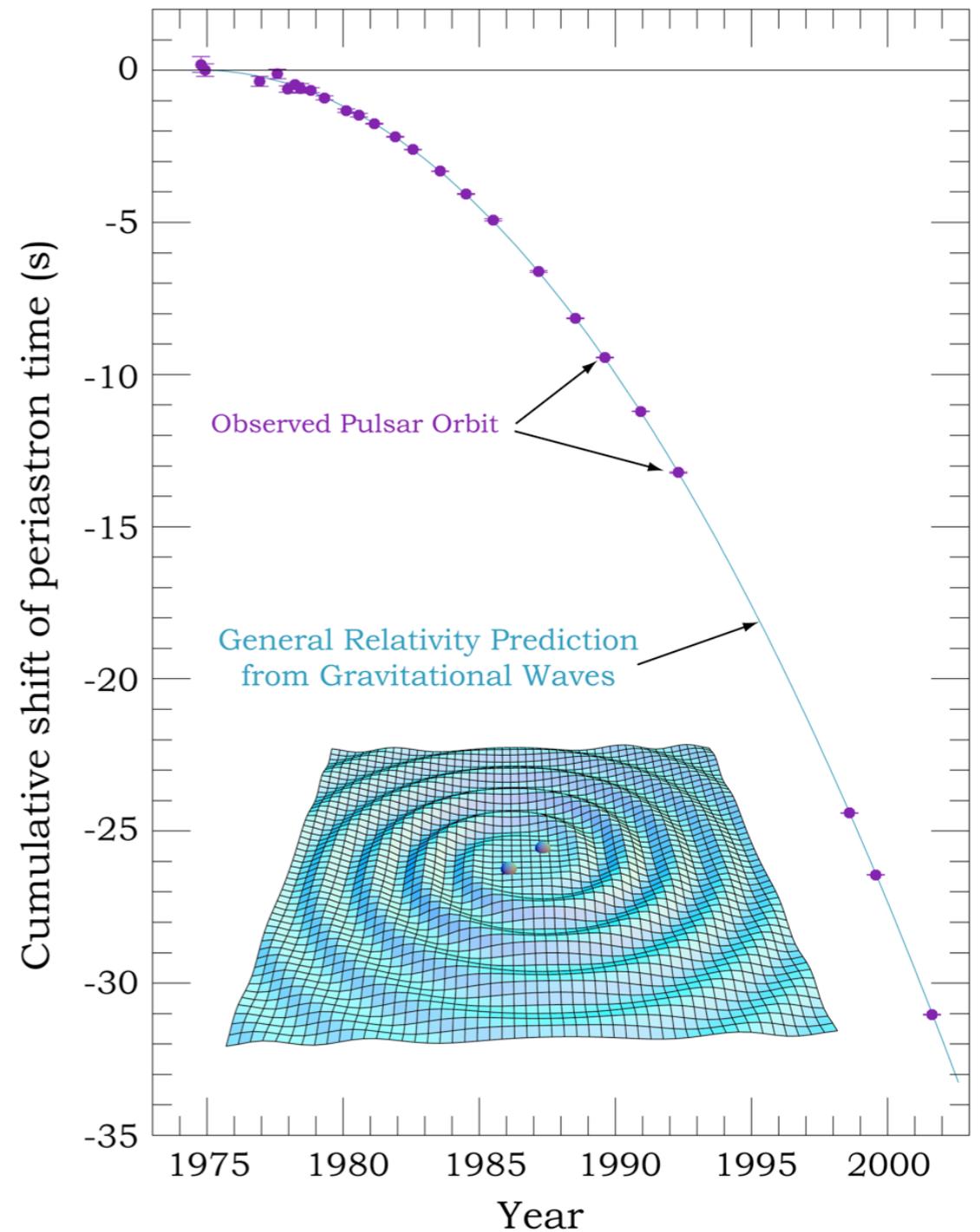
$$\Delta L \sim L h$$

- Oscillations of spacetime itself; generated by accelerated mass
- Propagates at speed of light
- Carry energy, momentum (similar to electromagnetic waves)
- Two polarizations

Evidence of Gravitational Radiation



Relativistic Binary Pulsars



http://www.srl.caltech.edu/lisa/graphics/LISA_science.html

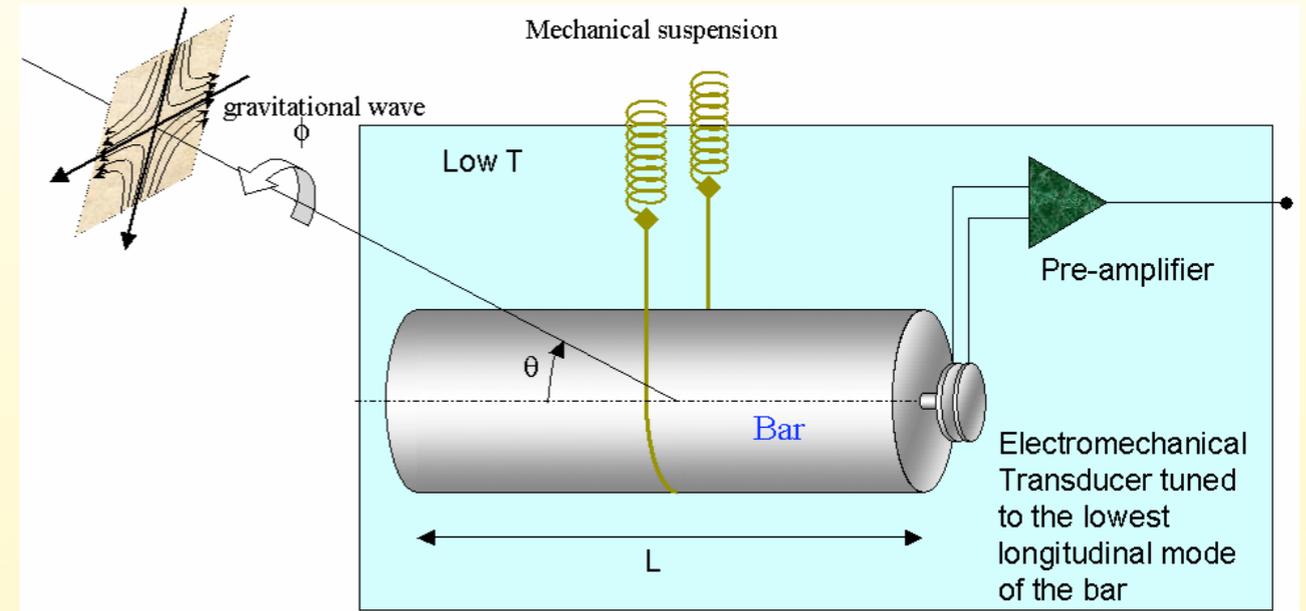
Data from Hulse-Taylor Pulsar

... will eventually merge in 85 Myrs

Early Days: Bar Detectors

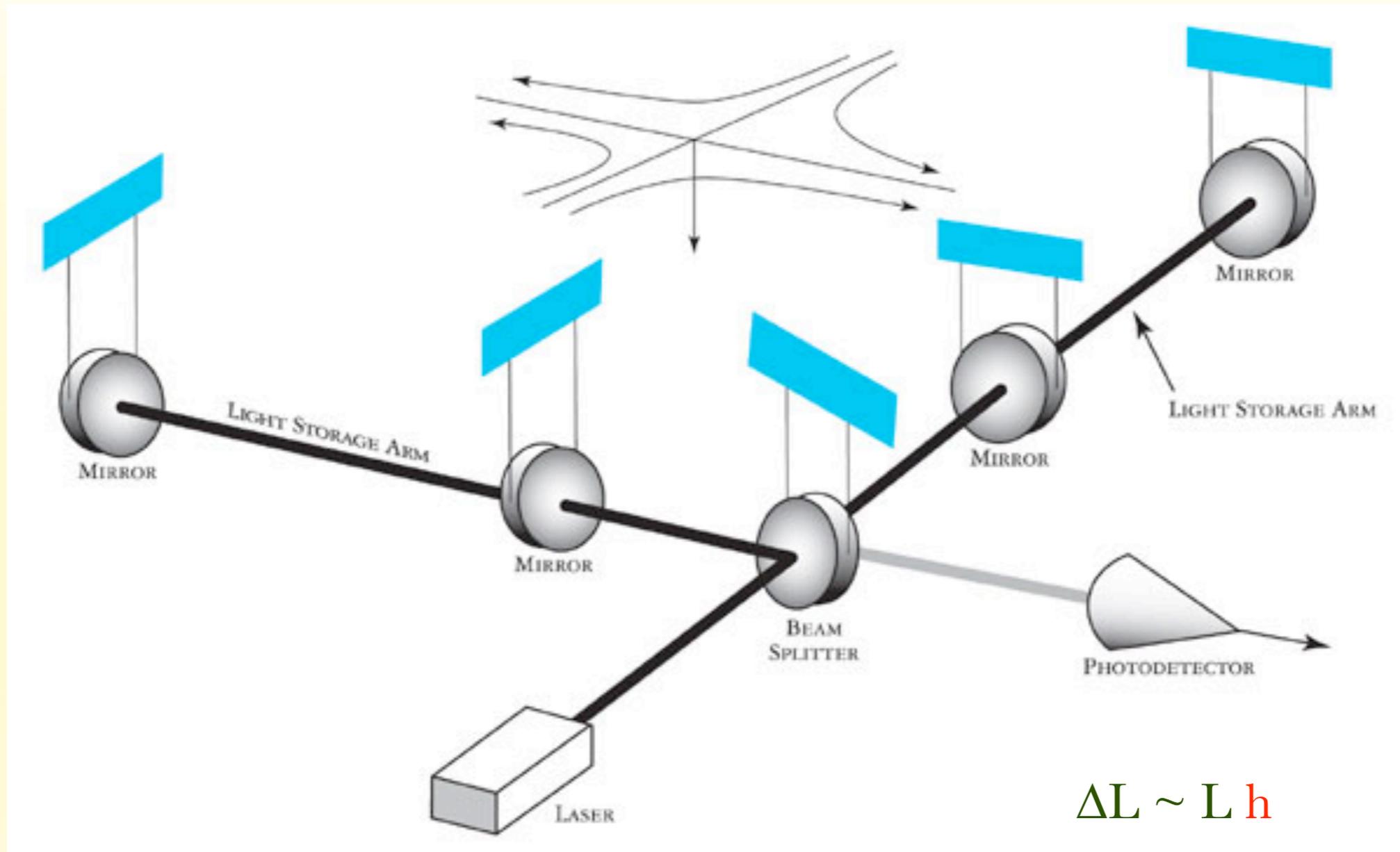


UNIVERSITY OF MARYLAND



- Resonant mass detector, invented by Joe Weber, 1960s. (Amplification around resonance)
- Claimed detections, but not verified.
- Modern bars stopped operations recently, replaced by laser interferometers

Laser Interferometers

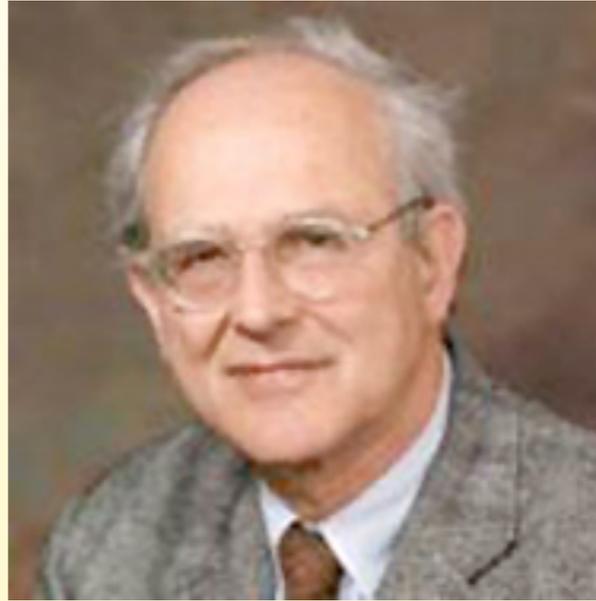


- Comprehensive proposal by Rainer Weiss in 1972. *[In the USSR, Postovoi and Gertsenshtein, but not comprehensive ...]*
- Long arms (4 km = 2.5 miles): broadband amplification
- Sensing by laser light, with resonant enhancement

Laser Interferometer Gravitational-wave Observatory (LIGO)



Ronold Drever
Glasgow, then Caltech



Rainer Weiss
MIT



Kip Thorne
Caltech

- Funded by the NSF in 1992, operated by Caltech and MIT
- \$365M, largest project ever funded by the NSF
- “LIGO Scientific Collaboration” includes ~ 500 scientists
- Finished one year of operation, “Enhanced LIGO” starts 2009, with 2-3 times sensitivity
- \$205M for upgrade to Advanced LIGO, with 15 times sensitivity (start operation in 2014)

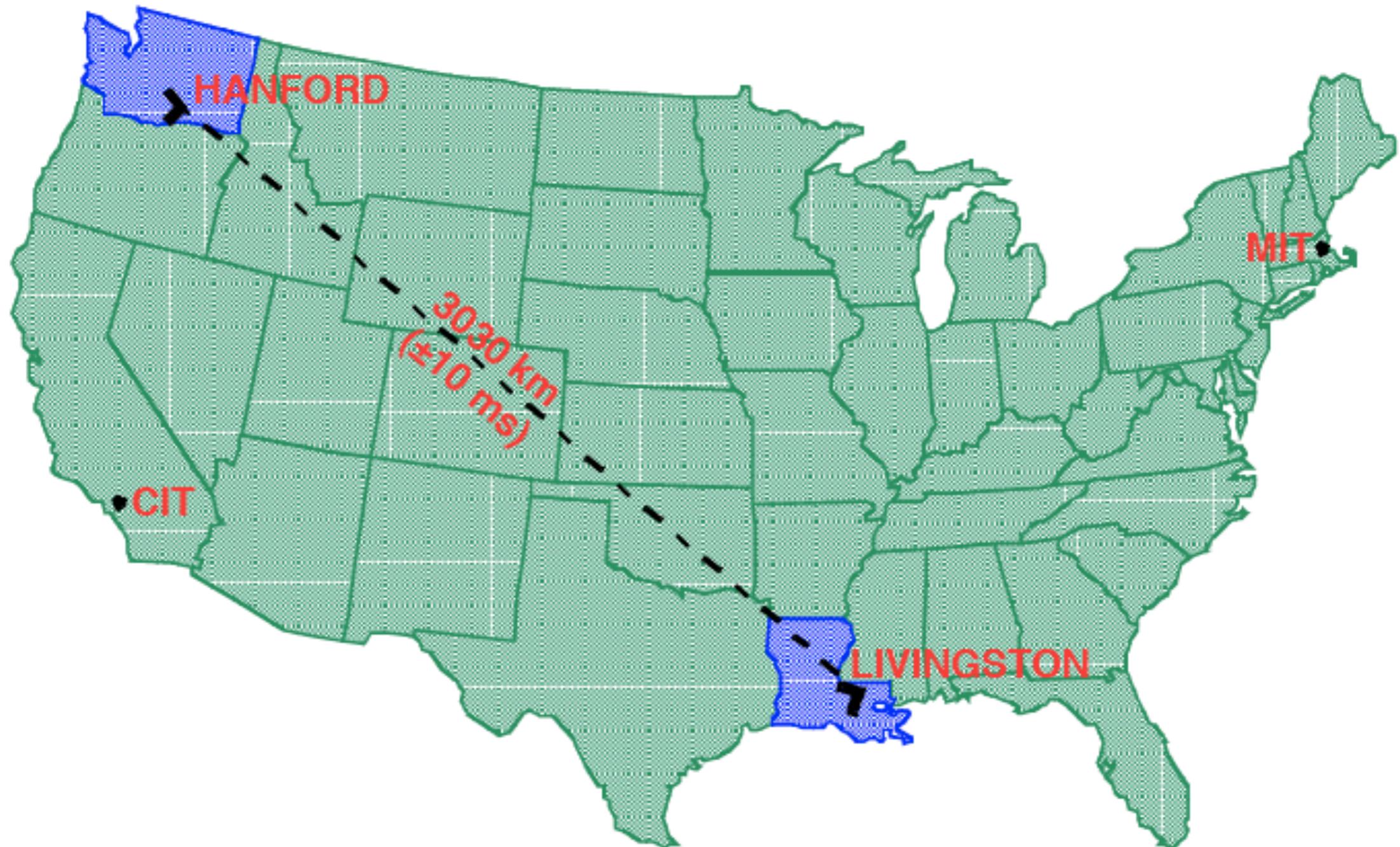
IMPLICATIONS FOR THE ORIGIN OF GRB 070201 FROM LIGO OBSERVATIONS

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The LIGO Scientific Collaboration, <http://www.ligo.org>

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- ³ Andrews University, Berrien Springs, MI 49104 USA
- ⁴ Australian National University, Canberra, 0200, Australia
- ⁵ California Institute of Technology, Pasadena, CA 91125, USA
- ⁶ Caltech-CaRT, Pasadena, CA 91125, USA
- ⁷ Cardiff University, Cardiff, CF24 3AA, United Kingdom
- ⁸ Carleton College, Northfield, MN 55057, USA
- ⁹ Charles Sturt University, Wagga Wagga, NSW 2678, Australia
- ¹⁰ Columbia University, New York, NY 10027, USA
- ¹¹ Embry-Riddle Aeronautical University, Prescott, AZ 86301 USA
- ¹² Hobart and William Smith Colleges, Geneva, NY 14456, USA
- ¹³ Inter-University Centre for Astronomy and Astrophysics, Pune - 411007, India
- ¹⁴ LIGO - California Institute of Technology, Pasadena, CA 91125, USA
- ¹⁵ LIGO Hanford Observatory, Richland, WA 99352, USA
- ¹⁶ LIGO Livingston Observatory, Livingston, LA 70754, USA
- ¹⁷ LIGO - Massachusetts Institute of Technology, Cambridge, MA 02139, USA
- ¹⁸ Louisiana State University, Baton Rouge, LA 70803, USA
- ¹⁹ Louisiana Tech University, Ruston, LA 71272, USA
- ²⁰ Loyola University, New Orleans, LA 70118, USA
- ²¹ Moscow State University, Moscow, 119992, Russia
- ²² NASA/Goddard Space Flight Center, Greenbelt, MD 20771, USA
- ²³ National Astronomical Observatory of Japan, Tokyo 181-8588, Japan
- ²⁴ Northwestern University, Evanston, IL 60208, USA
- ²⁵ Rochester Institute of Technology, Rochester, NY 14623, USA
- ²⁶ Rutherford Appleton Laboratory, Chilton, Didcot, Oxon OX11 0QX United Kingdom
- ²⁷ San Jose State University, San Jose, CA 95192, USA
- ²⁸ Southeastern Louisiana University, Hammond, LA 70402, USA
- ²⁹ Southern University and A&M College, Baton Rouge, LA 70813, USA
- ³⁰ Stanford University, Stanford, CA 94305, USA
- ³¹ Syracuse University, Syracuse, NY 13244, USA
- ³² The Pennsylvania State University, University Park, PA 16802, USA
- ³³ The University of Texas at Brownsville and Texas Southmost College, Brownsville, TX 78520, USA
- ³⁴ Trinity University, San Antonio, TX 78212, USA
- ³⁵ Universitat de les Illes Balears, E-07122 Palma de Mallorca, Spain
- ³⁶ Universität Hannover, D-30167 Hannover, Germany
- ³⁷ University of Adelaide, Adelaide, SA 5005, Australia
- ³⁸ University of Birmingham, Birmingham, B15 2TT, United Kingdom
- ³⁹ University of Florida, Gainesville, FL 32611, USA
- ⁴⁰ University of Glasgow, Glasgow, G12 8QQ, United Kingdom
- ⁴¹ University of Maryland, College Park, MD 20742 USA
- ⁴² University of Michigan, Ann Arbor, MI 48109, USA
- ⁴³ University of Oregon, Eugene, OR 97403, USA
- ⁴⁴ University of Rochester, Rochester, NY 14627, USA
- ⁴⁵ University of Salerno, 84084 Fisciano (Salerno), Italy
- ⁴⁶ University of Sannio at Benevento, I-82100 Benevento, Italy
- ⁴⁷ University of Southampton, Southampton, SO17 1BJ, United Kingdom
- ⁴⁸ University of Strathclyde, Glasgow, G1 1XQ, United Kingdom
- ⁴⁹ University of Washington, Seattle, WA, 98195
- ⁵⁰ University of Western Australia, Crawley, WA 6009, Australia
- ⁵¹ University of Wisconsin-Milwaukee, Milwaukee, WI 53201, USA
- ⁵² Washington State University, Pullman, WA 99164, USA

LIGO Sites



Reason for two detectors: **coincident detection, and localization of source**

LIGO Hanford Observatory



Hanford, WA (near Pasco-Richland-Kennewick, WA)

LIGO Livingston Observatory

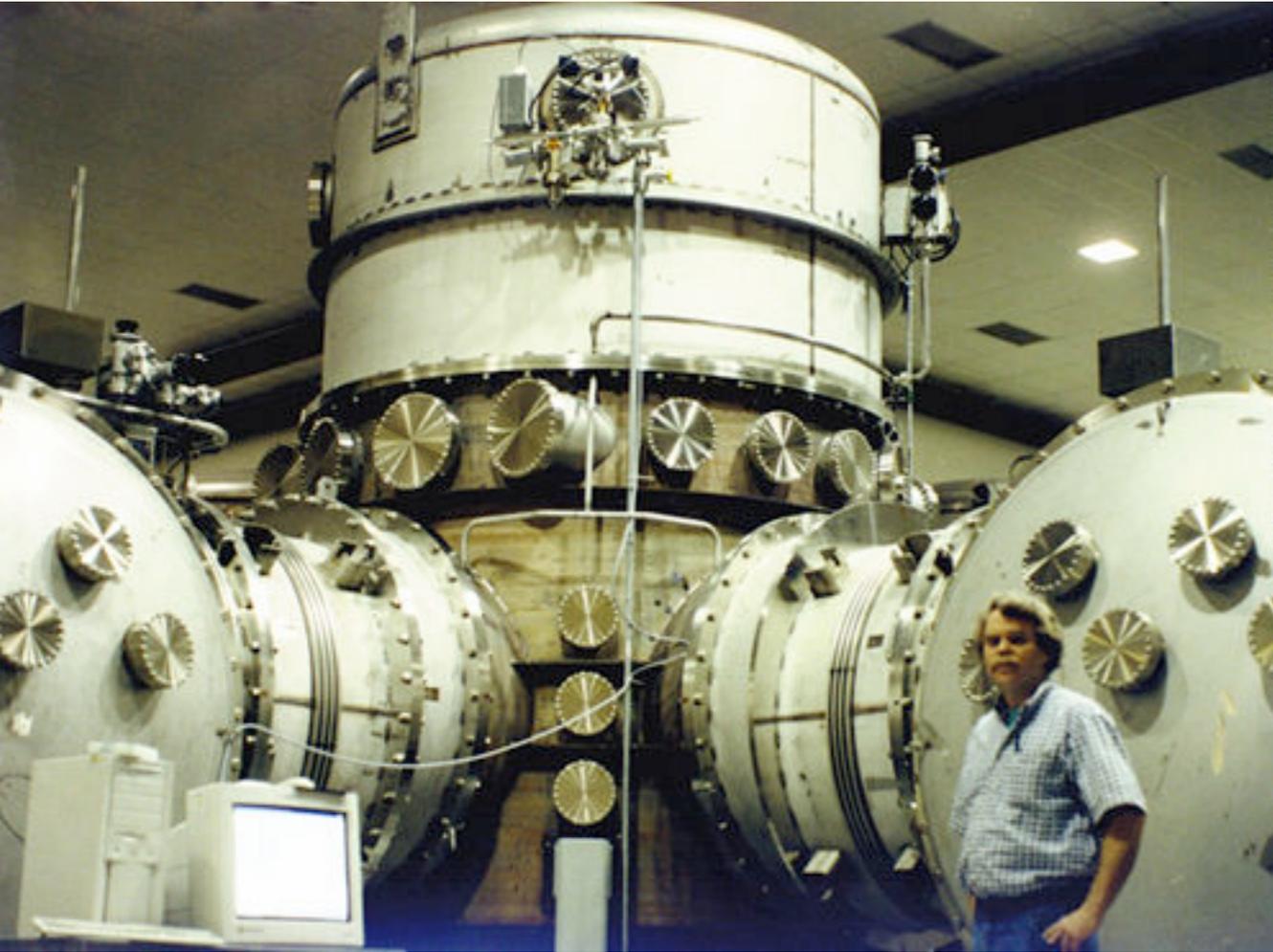


Livingston, LA (near Baton Rouge, LA)

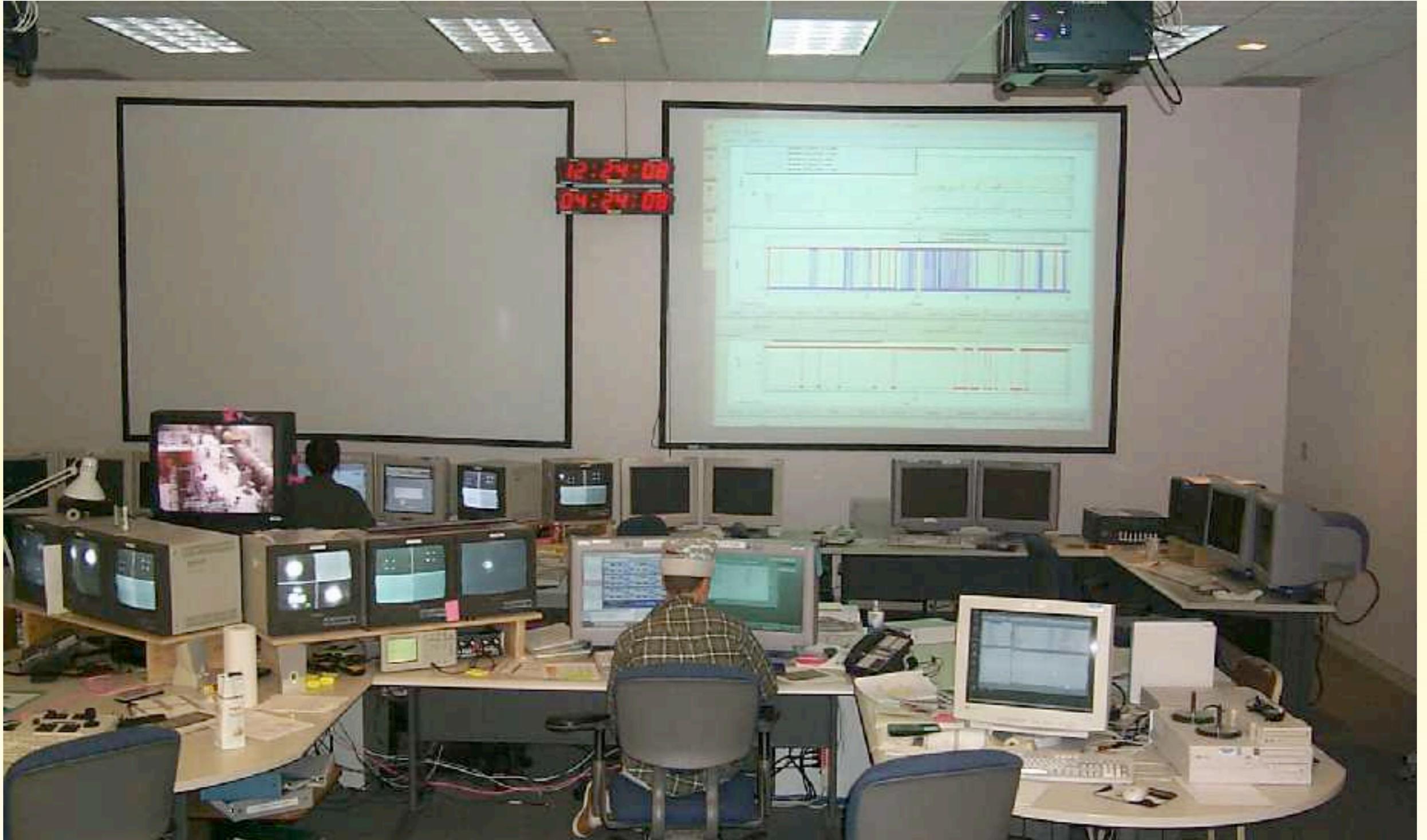
The Beam Tubes



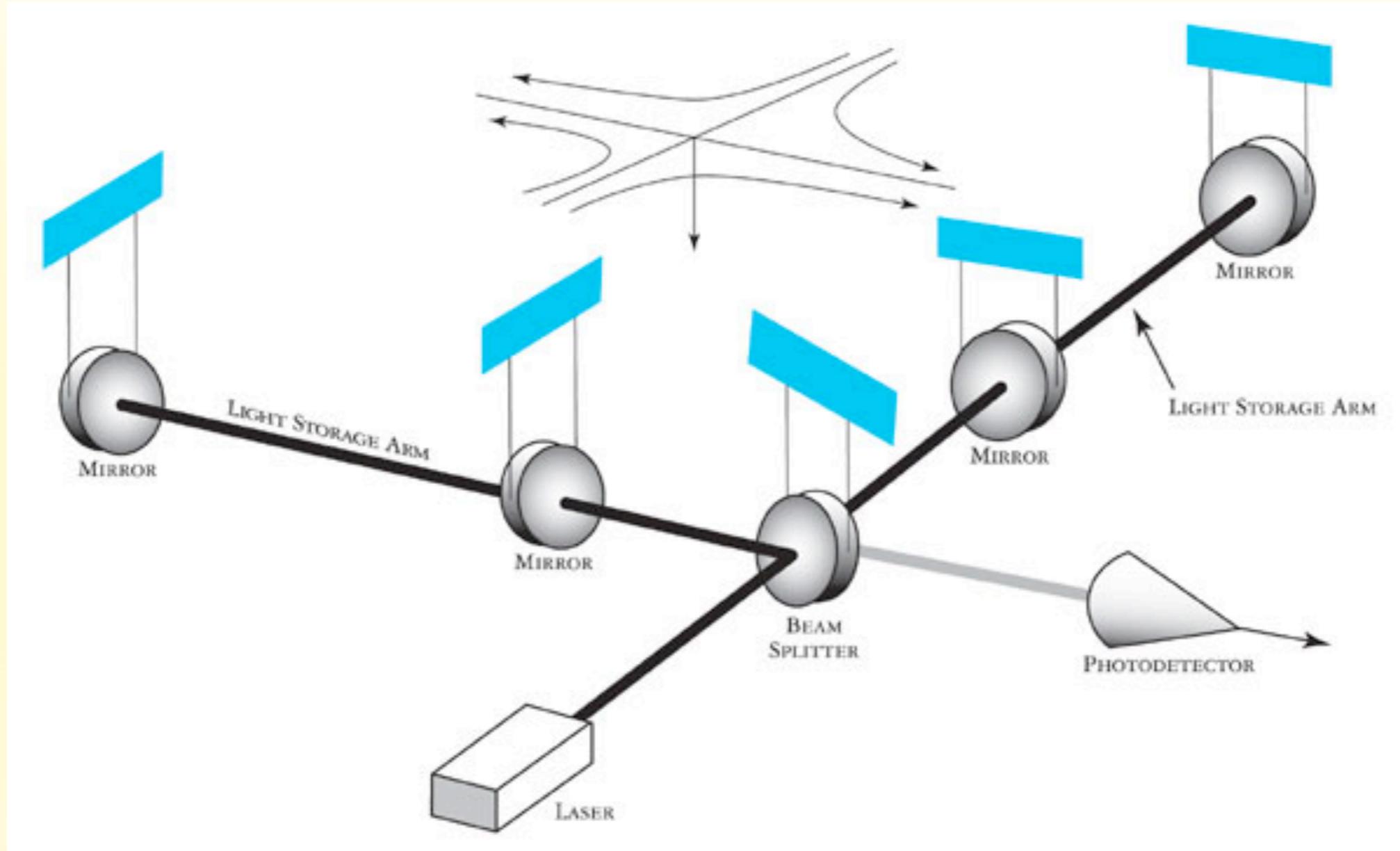
Vacuum Chambers



Control Room

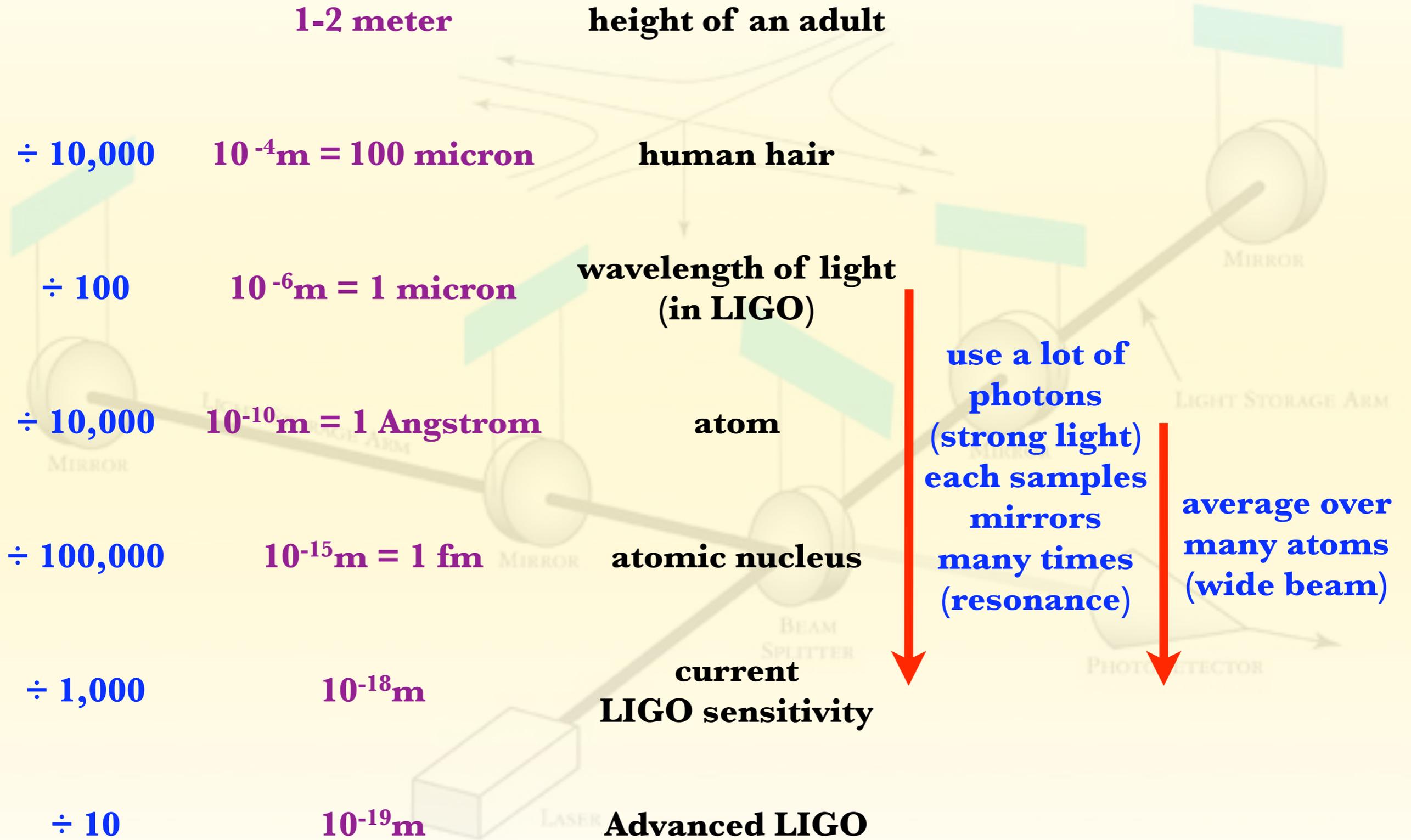


LIGO sensitivity



$$\Delta L = L h = 4000 \text{ m} \times 10^{-21} = 4 \times 10^{-18} \text{ m}$$

How small is 10^{-18} m? How is this possible?

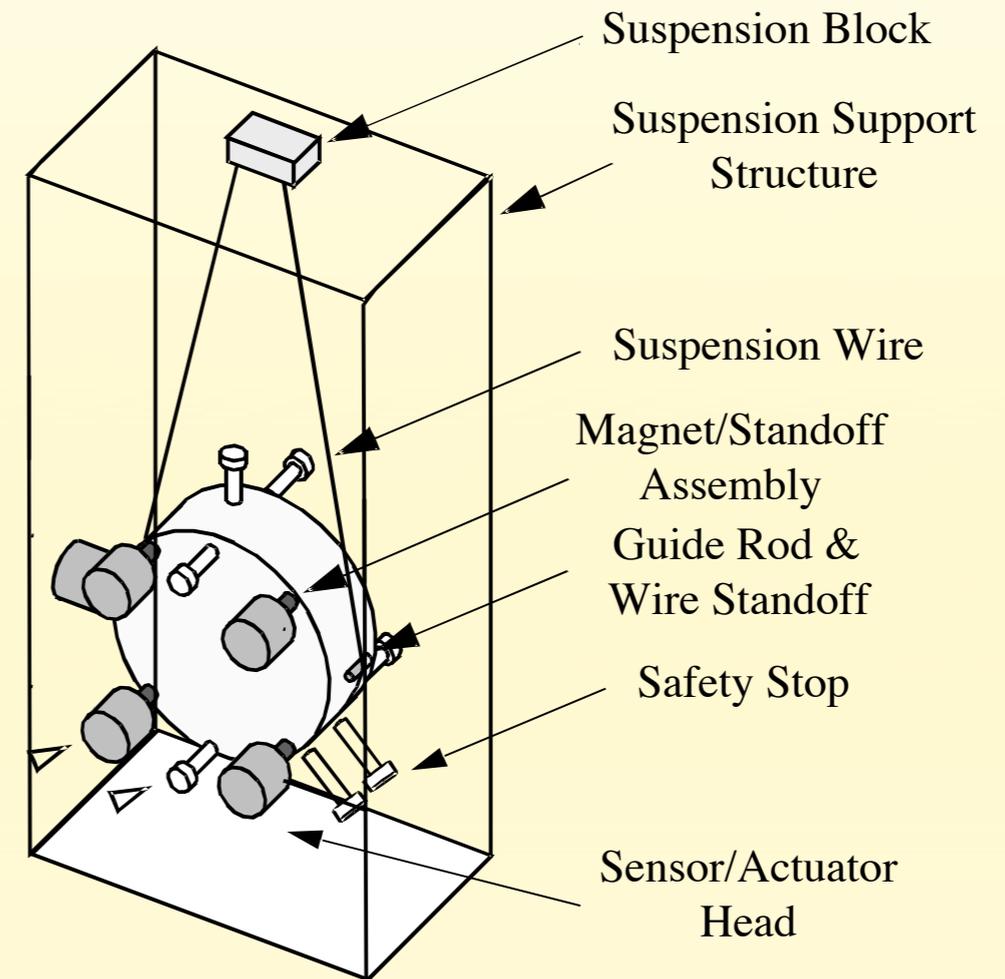


LIGO Mirrors



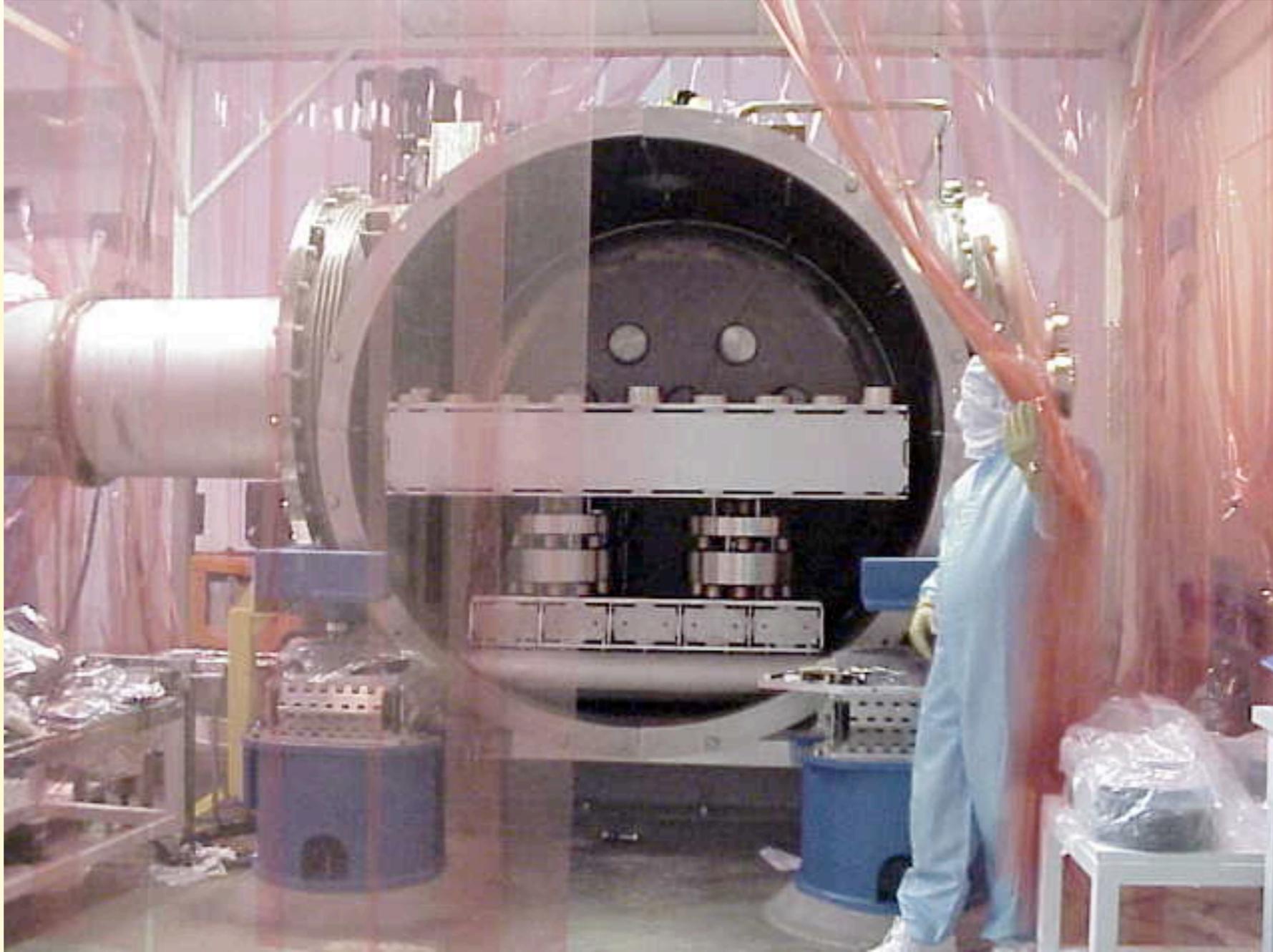
- Made from fused silica. Minimum size determined by diffraction.
- Weighs ~ 10 kg
- Light beam (~ 10 cm in diameter) averages over 10^{18} atoms
- Highly polished surface (with roughness ~ 10 nm, or ~ 100 atom layers)
- Low scattering and low optical loss (~ 100 ppm per bounce)

Mirror Suspension



- Suspended by steel wires
- Controlled by magnets clued on the back of mirrors
- High Q factor (relaxation time \sim few years)

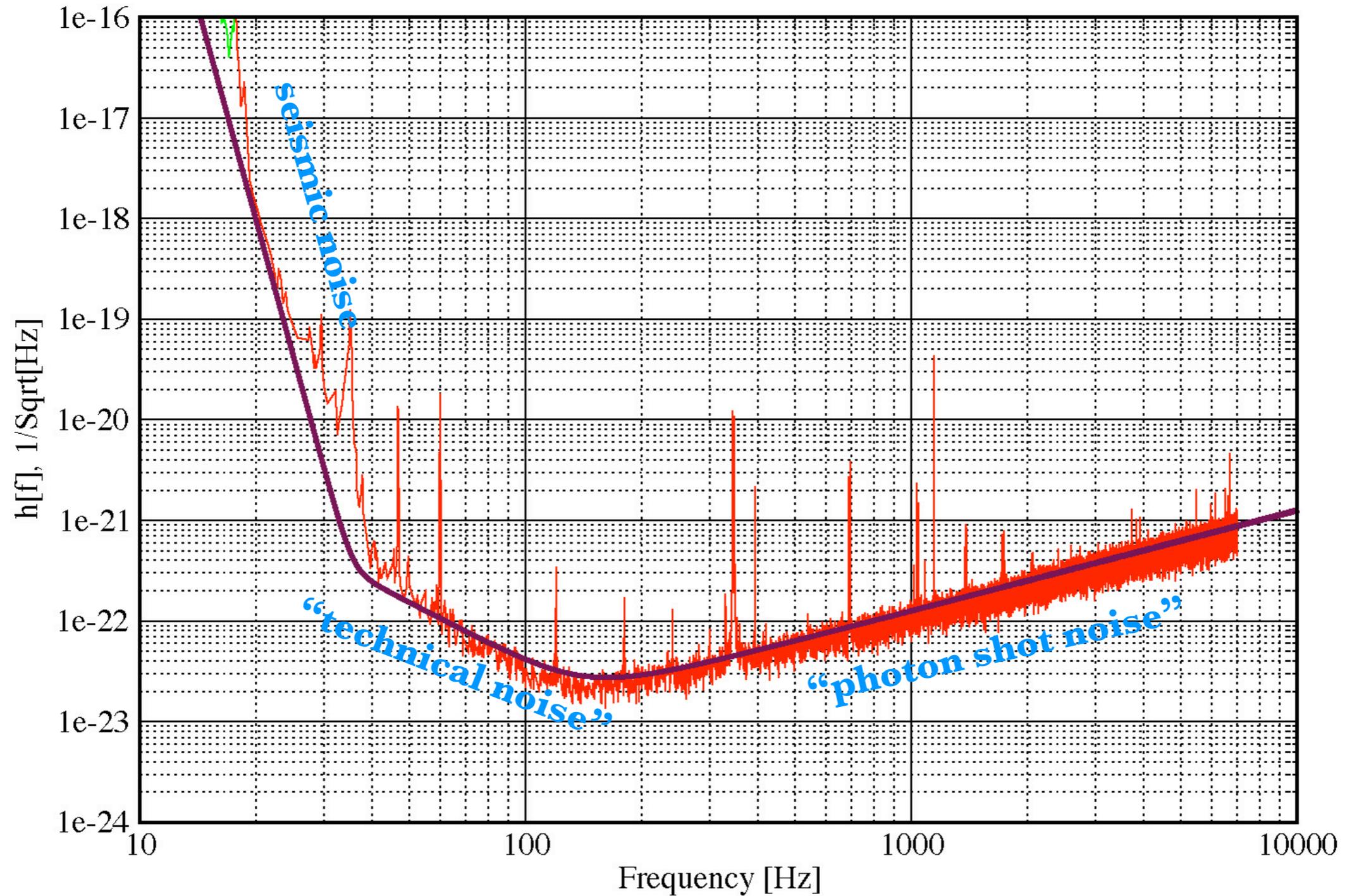
Seismic Isolation



- Multiple stages of isolation

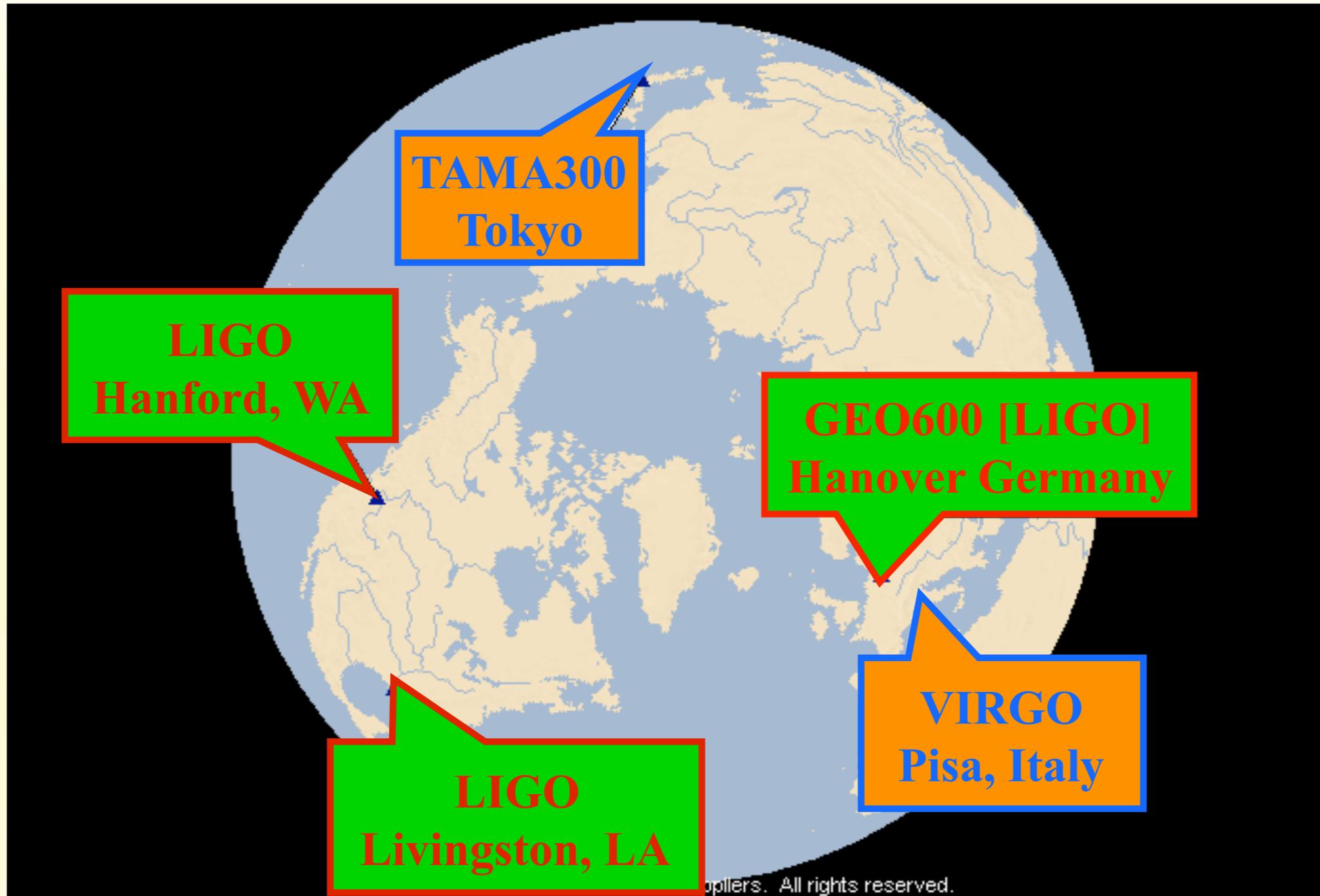


LIGO noise curve



Detection Band from 10Hz to 10000Hz

A Global Network



- Allows “angular localization” down to ~ 1 degree

A Global Network



VIRGO, Pisa, Italy, 3km
French-Italian Collaboration



GEO 600, Hannover, Germany, 600m
British-German Collaboration

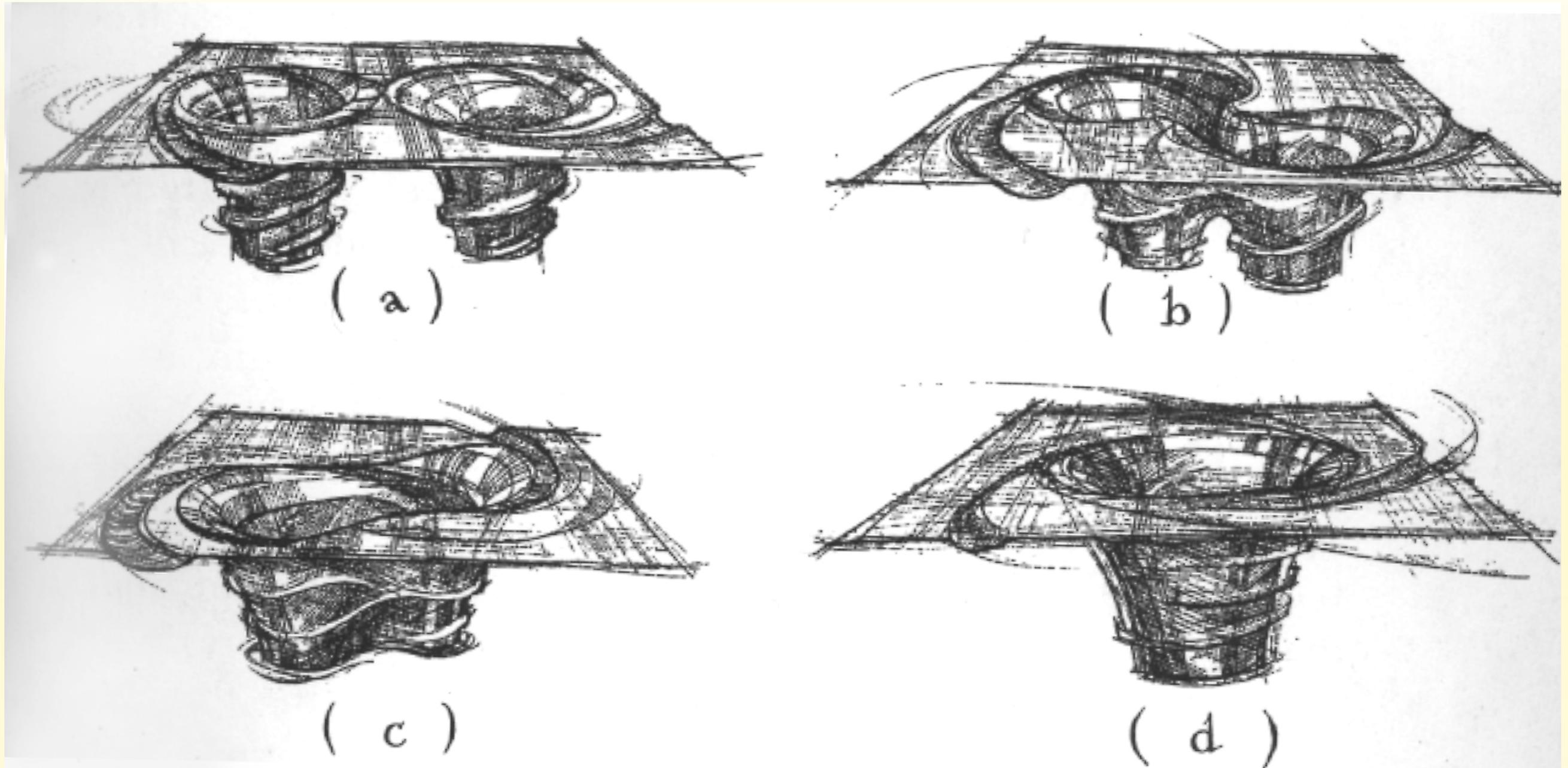


TAMA, Tokyo, Japan, 300m

Primary sources of LIGO

- **Collision of Black Holes/Neutron Stars**
- **Pulsars with asymmetry**
- **Explosions**
- **Stochastic Gravitational-Wave Background**

Black Hole Collisions



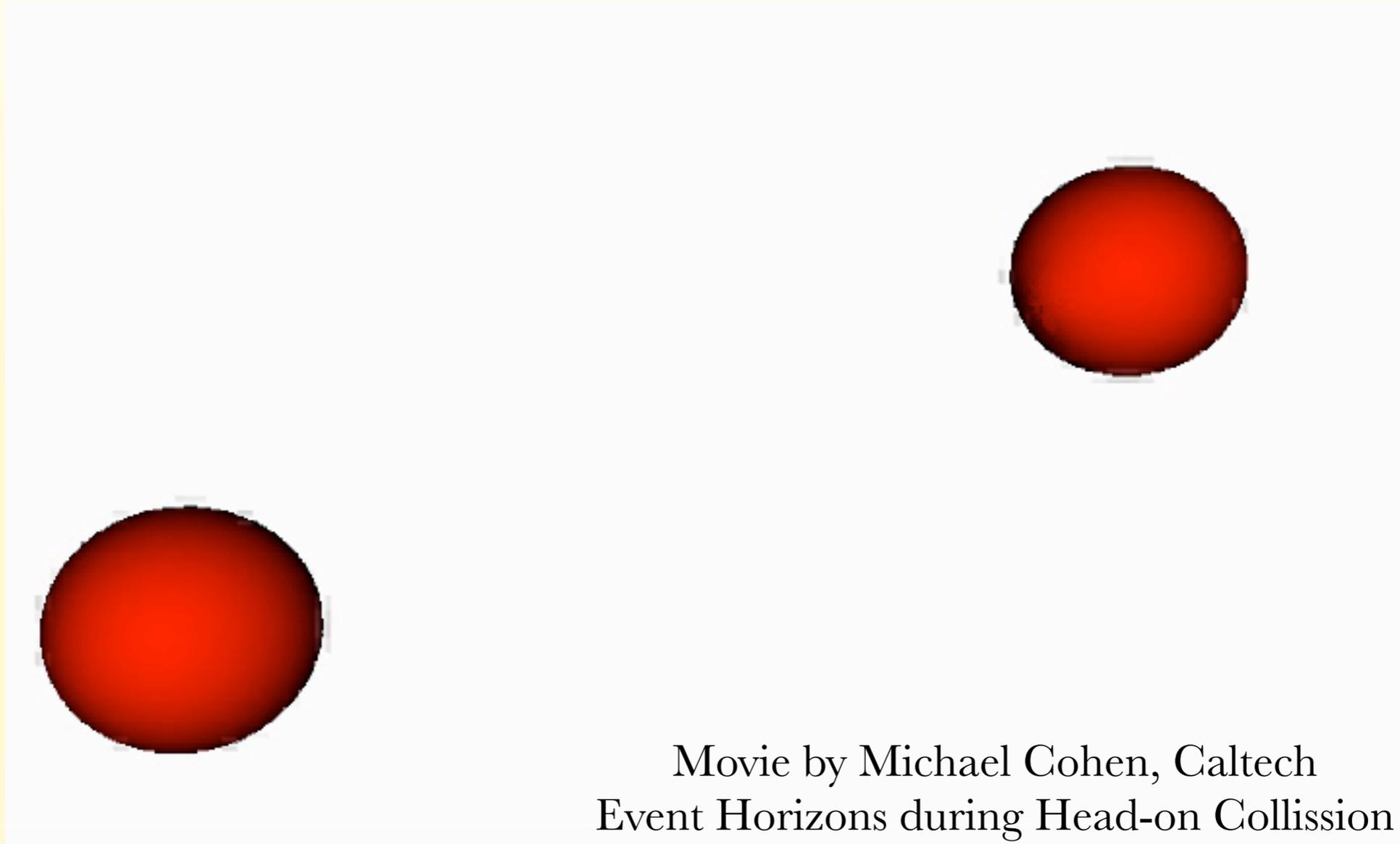
- Initial stage (“**inspiral**”): approximately a two-body motion
- Final stage (“**ringdown**”): perturbations to a single black hole
- Intermediate stage (“**merger**”): highly dynamical and nonlinear, can only be simulated numerically

Black Hole Collisions

Movie by Michael Cohen, Caltech
Event Horizons during Head-on Collision

- Started in the 1960s, difficult due to nonlinear nature of Einstein Equations, and freedom in the choice of frames.
- Waveforms very important for LIGO, because we need to “match” data with “templates”. Crucial in verifying that they are indeed black holes.
- Head-on collision: 1990s
- Merger in circular orbits (astrophysically interesting): only since 2005, active field

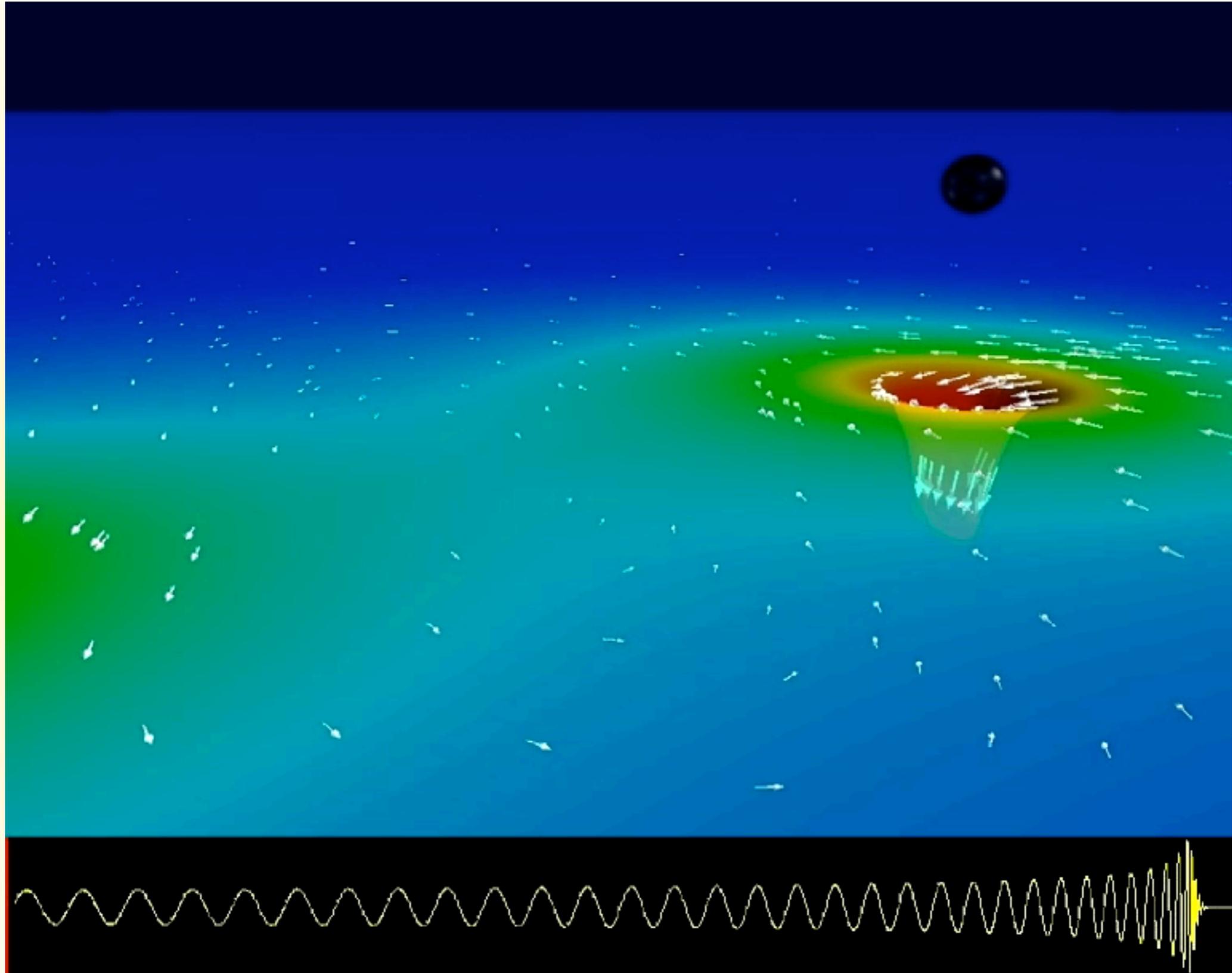
Black Hole Collisions



Movie by Michael Cohen, Caltech
Event Horizons during Head-on Collision

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- Head-on collision: 1990s
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Black Hole Collisions



Movie by Caltech-Cornell Numerical Relativity Collaboration
Mark Scheel, Harald Pfeiffer, Lee Lindblom, et al.

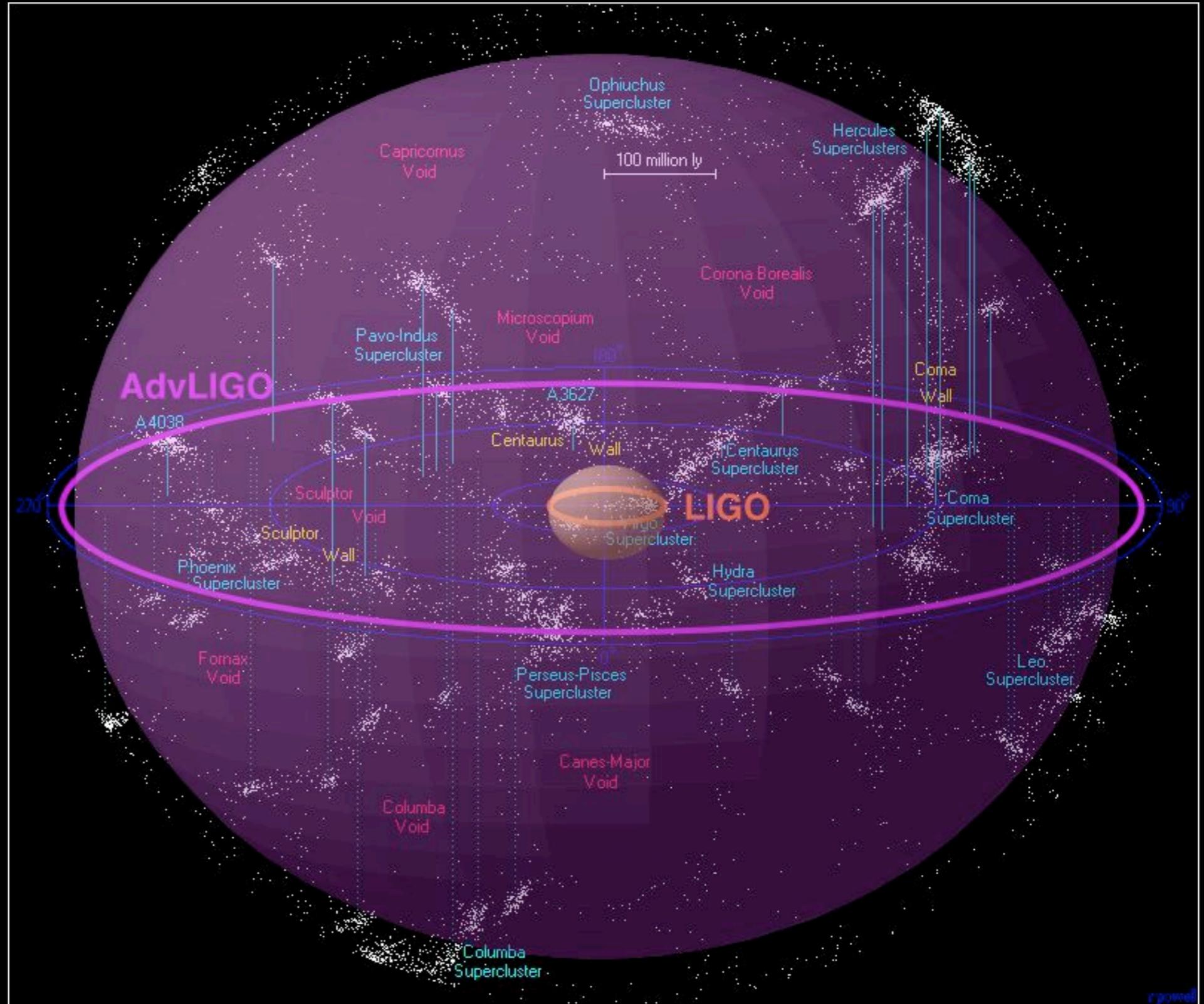
initial LIGO (2005-07)
300 million light years
~1 BHBH/10 yr



Enhanced LIGO (2009-10)
600 million light years
~1 BHBH/yr



Advanced LIGO (2014-)
5 billion light years
~1 BHBH/day or week



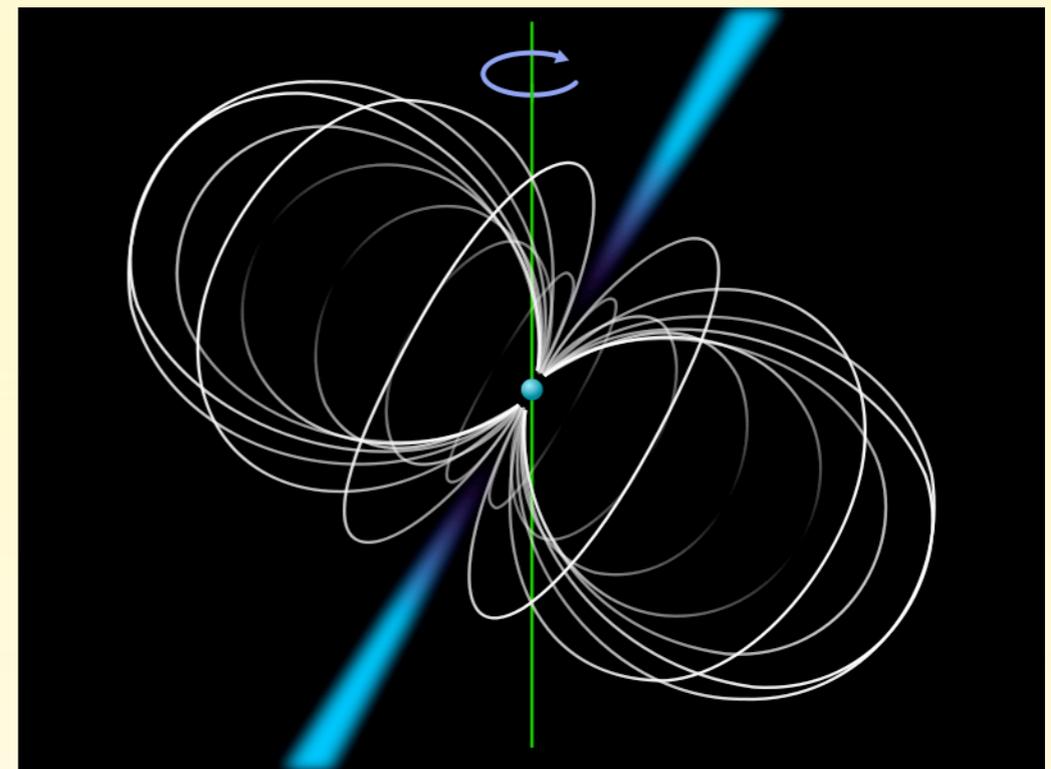
Pulsars (2005-07)

Asymmetric pulsars will emit gravitational waves



The [Crab Pulsar](#) (combined data from Hubble telescope and Chandra X-ray Telescope)

Result of a supernova in 1054



LIGO: less than 4% loss in rotation energy is released in gravitational waves
(rest of it released in driving charged particles)

EINSTEIN@HOME

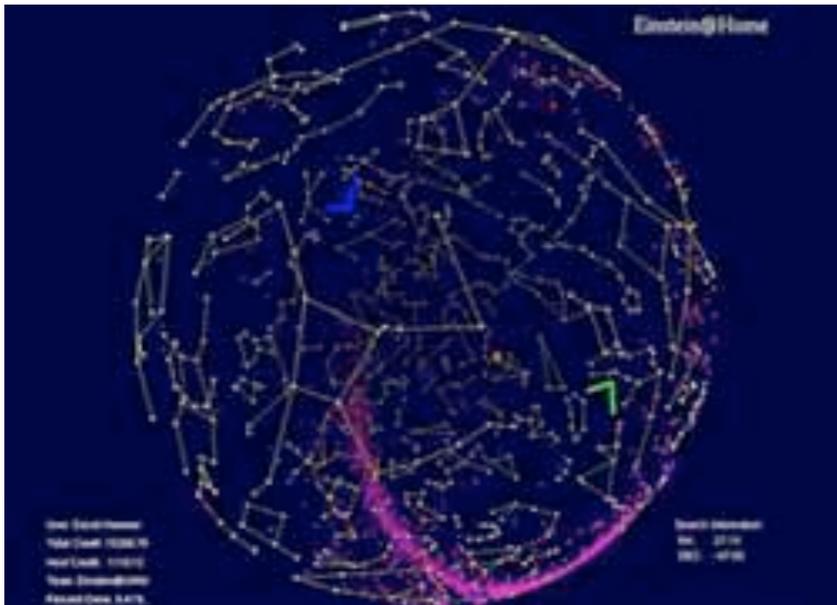
E I N S T E I N @ H O M E

Catch a Wave From Space

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[Join Einstein@Home](#)



Einstein@Home screensaver

According to Albert Einstein, we live in a universe full of gravitational waves. He suggested that the movements of heavy objects, such as black holes and dense stars, create waves that change space and time. We have a chance to detect these waves, but we need your help to do it!

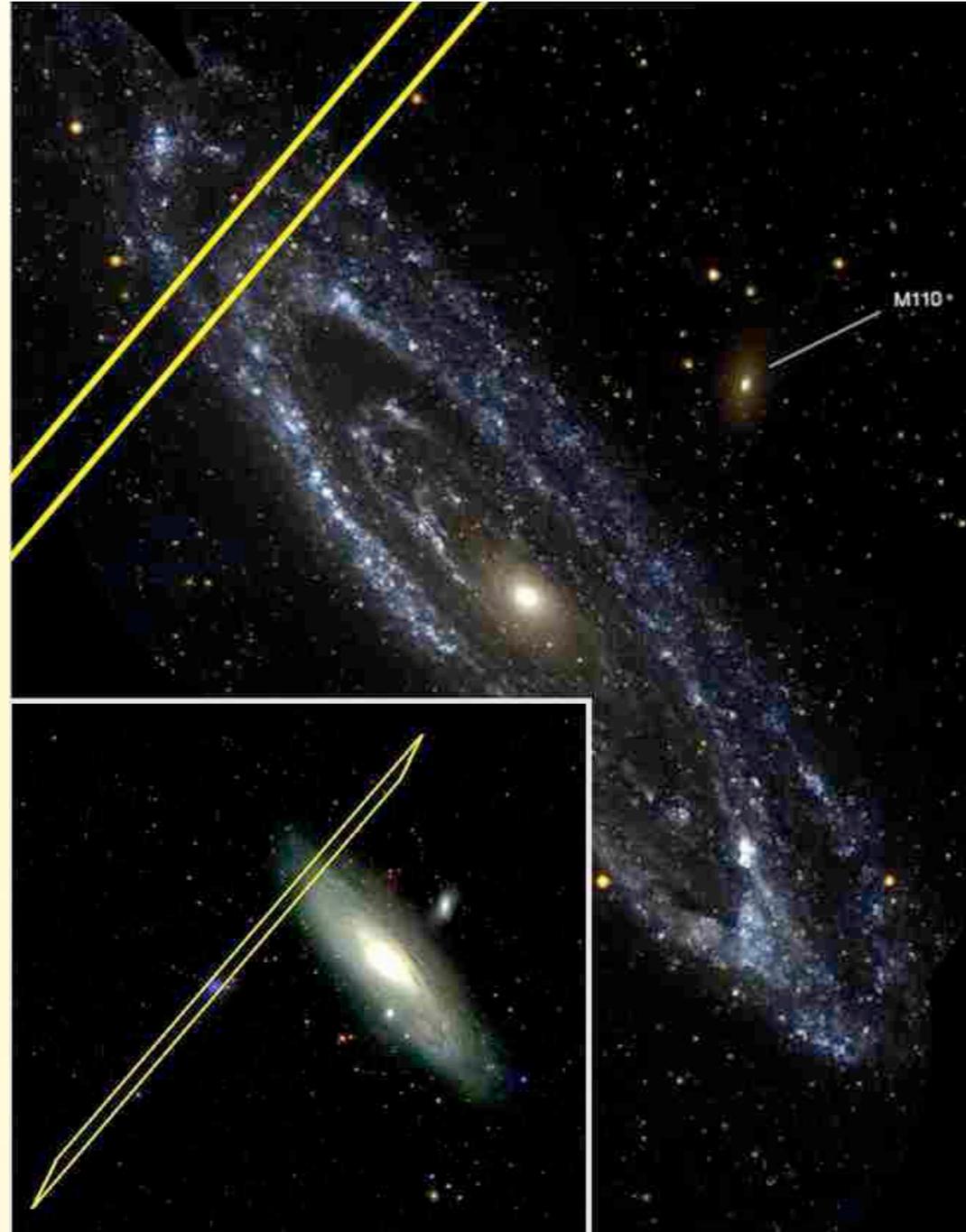
Einstein@Home uses computer time donated by computer owners all over the world to process data from gravitational wave detectors. Participants in Einstein@Home download software to their computers, which process gravitational wave data when not being used for other computer applications, like word processors or games. Einstein@Home doesn't affect the performance of computers and greatly speeds up this exciting research.

[Learn more about the project.](#)



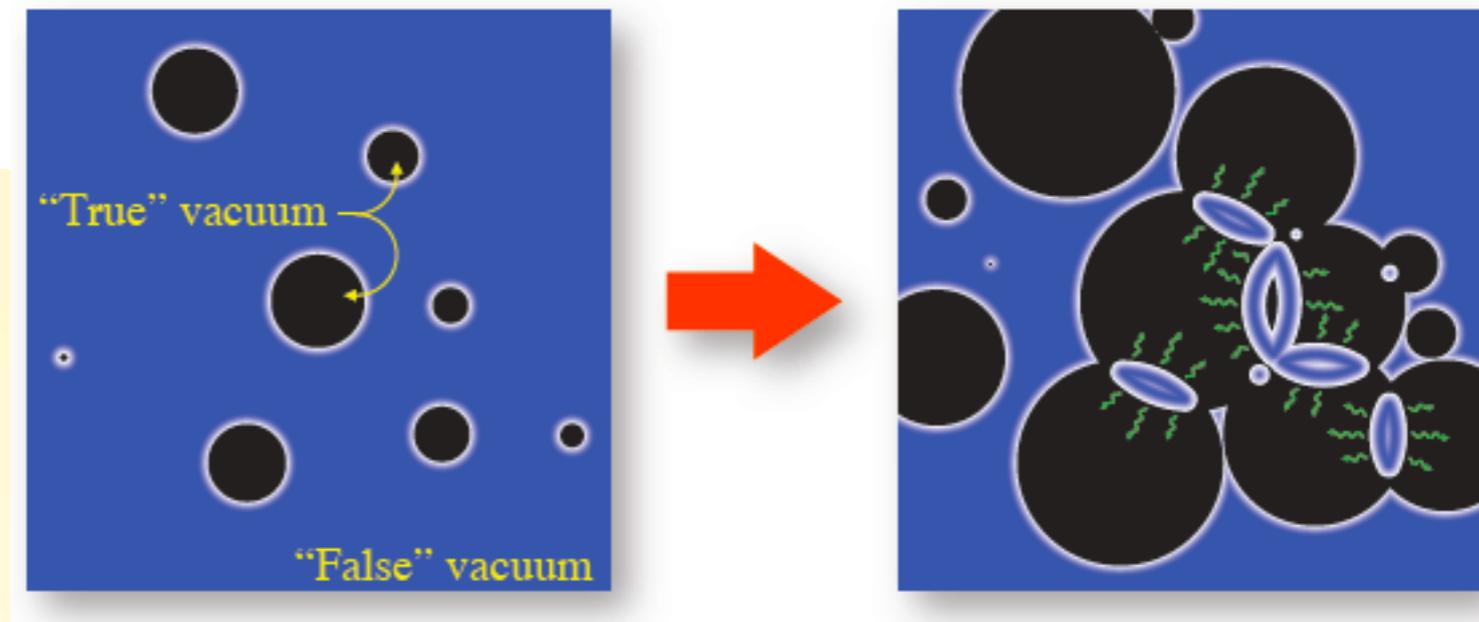
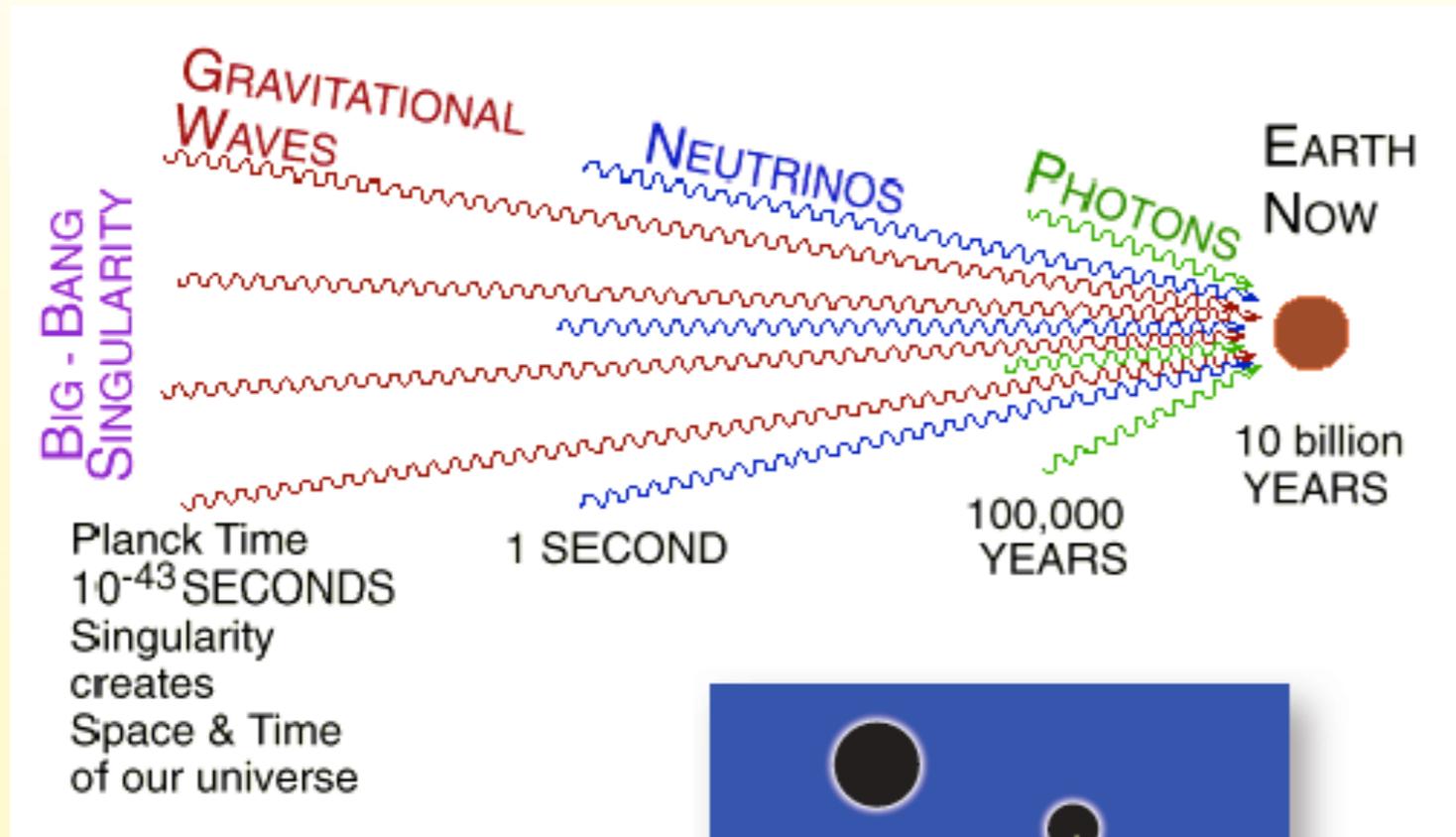
<http://www.einsteinathome.org/index.html>

Gamma-Ray Bursts (2007)



- Gamma-Ray Burst 070201, **if in Andromeda Galaxy** (2.5Mly or 0.8 Mpc), **then not a binary neutron-star merger.**

Stochastic Gravitational-Wave Background



- Quantum fluctuations of spacetime at the "birth" of the universe
- Stochastic waves generated by "phase transitions"

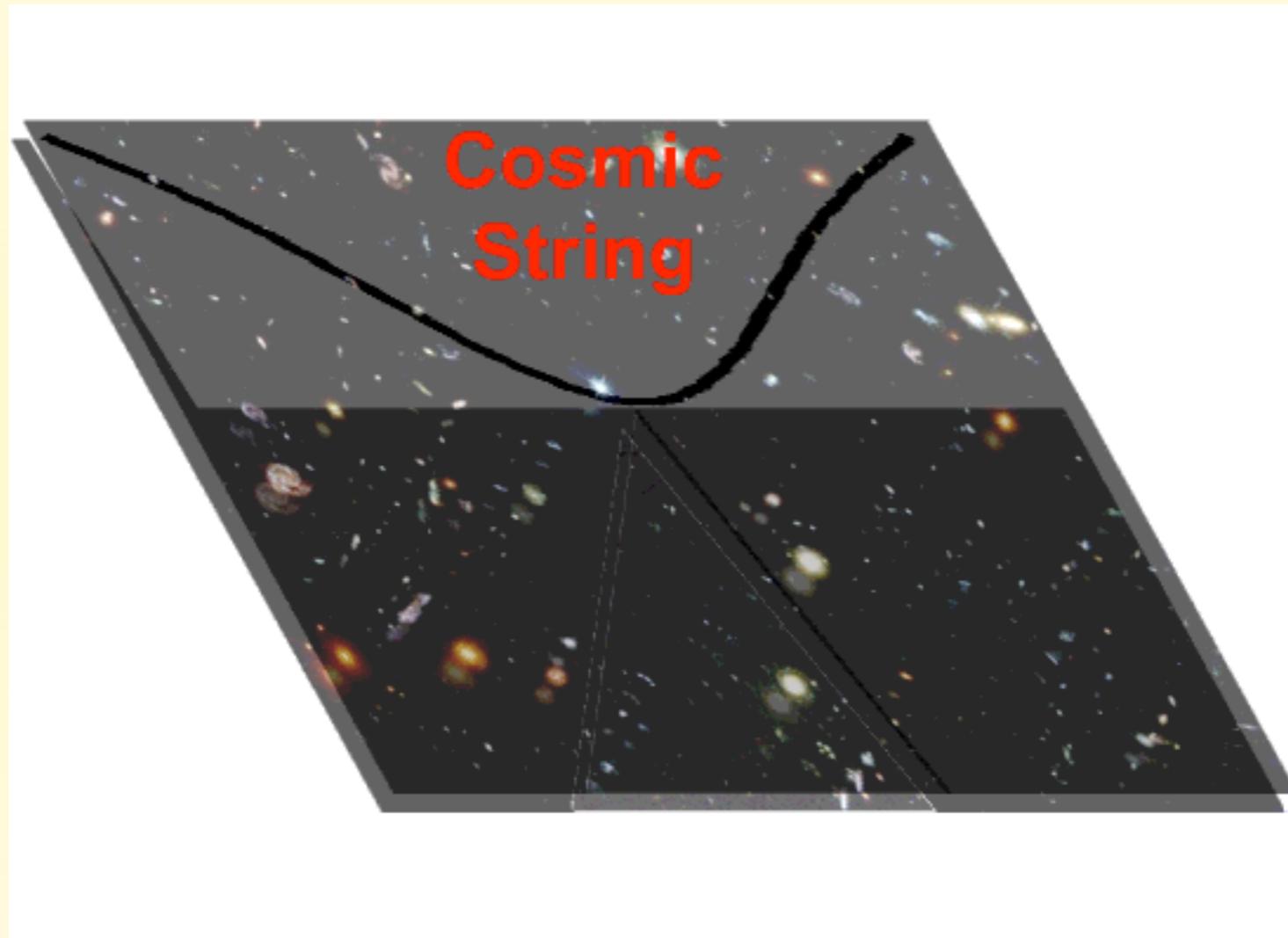
A test for string theory??

- Bursts from cosmic strings and/or cosmic superstrings??
- Highly speculative, but might provide evidence for string theory ...

Animation by Bret Underwood, University of Wisconsin

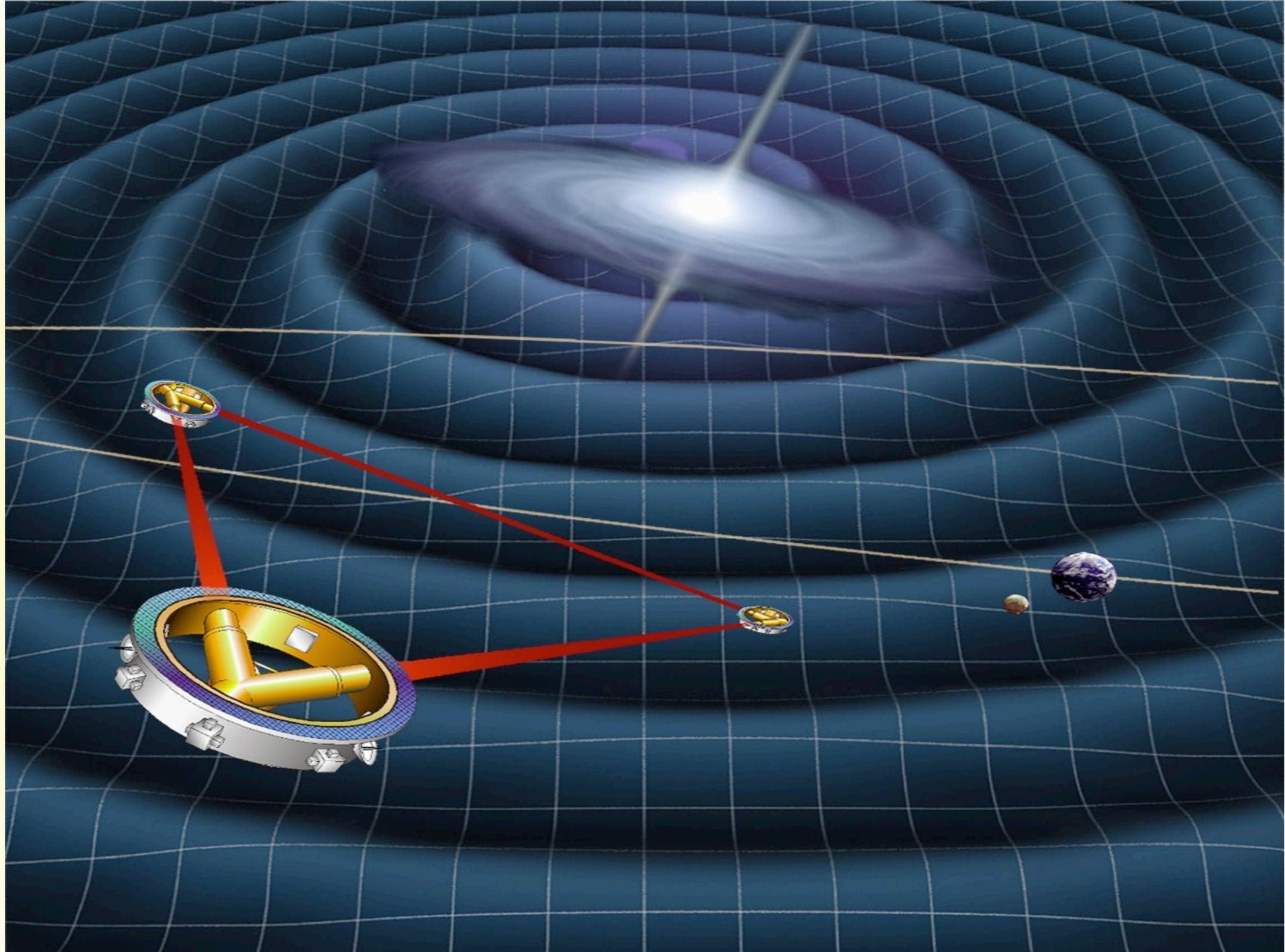
A test for string theory??

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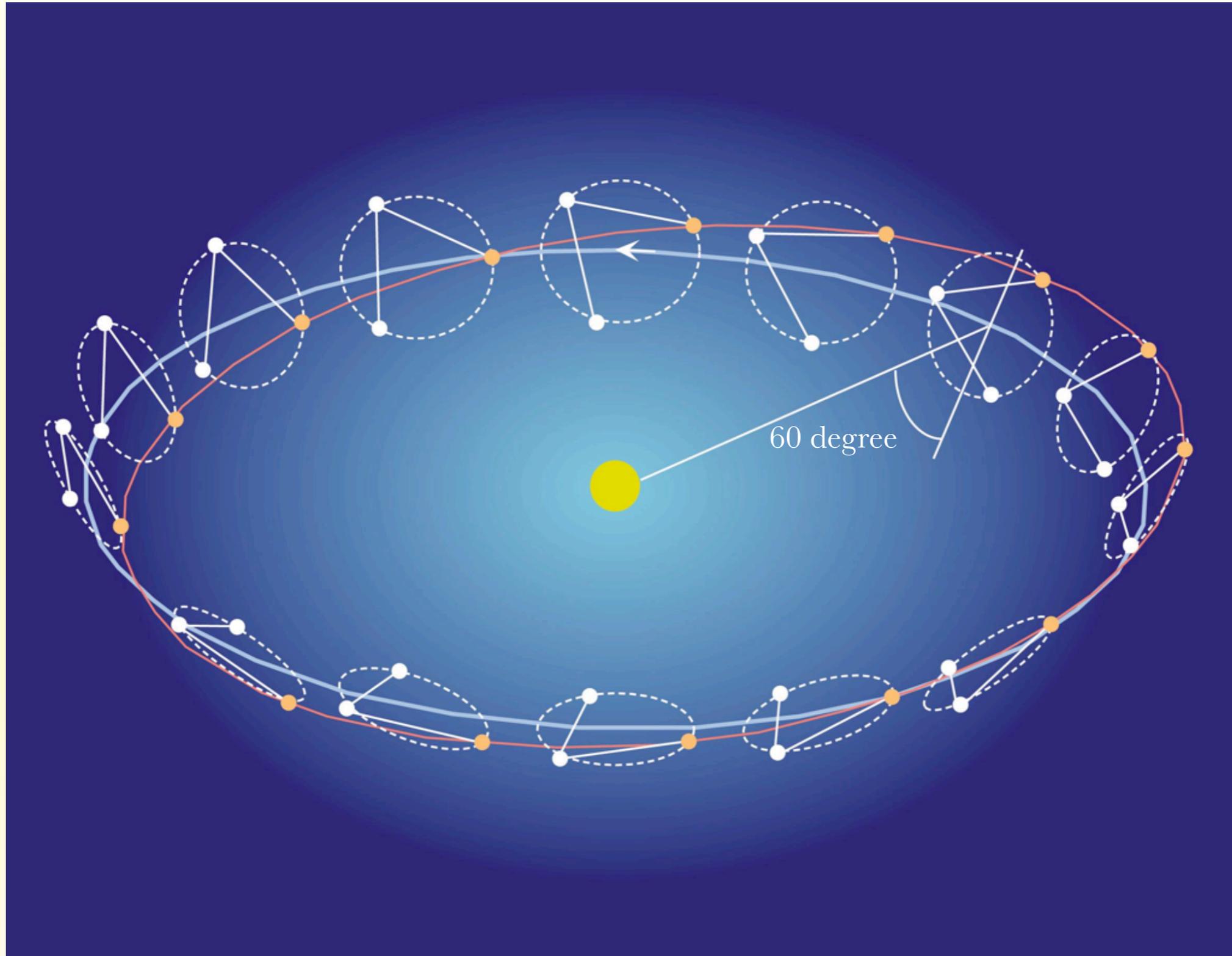
Animation by Bret Underwood, University of Wisconsin

Laser Interferometer Space Antenna



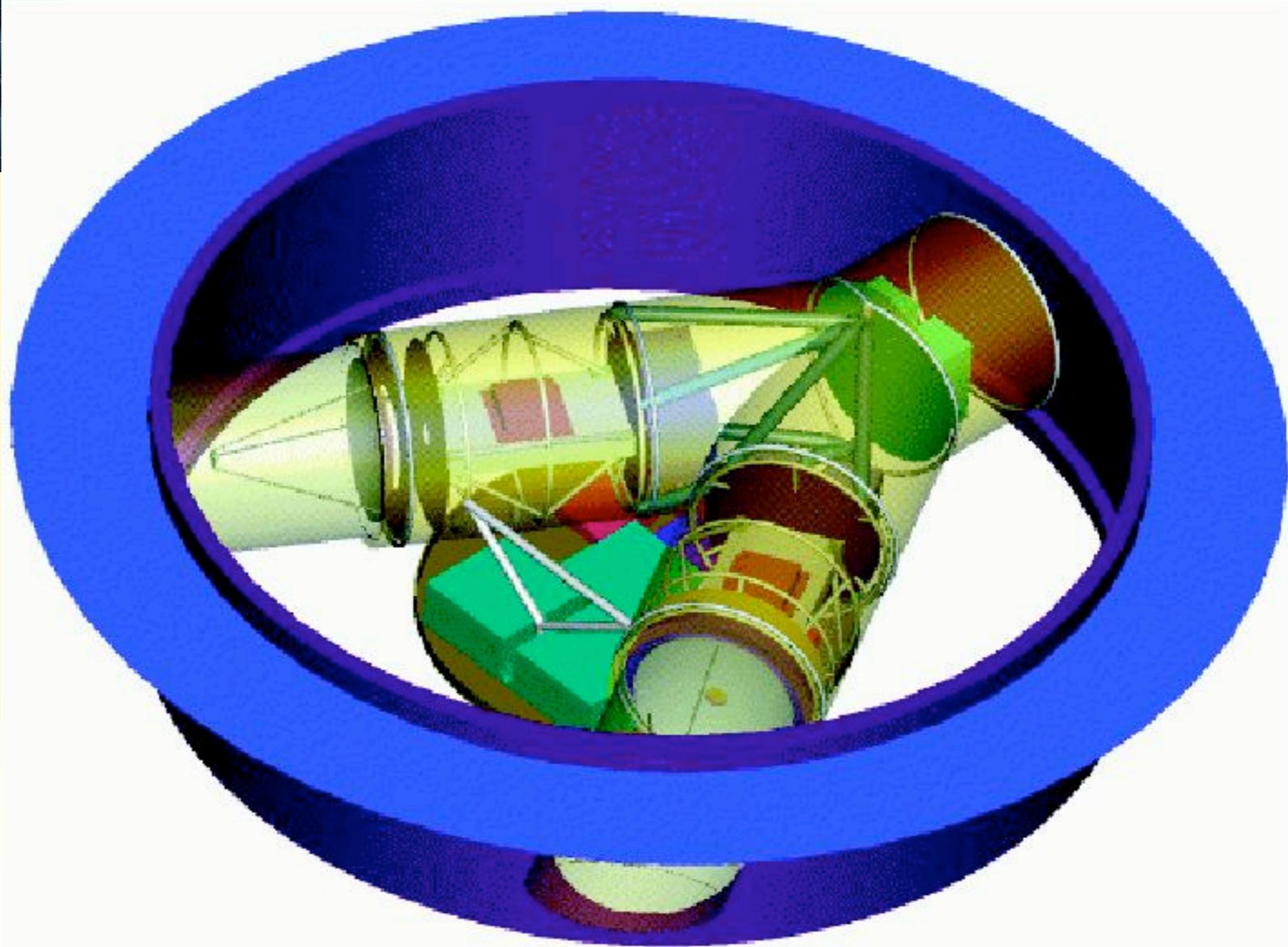
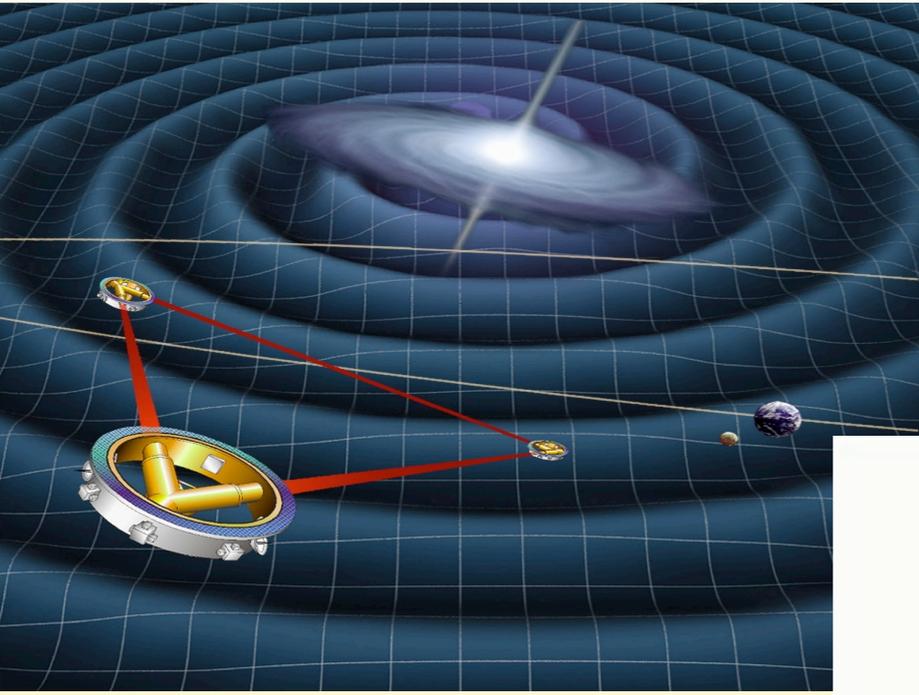
Joint NASA-ESA Project

Laser Interferometer Space Antenna

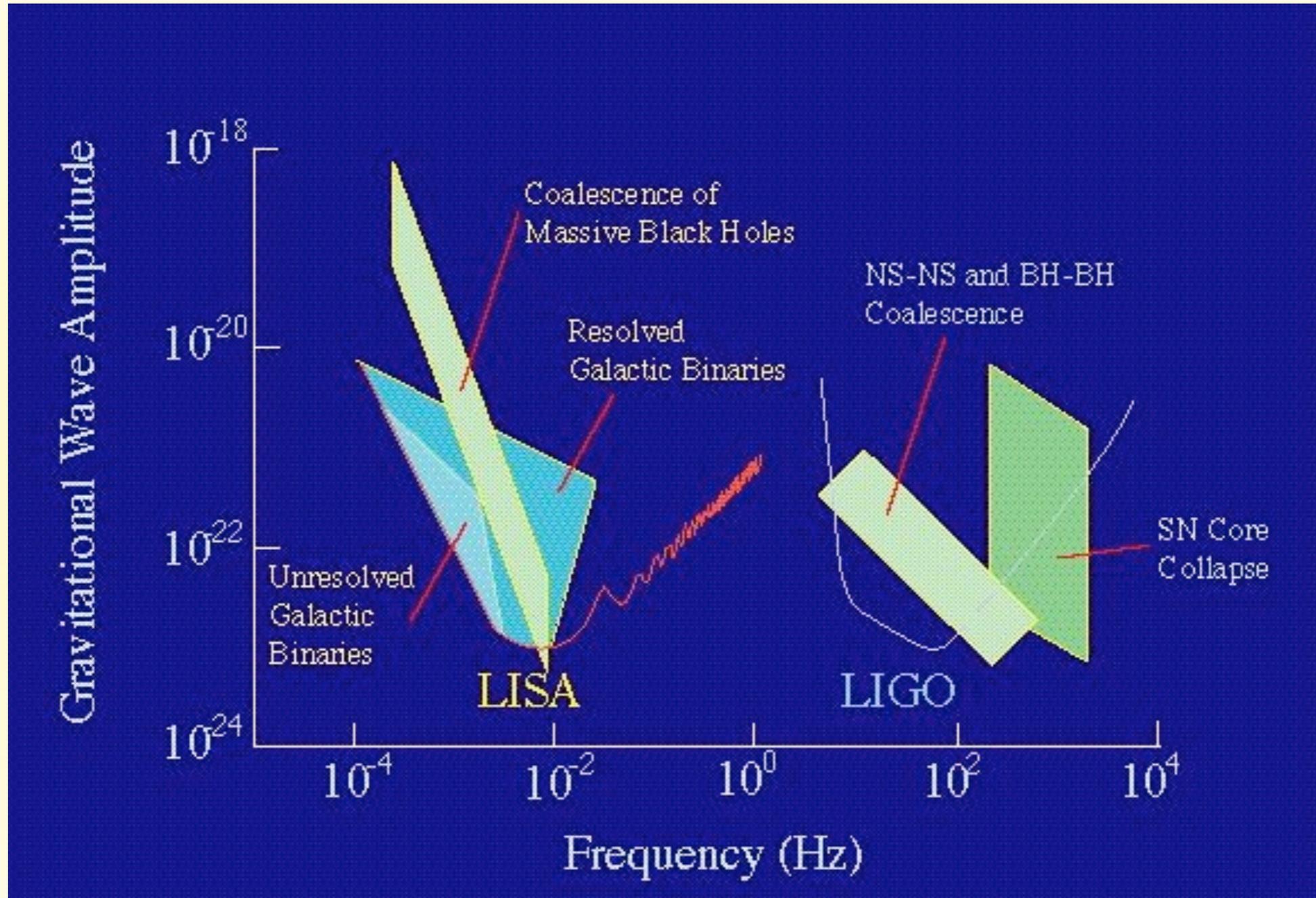


$L = 5$ million km
period = 1 year
operation time = 3 years (nominal)

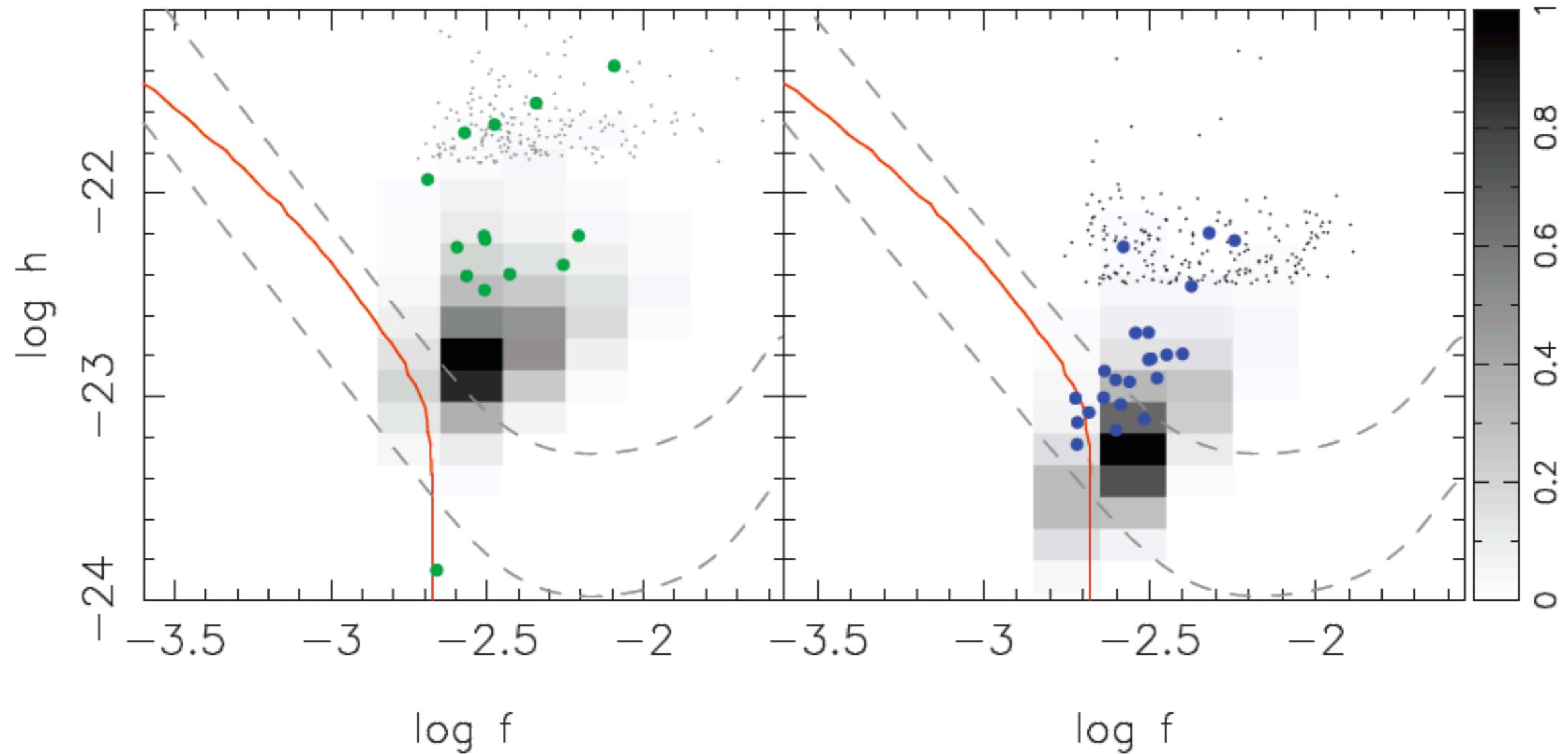
LISA Spacecraft



LISA Sensitivity



Binaries in the Milky Way Galaxy



- More than 10^4 **White-Dwarf Binaries**
- More than 10 known **Neutron-Star Binaries**
- Un-resolvable **White Dwarf Binary** signals increase noise level

Mergers of Galaxies



Image by B. Whitmore (STSci), F. Schweizer (DTM), NASA

- Most galaxies have gone through merger, as a result of structure evolution of the universe
- Supermassive Black Hole Mergers offer clues to *history of galaxy mergers* and *evolution of supermassive black holes*

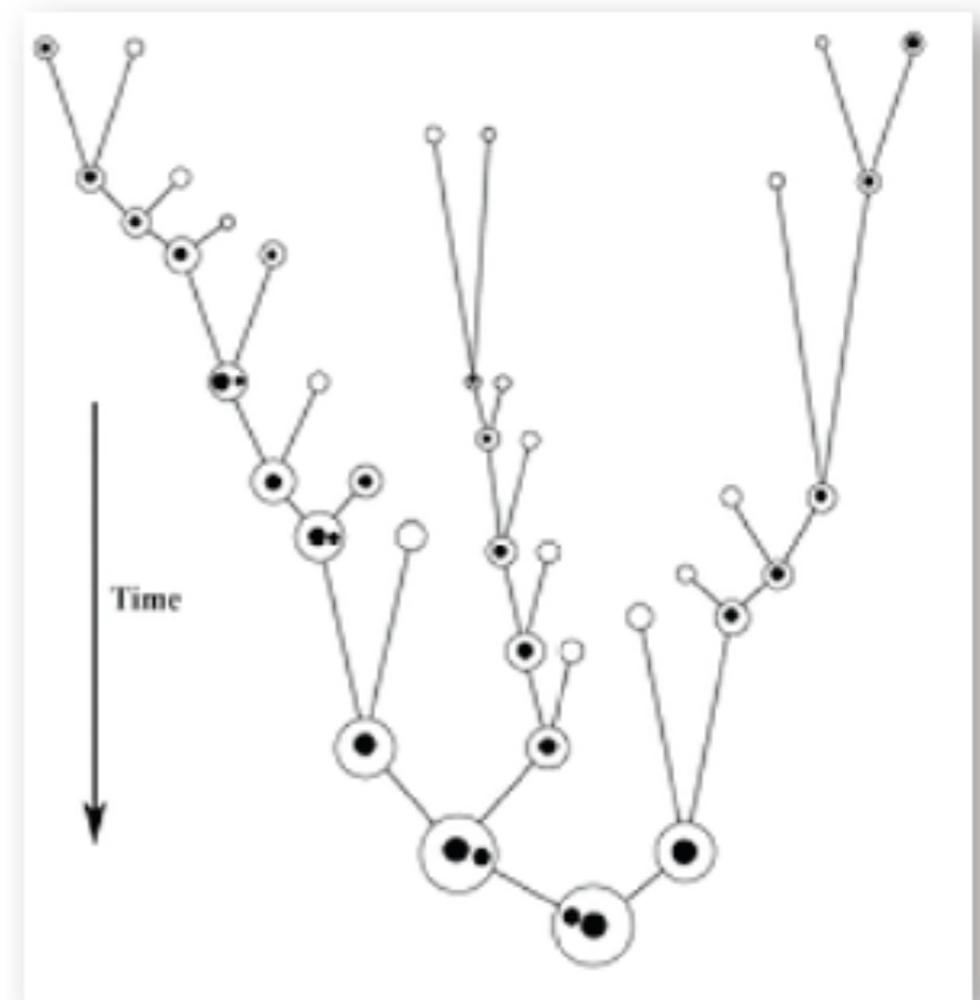
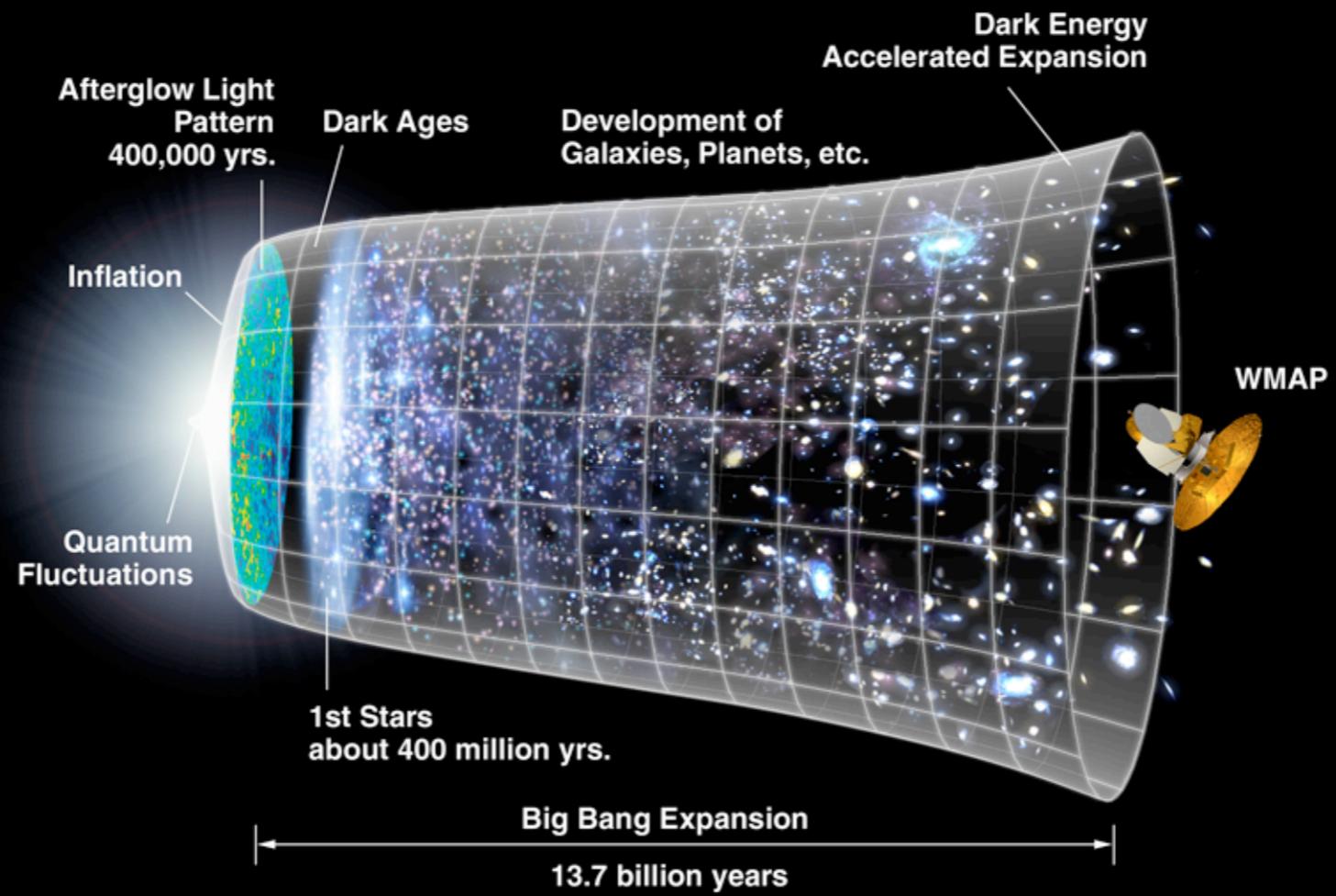
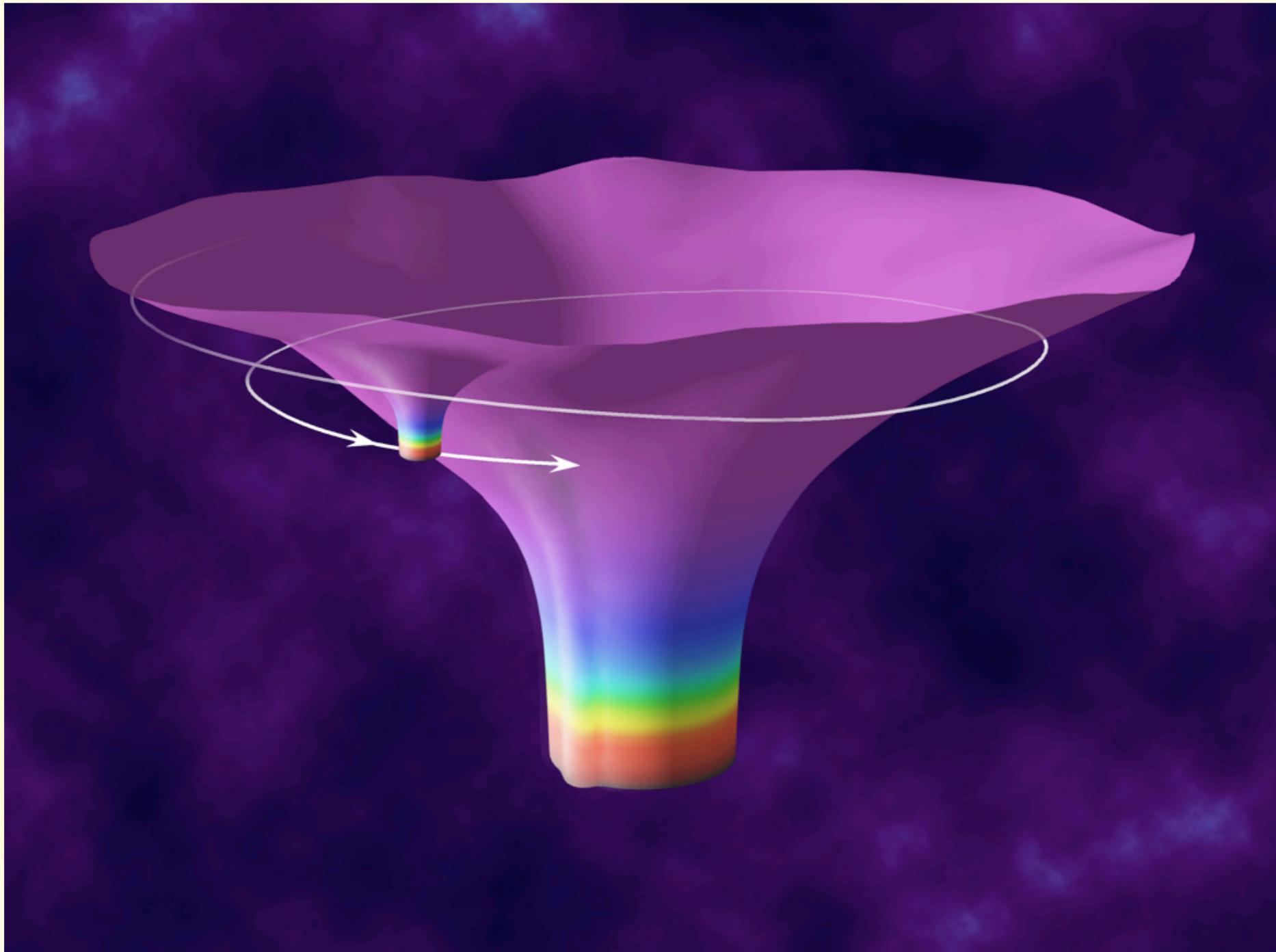


Figure 3-5: A cartoon of the merger-tree history of the assembly of a galaxy and its central black hole in cold-dark matter cosmology. Time increases from top to bottom, and the horizontal axis is a spatial direction. In this case the final galaxy is assembled from the merger of twenty smaller galaxies, containing a total of four seed black holes, and results in four mergers of binary black holes.



Mapping Spacetime Around Black Holes

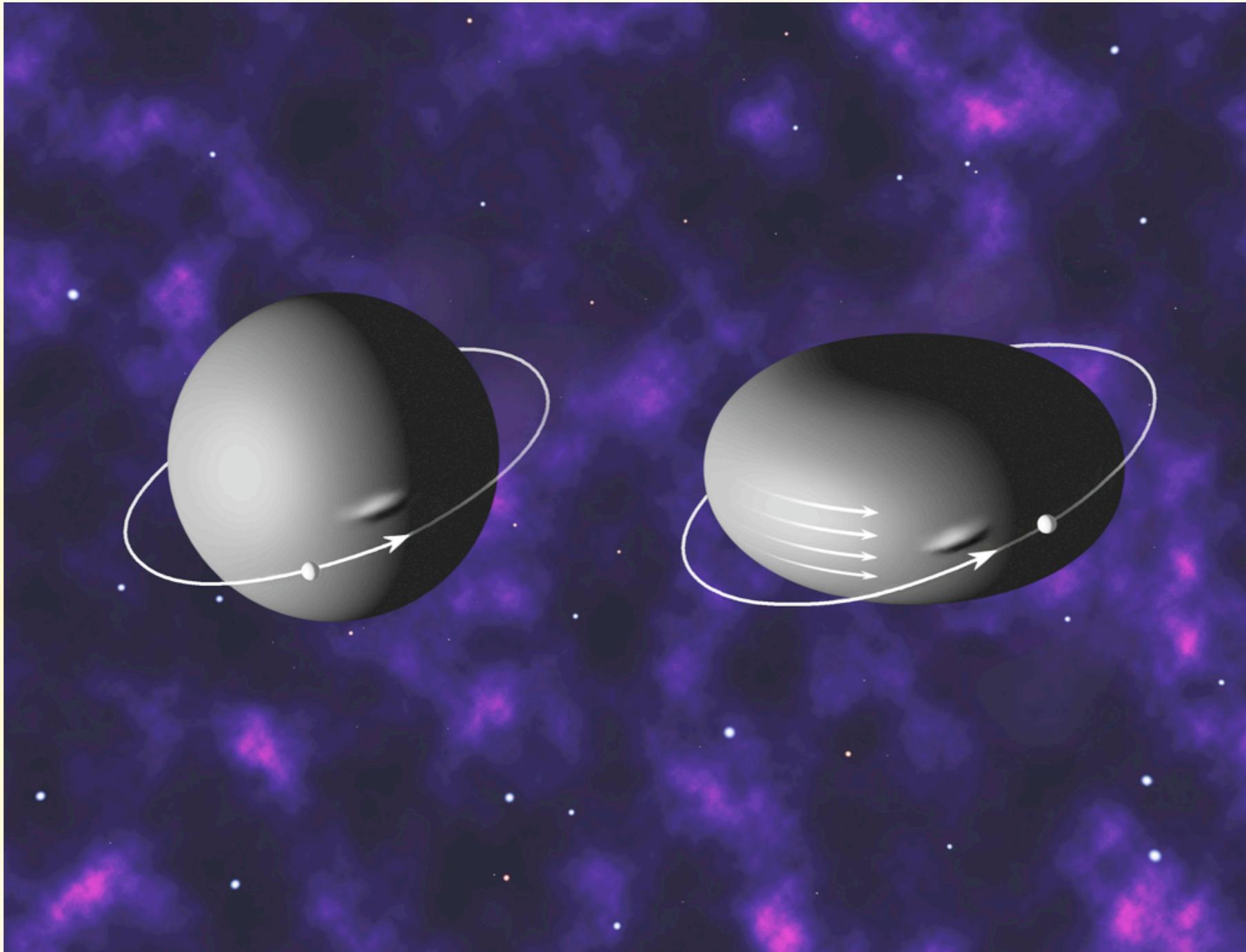
Are they really black holes?



10 solar mass into 10^6 solar mass, more than 10^5 wave cycles
provide fine map of spacetime geometry

Probing the Black Hole Horizon

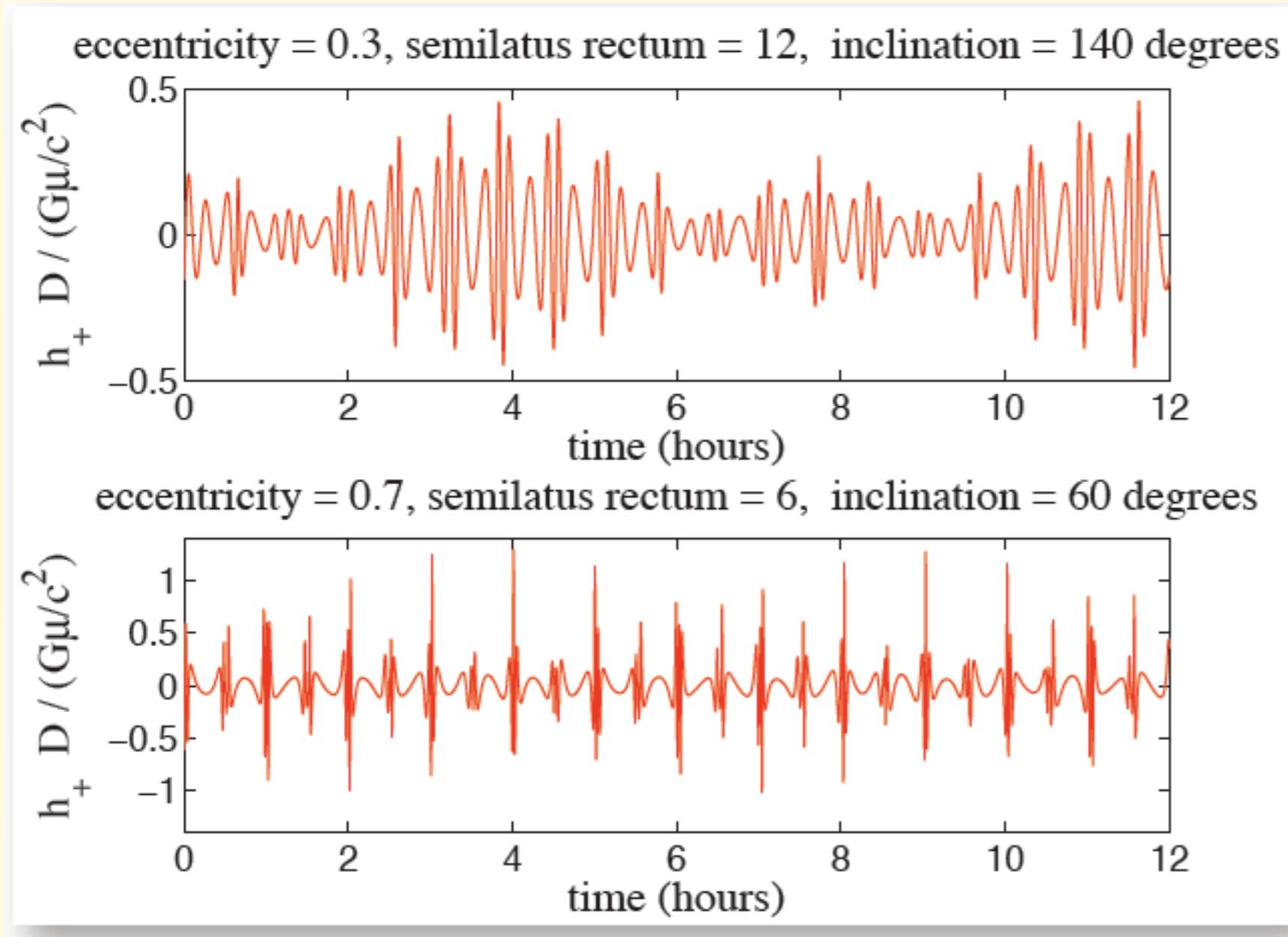
Are they really black holes?



10 solar mass into 10^6 solar mass, more than 10^5 wave cycles
probing response of event horizon via tidal interaction

Mapping and Probing Black Holes

physical information must be decoded from waveforms like this



$$\times (2 \times 365 \times 3)$$

$$\parallel$$

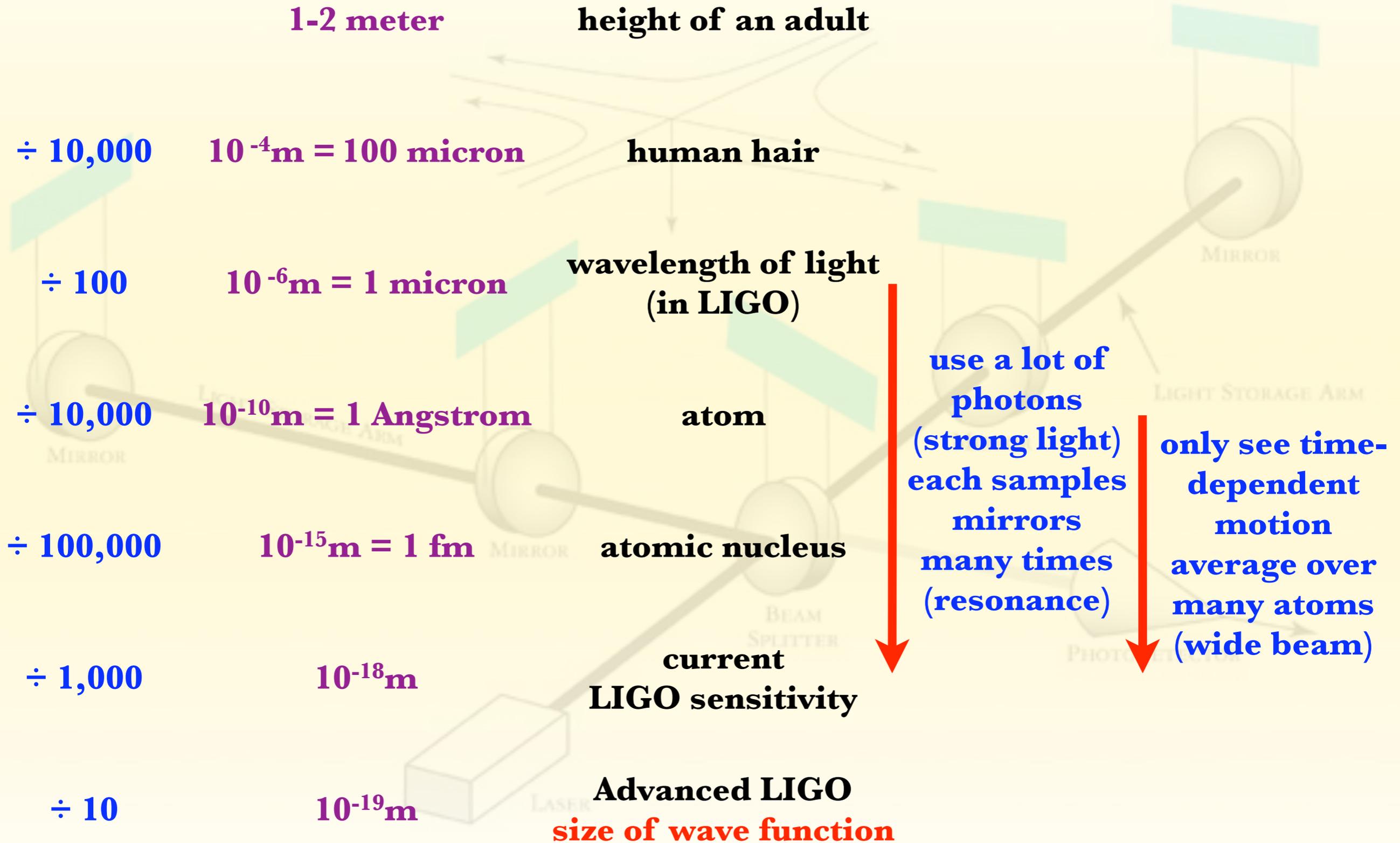
$$2200$$

computationally and theoretically challenging

Summary

- Gravitational-Wave Astronomy has just started
- Eventually, we will be able to, **experimentally**
 - confirm Gravitational Waves by direct measurement ($\ll 10$)
 - detect waves from black hole/neutron star collisions, and study non-linear, highly dynamical spacetime ($\ll 10$)
 - study gravitational waves associated with gamma-ray bursts and other astrophysical explosions (< 10)
 - study merger history of galaxies, understand evolution of supermassive black holes ($\sim 15-20$)
 - map and probe black hole spacetime ($\sim 15-20$)
 - study stochastic background, phase transitions in the early universe, and possible indications of string theory (> 20)
- **In the mean time theoretically**
 - study of dynamics of highly non-linear spacetimes
 - foundations for space-time mapping and horizon probing
 - foundations for study quantum mechanics using gravitational-wave experiments ...

How small is 10^{-18} m? How is this possible?



Quantum Mechanics



- Heisenberg Uncertainty Principle: **position and momentum cannot be determined simultaneously**

$$\hbar = 10^{-34} \text{ Joule} \cdot \text{sec}$$

“Standard Quantum Limit”

- Measurement of mirror location at two separate times

$$\Delta X_{\text{tot}} = \Delta X + \tau \frac{\Delta P}{M} \geq 2\sqrt{\frac{\tau \Delta X \Delta P}{M}} \sim \sqrt{\hbar \tau / M}$$

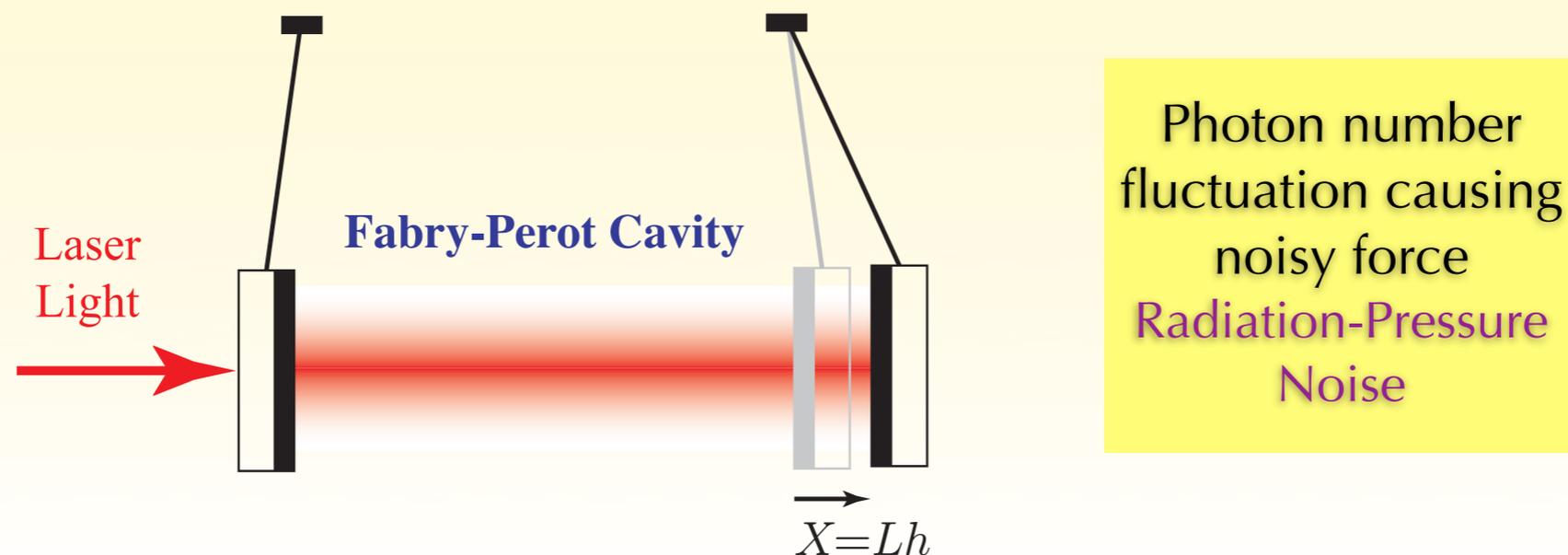
error in initial location

error in initial speed

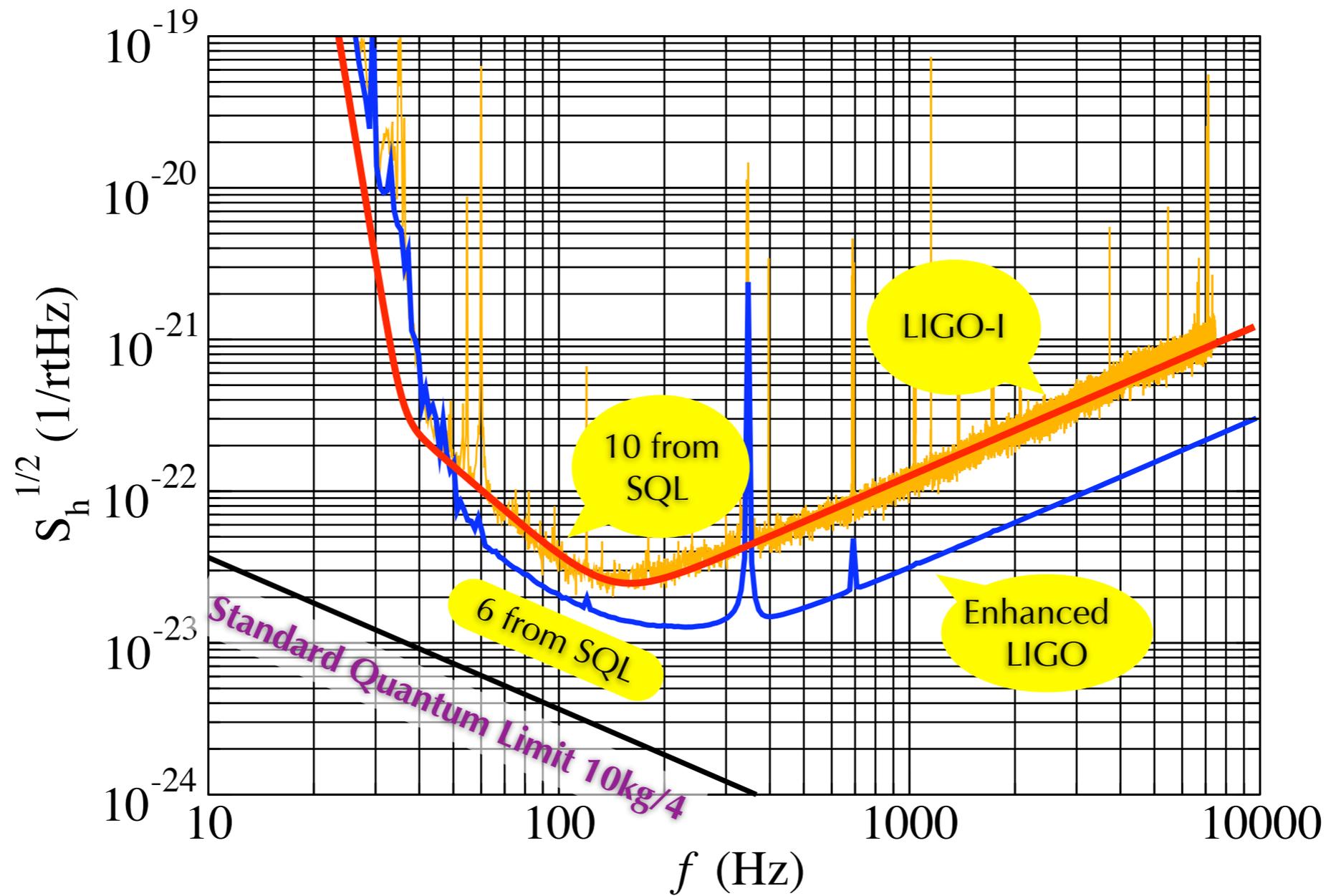
- For $M=10$ kg and $\tau = 0.01$ second

$$\Delta X_{\text{tot}} > 10^{-19} \text{ m}$$

- In reality, this Limit will be imposed by Radiation-Pressure Noise

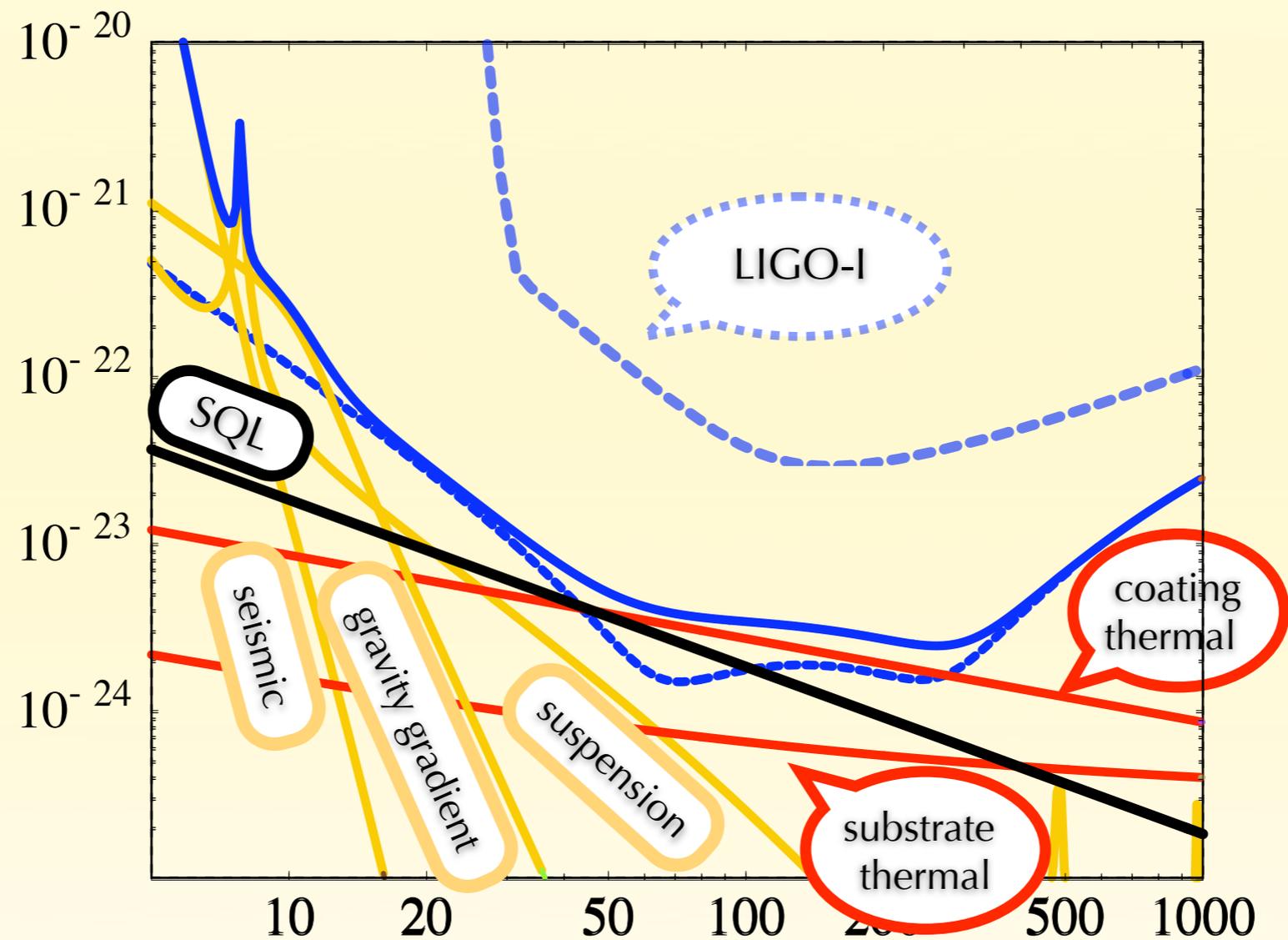


“Standard Quantum Limit”



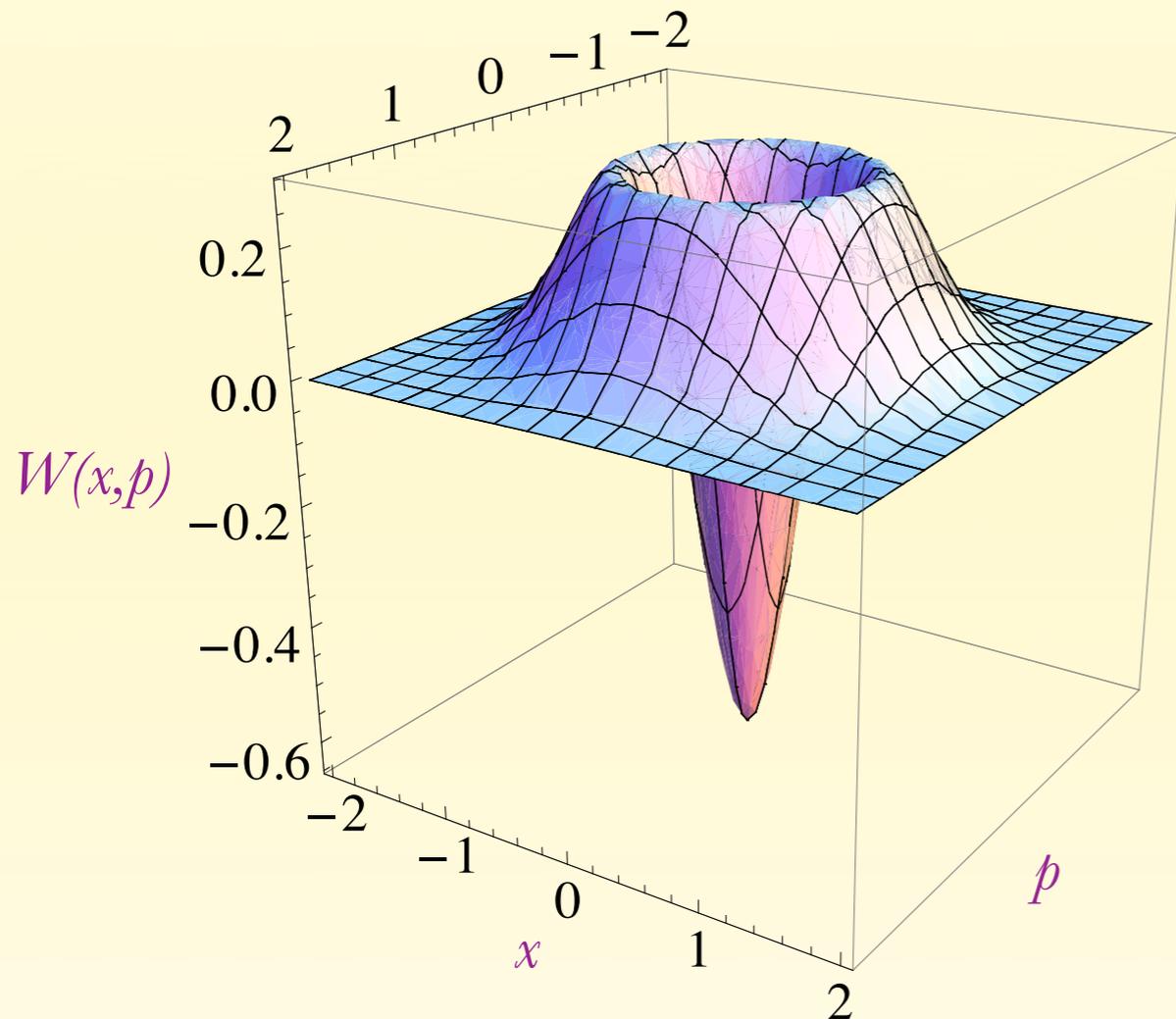
“Standard Quantum Limit”

- Advanced LIGO will “touch” the SQL
- Various prototype interferometers will *reveal* before Advanced LIGO

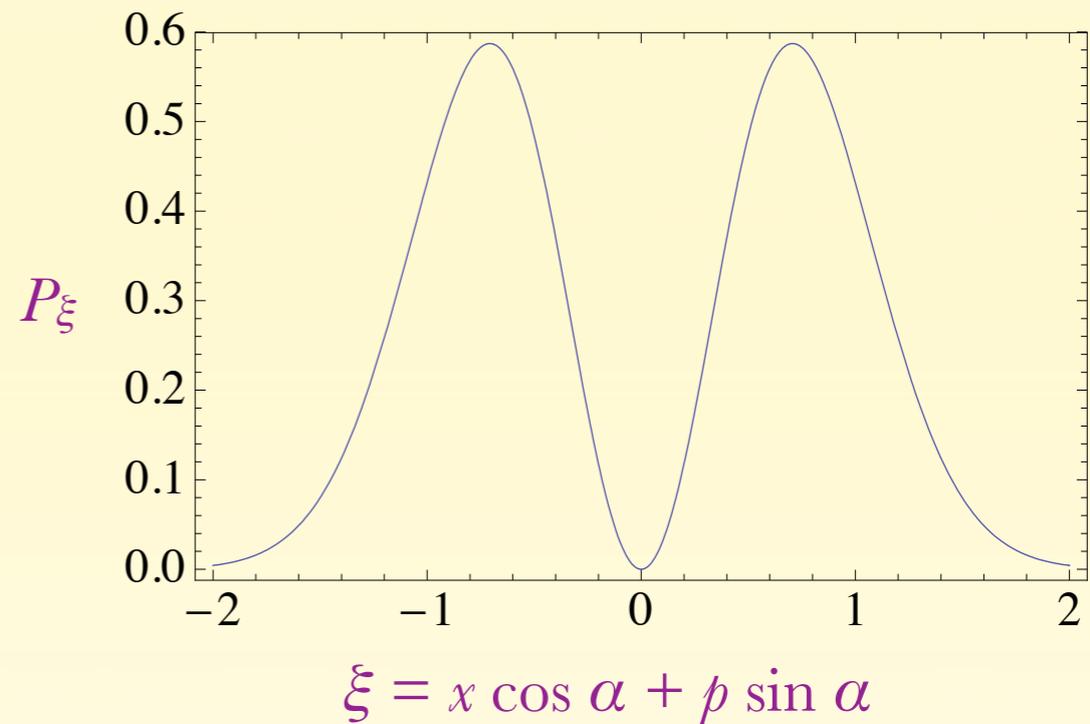


Macroscopic Quantum Mechanics

- With **classical noises** below the Standard Quantum Limit, light can be used to **create** and **probe** quantum mechanical states of mirrors
- Example, creation of a quantum state with **non-positive effective joint probability distribution** (**Wigner Function**) among (x,p)



effective joint distribution



marginal distribution

There is no classical correspondence!!